저작자표시-비영리-변경금지 2.0 대한민국

이용자는 아래의 조건을 따르는 경우에 한하여 자유롭게

- 이 저작물을 복제, 배포, 전송, 전시, 공연 및 방송할 수 있습니다.

다음과 같은 조건을 따라야 합니다:

저작자표시. 귀하는 원저작자를 표시하여야 합니다.

비영리. 귀하는 이 저작물을 영리 목적으로 이용할 수 없습니다.

변경금지. 귀하는 이 저작물을 개작, 변형 또는 가공할 수 없습니다.

- 귀하는, 이 저작물의 재이용이나 배포의 경우, 이 저작물에 적용된 이용허락조건을 명확하게 나타내어야 합니다.
- 저작권자로부터 별도의 허가를 받으면 이러한 조건들은 적용되지 않습니다.

저작권법에 따른 이용자의 권리는 위의 내용에 의하여 영향을 받지 않습니다.

이것은 이용허락규약(Legal Code)을 이해하기 쉽게 요약한 것입니다.

Disclaimer
Experimental Study of Local Scouring
at the Downstream of River Bed Protection

하천 하상보호구조물 하류부에서
국부세굴에 관한 실험적 연구

2016 년 2 월

서울대학교 대학원
건설환경공학부
박 성 원
ABSTRACT OF DISSERTATION

Experimental Study of Local Scouring
at the Downstream of River Bed Protection

by Sung Won Park

Doctor of Philosophy in Civil and Environmental Engineering
Seoul National University

Professor Jin Hwan Hwang, Advisor

Local scouring at the downstream of the river bed protection is one of the most important parts of the design criteria and sustainable management of the upstream hydraulic structures, such as dam spillway, gated or fixed weir. Especially, bed erosions in the vicinity of hydraulic structures and temporal development of maximum scour depth can threaten the safeties of hydraulic structures. From the previous researches, it has been known that dominant factors on local scouring were temporal development of the scour depth, initial flow and turbulent characteristics and properties of the river bed materials from the numerical and experimental approaches. However inappropriate the assumptions of previous researches and limitation of the measurement and monitoring caused the application of various empirical coefficients and scour prediction.
In this study, physical tests of the local scouring at the downstream of the fixed bed were conducted with movable bed materials with advanced laboratory facilities. Experimental approaches were focused on the temporal evolution of scoured hole and flow and turbulence characteristics in it at each time step in order to analyze the countermeasure of the excessive losses of the bed materials near the longitudinal transition. From the temporal change of the bed elevation at each time step, the empirical relationships between temporal change of the maximum scour depth and hydraulic conditions were concluded and can be used prediction of the value of the maximum scour depth. Especially depth averaged relative turbulence intensity at the longitudinal transition of bed and bed shear stress were revealed the dominant factors on the temporal change and equilibrium value of the maximum scour depth. To analyze the flow and turbulence characteristics in the stabilized scoured hole, similar physical process near the backward facing step were conducted with using the PIV and ADV measurement system. High resolution PIV system was helpful to analyze the flow pattern near the step and results of the 3-D ADV system were postprocessed with despiking method and ensemble averaging which was based on consideration of the integral time scale. With the analysis of the flow and turbulence results in the stabilized scoured hole, occurrence of the reversal flow and turbulent shear layer near the scoured hole was revealed to be dominant on the additional bed losses from the bed.

To find the appropriate countermeasure of the maximum scour depth, additional tests with mesh grid generated turbulent flow near the transition were conducted with same condition of the upstream water supply and water depth at the end of the laboratory flume. Results of the larger values of the depth averaged relative turbulence intensity were concluded the detention of the temporal change of scour depth and decrease of the equilibrium-maximum scour depth. Empirical equations which were suggested in this study, can be used to predict
the maximum scour depth with well-known hydraulic parameters. And they can be also applied to be the quantitative index of improvement and design of the river bed protection for the less erosion of the bed materials near the river bed protection.

**keywords:** Local Scouring, River Bed Protection, Depth-averaged Relative Turbulence Intensity, Maximum Scour Depth, Bed Shear Stress, Turbulence Shear Layer, Mesh Grid Generated Turbulent Flow

*Student Number:* 2009-30231
TABLE OF CONTENTS

ABSTRACT OF DISSERTATION ................................................................................ i
LIST OF FIGURES .................................................................................................... vii
LIST OF TABLES ....................................................................................................... xii
LIST OF SYMBOLS .................................................................................................. xiii

CHAPTER 1. INTRODUCTION ................................................................................. 1
  1.1 Background ........................................................................................................ 1
  1.2 Objectives .......................................................................................................... 2
  1.3 Thesis Overview ................................................................................................ 3

CHAPTER 2. THEORETICAL BACKGROUNDS .................................................... 5
  2.1 Local Scouring and Equilibrium State .............................................................. 5
    2.1.1 Conceptual Model ....................................................................................... 5
    2.1.2 Temporal Development ............................................................................... 7
    2.1.3 Equilibrium State ...................................................................................... 13
  2.2 Mean and Turbulent Flow in Open Channel Flow ............................................. 18
    2.2.1 Bed Roughness Effects .............................................................................. 18
    2.2.2 Initiation of Motion ................................................................................... 23
    2.2.3 Backward Facing Step Flow ...................................................................... 24
  2.3 Estimation of Flow and Turbulence Properties ............................................... 27
    2.3.1 Despiking Method ..................................................................................... 27
    2.3.2 Integral Time Scale and Ensemble Averaging ............................................. 29
    2.3.3 Mean and Turbulent Flow .......................................................................... 33
2.3.4 Bed Shear Stress........................................................................................................ 37

CHAPTER 3. LABORATORY EXPERIMENTS................................................................. 44

3.1 Experimental Setup .................................................................................................. 44
  3.1.1 Experimental Flume .......................................................................................... 44
  3.1.2 Water Supply and Control............................................................................... 49

3.2 Experimental Measurement ................................................................................... 53
  3.2.1 Measuring Apparatus....................................................................................... 53
  3.2.2 Experimental Conditions .............................................................................. 62
  3.2.3 Experimental Procedure.............................................................................. 62

CHAPTER 4. EXPERIMENTAL RESULTS AND ANALYSIS ...................................... 67

4.1 Flow and Turbulence Structures at the Transition................................................. 67
  4.1.1 Characteristics of Mean and Turbulent Flow .............................................. 67
  4.1.2 Characteristic Length Scale ....................................................................... 107

4.2 Temporal Development of Local Scour Hole ....................................................... 116
  4.2.1 Scour Test ...................................................................................................... 116
  4.2.2 Dimensions of Scoured Hole ...................................................................... 116
  4.2.3 Normalized Maximum Scour Depth ........................................................... 123
  4.2.4 Equilibrium-maximum Scour Depth .......................................................... 132

4.3 Flow and Turbulence in Scoured Hole ................................................................. 134
  4.3.1 Flow Separation and Turbulent Shear Layer.............................................. 134
  4.3.2 Bed Shear Stress in Scoured Hole............................................................. 137
  4.3.3 Energy Dissipation Rate .............................................................................. 142
4.3.4 Flow and Turbulence Distribution in the Scoured Hole ............................ 146

CHAPTER 5. LOCAL SCOURING WITH MESH GRID GENERATED TURBULENT FLOW.............................................................................................................. 155

5.1 Experimental Setup .................................................................................. 155
5.2 Comparison of Flow and Turbulence at the Transition ............................. 155
5.3 Comparison of Local Scouring ................................................................. 160

5.3.1 Temporal Development of Local Scour Hole ....................................... 160
5.3.2 Maximum Scour Depth ...................................................................... 160

CHAPTER 6. FUNCTIONAL RELATIONSHIPS BETWEEN DOMINANT FACTORS AND LOCAL SCOURING ......................................................... 165

6.1 Dominant Factors on Local Scouring .................................................... 165
6.2 Equilibrium-maximum Scour Depth ....................................................... 165

CHAPTER 7. SUMMARIES AND CONCLUSIONS .............................................. 167

REFERENCES ...................................................................................................... 169

ABSTRACT IN KOREAN ....................................................................................... 178
LIST OF FIGURES

Figure 1.1 Schematic Diagram of the Research Methodologies........................................ 4

Figure 2.1 Conceptual Model of Local Scoured Hole at the Downstream of Fixed Bed.... 6

Figure 2.2 Figure 2.2 Temporal Phases of Normalized Maximum Scour Depth (Hoffmans and Verheij, 1997) ................................................................. 8

Figure 2.3 Equilibrium State of Maximum Scour Depth and Flow Characteristics ...... 14

Figure 2.4 Shields Diagram (Revised by Hoffmans and Verheij, 1997) ....................... 16

Figure 2.5 Schematic Diagram of 2-D Tubulent Boundary Layer and Shear Stress on a Smooth Flat Plate (Daily and Harleman, 1966) ................................. 19

Figure 2.6 Classification of Hydraulic Roughness (Nezu and Nakagawa, 1993) ............ 22

Figure 2.7 Flow Separation and Turbulent Shear Layer in Abrupt Change of Bed Roughness ................................................................................................. 25

Figure 2.8 Flow Separation and Turbulent Shear Layer in Backward-facing Step Flow.. 25

Figure 2.9 Variation of Normalized Reattachment length Scale and the Reynolds Number in Backward-facing Step Flow in Open Channel ................................. 26

Figure 2.10 Auto-correlation and Integral Time Scale (Kundu and Cohen, 2008) ........ 30

Figure 2.11 Schematic Diagram of Ensemble Averaging with Using Integral Time Scale.............................................................................................................. 32

Figure 2.12 Functional Relationship between Dimensionless Stream-wise Velocity and Depth (Kundu and Cohen, 2008) ....................................................... 38

Figure 2.13 Vertical Distributions of Shear Stress in Open Channel Flow .................... 40

Figure 3.1 A photo of Flume from the Head Tank ....................................................... 45

Figure 3.2 Photos of Head Tank .............................................................................. 46
Figure 3.3 Photos of Flume from the Tail Gate .............................................................. 47
Figure 3.4 A Photo of Tailgate at the End of the Flume .................................................. 48
Figure 3.5 Schematic Diagram of Experimental Flume .................................................. 50
Figure 3.6 A Photo of Carriage and Auto-traverse System .............................................. 50
Figure 3.7 A Photo of Ultrasonic Flowmeter (Ultraflux, France) .................................... 51
Figure 3.8 A Photo of Water Supply Pump .................................................................... 51
Figure 3.9 A Photo of the Control Panel and Display ..................................................... 52
Figure 3.10 Schematic Diagram of the Pulse Coherent Processing of micro-ADV ......... 54
Figure 3.11 Bottom View of Vectrino Velocimeter (Nortek, 2009) ................................. 55
Figure 3.12 Schematic Diagram of Sweet Spot of the Vectrino (Nortek, 2009) ............... 55
Figure 3.13 Schematic Diagram of the PIV Measurement and Its Processing ................. 58
Figure 3.14 Photo and Specifications of PIV Laser Supply ............................................ 59
Figure 3.15 Photo and Specifications of Laser Filtering Optics ...................................... 59
Figure 3.16 Photo and Specifications of PIV Synchronizer ............................................ 60
Figure 3.17 Photo and Specifications of CCD Camera ................................................... 60
Figure 3.18 Schematic Diagram of PIV Arrangement and Measurement ....................... 61
Figure 3.19 Flow Chart of Data Acquisition ............................................................... 65
Figure 3.20 Results of the Sieve Analysis ...................................................................... 66
Figure 4.1 Schematic Diagram of Step Model and Measuring Setup .............................. 68
Figure 4.2 Linear Regression between the First Zero Crossing and Integral Time Scale . 76
Figure 4.3 Two-dimensional Vector Profiles in Backward-facing Step Flow ................. 78
Figure 4.4 Vertical Distributions of Stream-wise Direction Velocity in Backward-facing
Step Flow ..................................................................................................................... 79
Figure 4.5 Vertical Distributions of Water-depth Direction Velocity in Backward-facing
Step Flow .................................................................................................................................................. 80

Figure 4.6 Estimation of Bed Shear Stress with LOW Method......................................................... 82

Figure 4.7 Vertical Distributions of Stream-wise Turbulence Intensity in Backward-facing
Step Flow .................................................................................................................................................. 83

Figure 4.8 Vertical Distributions Water-depth direction Turbulence Intensity in Backward-facing
Step Flow ................................................................................................................................................. 84

Figure 4.9 Vertical Distributions of Turbulent Kinetic Energy in Backward-facing Step
Flow .......................................................................................................................................................... 85

Figure 4.10 Vertical Distributions of Reynolds Shear Stress in Backward-facing Step Flow
............................................................................................................................................................... 86

Figure 4.11 Estimation of Bed Shear Stress with RSS method (Run-1) in Backward-facing
Step Flow ................................................................................................................................................... 87

Figure 4.12 Longitudinal Distribution of Bed Shear Stress on Backward Facing Step .... 89

Figure 4.13 Schematic Diagram of 3-D Flow Measurement at Longitudinal Transition.. 91

Figure 4.14 Vertical Distribution of Stream-wise Velocity at Longitudinal Transition..... 92

Figure 4.15 Comparisons between Measured and Calculated Values of Normalized Stream-wise Velocity Distribution at Longitudinal Transition ......................... 94

Figure 4.16 Vertical Distribution of Normalized Turbulence Kinetic Energy at Longitudinal
Transition .................................................................................................................................................... 95

Figure 4.17 Comparisons between Measured and Calculated Values of Normalized
Turbulent Kinetic Energy Distribution at Longitudinal Transition......................... 97

Figure 4.18 Vertical Distribution of Normalized Reynolds Shear Stress at Longitudinal
Transition ................................................................................................................................................... 98

Figure 4.19 Comparisons between Measured and Calculated Values of Normalized
Scour Depth.......................................................................................................................... 133

Figure 4.34 Relationship between the Normalized Maximum Scour Depth and Time... 133
Figure 4.35 Snapshot of Visualization Particle in the Scoured Hole ......................... 135
Figure 4.36 Two-dimensional Vector Profiles in Scoured Hole ................................. 135
Figure 4.37 Distribution of Mean Flow and Turbulent Kinetic Energy in the Scoured
Hole .................................................................................................................................. 136
Figure 4.38 Temporal Change of Turbulence Properties near the Bed of Scoured Hole 138
Figure 4.39 Longitudinal Distribution of Energy Slope in the Scoured Hole .......... 144
Figure 4.40 Dimensionless Energy Slope and Hydraulic Radius in the Scoured Hole... 144
Figure 4.41 Error Analysis of Empirical Equation of Energy slope ......................... 145
Figure 4.42 Distribution of Measuring Grid Points in Scoured Hole (case B-Q35h144d12;
at t= 330 hrs. later)............................................................................................................ 147
Figure 4.43 Spiked Values of Velocity Data and Confidence Ellipses...................... 148
Figure 4.44 Filtered Values of Velocity Data and Confidence Ellipses..................... 149
Figure 4.45 Flow and Turbulence Distributions in Stablized Scoured Hole (case B-
Q35h144d12; at t= 330 hrs. later)..................................................................................... 150
Figure 5.1 Schematic Diagram of MGGT Flow and Scour Test............................... 156
Figure 5.2 Comparisons of LOW Methods at the Transition ................................. 157
Figure 5.3 Comparisons of TKE Methods at the transition...................................... 158
Figure 5.4 Temporal Change of Bed Profiles in MGGT Flow Condition............... 162
Figure 5.5 Comparisons of the Temporal Development of Maximum Scour Depth ..... 163
Figure 6.1 Empirical Relationship between Equilibrium Coefficient and the Normalized
Equilibrium-maximum Scour Depth............................................................................... 166
LIST OF TABLES

Table 2.1 Empirical Coefficients and Exponents in Equation 2.2 (Hoffmans and Verheij, 1997) .................................................................................................................. 12
Table 2.2 Turbulence Coefficient at the Transition (Hoffmans and Verheij, 1997) .......... 16
Table 3.1 Specification of Measuring Apparatus (Nortek, 2009) ................................. 56
Table 3.2 Experimental Conditions of Scour Test ............................................................ 63
Table 4.1 Hydraulic Condition of Step Model Test .......................................................... 68
Table 4.2 Estimation of Integral Time Scale (Run1_section1) ........................................... 70
Table 4.3 Comparison of Bed Shear Stress with two Methods in Backward-facing Step Flow .................................................................................................................. 89
Table 4.4 Experimental Conditions of Flow Test at Longitudinal Transition ............... 91
Table 4.5 Comparisons of Hydraulic Conditions and Bed Shear Stress with Various Estimation Methods at Longitudinal Transition .................................................. 102
Table 4.6 Flow Parameters and Results of Backward-facing Step Test ......................... 111
Table 4.7 Initial Parameters of Scour Test ...................................................................... 130
Table 4.8 Dominant Factors of Scour Test ................................................................. 131
Table 5.1 Experimental Conditions of MGGT Flow Test at Longitudinal Transition .... 156
Table 5.2 Hydraulic Conditions of MGGT Flow Test ................................................... 159
Table 5.3 Experimental Conditions of MGGT Scour Test ............................................ 161
# LIST OF SYMBOLS

**Latin Uppercase**

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>$A$</td>
<td>Cross section</td>
</tr>
<tr>
<td>$C$</td>
<td>Chézy friction coefficient</td>
</tr>
<tr>
<td>$C_{eq}$</td>
<td>Equilibrium Coefficient of Local Scouring</td>
</tr>
<tr>
<td>$C_r$</td>
<td>Integral coefficient (~8.5±15%)</td>
</tr>
<tr>
<td>$C_s$</td>
<td>Integral coefficient (~5.0±25%)</td>
</tr>
<tr>
<td>$D_s$</td>
<td>Sedimentological diameter</td>
</tr>
<tr>
<td>$E$</td>
<td>Expected values</td>
</tr>
<tr>
<td>$\text{Fr}$</td>
<td>Froude number</td>
</tr>
<tr>
<td>$K$</td>
<td>Calibration coefficient</td>
</tr>
<tr>
<td>$K_1$</td>
<td>Coefficient</td>
</tr>
<tr>
<td>$L_s$</td>
<td>Total length of scour hole (e.g. longitudinal length from the transition to the first initial bed elevation at each time step)</td>
</tr>
<tr>
<td>$L_1$</td>
<td>Longitudinal distance from the longitudinal transition ($x = 0$) to the location of $y_m$ at each time step</td>
</tr>
<tr>
<td>$P$</td>
<td>Pressure</td>
</tr>
<tr>
<td>$Q$</td>
<td>Water discharge</td>
</tr>
<tr>
<td>$\text{Re}$</td>
<td>Reynolds number</td>
</tr>
<tr>
<td>$\text{Re}_*$</td>
<td>Boundary Reynolds number</td>
</tr>
<tr>
<td>$R_h$</td>
<td>Hydraulic radius</td>
</tr>
<tr>
<td>$S_f$</td>
<td>Friction slope</td>
</tr>
<tr>
<td>$S_0$</td>
<td>Bed slope</td>
</tr>
</tbody>
</table>
$T_i$  Integral time scale
$U_c$  Critical mean velocity
$U_e$  External freestream velocity
$U_{m,e}$  Cross-sectional velocity of equilibrium state at $x = L_1$
$U_0$  Cross-sectional velocity

**Latin Lowercase**

$a$  Calibration exponent of density
$a_m$  Value of the maxima axe of PST method
$a_1$  Calibration coefficient of energy slope regression
$a_2$  Calibration exponent of energy slope regression
$b$  Calibration exponent of turbulence coefficient
$b_m$  Value of the minima axe of PST method
$c$  Calibration exponent of Froude number
$d$  Calibration exponent of Reynolds number
$d_s$  Diameter of sediment particle
$d_{50}$  Median size of $d_s$
$e$  Exponential
$f_{DW}$  Friction coefficient of Darcy Weisbach equation
$g$  Gravitational acceleration
$h_{m,e}$  Water depth of equilibrium state at $x = L_1$
$h_0$  Water depth at the longitudinal transition ($x = 0$)
$k$  Turbulent kinetic energy per unit mass
$k_b$  Turbulent kinetic energy at $u_* z/\nu = 70$
\( k_x \) Nikuradse’s equivalent roughness height

\( k_x \) Stream-wise directional turbulence intensity

\( k_y \) Span-wise directional turbulence intensity

\( k_z \) Water-depth directional turbulence intensity

\( k_0 \) Depth-averaged turbulent kinetic energy at the transition

\( q_{m,e} \) Discharge per unit width of equilibrium state at \( x = L_1 \)

\( q_0 \) Discharge per unit width at the longitudinal transition (\( x = 0 \))

\( r \) Correlation coefficient

\( r_0 \) Depth-averaged relative turbulence intensity

\( t \) Elapsed time

\( t_n \) Time step

\( t_1 \) Characteristic time at which \( y_m = h_0 \)

\( u \) Instantaneous velocity of stream-wise direction

\( u' \) Turbulence intensity of stream-wise direction

\( u^* \) Bed shear velocity

\( u^*_c \) Critical shear velocity

\( v \) Instantaneous velocity of span-wise direction

\( v' \) Turbulence intensity of span-wise direction

\( w \) Instantaneous velocity of water-depth direction

\( w' \) Turbulence intensity of water-depth direction

\( y_m \) Maximum scour depth (e.g. the first minimum value of bed elevation from the transition at each time step)
**Greek Uppercase**

$\Delta^n$ The $n^{th}$ derivatives

**Greek Lowercase**

$\alpha$ Turbulence coefficient

$\alpha_u$ Coefficient of stream-wise directional turbulence intensity

$\alpha_v$ Coefficient of span-wise directional turbulence intensity

$\alpha_w$ Coefficient of water-depth directional turbulence intensity

$\alpha_{uv}$ Calibration coefficient of stream-wise directional turbulence intensity

$\alpha_{uw}$ Coefficient of stream-wise directional turbulence intensity

$\alpha_0$ Coefficient of $k_0$

$\alpha_1$ Calibration Coefficient of $r_0$ with Froude number

$\alpha_2$ Calibration Coefficient of $r_0$ with Reynolds number

$\alpha_3$ Regression Coefficient of $r_0$

$\beta_1$ Calibration exponent $r_0$ with Froude number

$\beta_2$ Calibration exponent of $r_0$ with Reynolds number

$\delta$ Boundary layer thickness

$\delta^*$ Displacement thickness

$\theta$ Momentum thickness

$\theta_d$ Downstream scour slope (bed slope of the positions from $L_1$ to $L_s$)

$\theta_r$ Rotation angle of the principal axis in PST method

$\theta_u$ Upstream scour slope (bed slope from longitudinal transition to the $L_1$)
<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\kappa$</td>
<td>Von Kármán Coefficient</td>
</tr>
<tr>
<td>$\gamma$</td>
<td>Calibration exponent</td>
</tr>
<tr>
<td>$\mu$</td>
<td>Dynamic viscosity of water</td>
</tr>
<tr>
<td>$\nu$</td>
<td>Kinematic viscosity of water</td>
</tr>
<tr>
<td>$\rho_w$</td>
<td>Density of water</td>
</tr>
<tr>
<td>$\psi_c$</td>
<td>Shields’ parameter</td>
</tr>
<tr>
<td>$\sigma$</td>
<td>Standard deviation</td>
</tr>
<tr>
<td>$\lambda$</td>
<td>Characteristic length scale</td>
</tr>
<tr>
<td>$\lambda U$</td>
<td>Universal threshold term</td>
</tr>
<tr>
<td>$\xi_i$</td>
<td>Random variable</td>
</tr>
<tr>
<td>$\tau$</td>
<td>Time lag</td>
</tr>
<tr>
<td>$\tau_0$</td>
<td>Bed shear stress</td>
</tr>
<tr>
<td>$\tau_{0,RSS}$</td>
<td>Bed shear stress using vertical distribution of the Reynolds shear stress</td>
</tr>
</tbody>
</table>
CHAPTER 1
INTRODUCTIONS

1.1 Backgrounds

Hydraulic structures, such as spillway of dam, culvert and weir in rivers and streams are generally built with additial structures of appropriate scales and shapes. Those additional structures are called as bed protection and distinguished with energy dissipation, stilling basin, apron, and end sill. All of them have their function and play important roles to reduce the excessive losses of bed materials and convert the hydraulic jump or jet flow into stabilized flow patterns (USBR, 1984; USBR, 1987, USACE, 1987; USACE, 1992; CIRIA, 2007).

In most conditions of flow and sediment transport in field, higher turbulent flow is generated due to the constriction of the channel width and depth, control of the water discharge from the upstream. Therefore, bed protections are often constructed in order to protect the structures and also river bed. Even though the bed protections are setup, excessive loss and erosion of bed materials are occurred locally and frequently. This erosion is called as the local scour hole and it can threaten the safety of the upstream structures and cause the failure of the upstream structures. Therefore, prediction and prevention of the local scouring should be performed with consideration of various situations (USACE, 1987; USACE, 1992; CIRIA, 2007). Recently, functions and designs of hydraulic structures at the upstream of the bed protections become more complicated. However, limitations of design procedure of bed protection frequently made the local scouring and failure of the hydraulic structures also. Therefore previous design process also should be modified to overcome the limitations with considerations of physical process of local scouring.
1.2 Objectives

The purpose of this study is to reveal the physical mechanism of local scouring with experimental approaches and analyze the method to reduce the predicted scouring scales. And results of this experimental study can be helpful for estimation. Motivations of this study are as follows:

a) Dominant factors:

What are the dominant factors on local scour?
What are the research of dominant factors on local scouring recently revealed?
What made the local scouring with those factors?

b) Equilibrium State:

How can the local scouring reach to the equilibrium state?
Is it possible to estimate the equilibrium state of the maximum scour depth?
Is previously suggested equations to predict the equilibrium maximum scour depth appropriate and applicable to the most cases?

c) Flow Characteristics:

What are the hydraulic characteristics in the scoured hole?
Do they affect to the local scouring?

d) Engineering Application:

How can this research be applied to the field conditions and problems?
1.3 Overview of Thesis

Theoretical backgrounds of flow patterns in various boundary and sedimentological parameters were reviewed in Chapter 2. And experimental setup and concepts of the tests were explained in Chapter 3 with measuring apparatus and research procedures. Chapter 4 consists of two parts. Firstly, temporal changes of local scouring were analyzed with experimental results. And secondly, flow and turbulence characteristics, which can be dominant on sediment transport in the stabilized scoured were measured and compared with the scour process. And the MGGT flow condition, which can be a new concept of the countermeasure against the local scouring at the downstream of the fixed bed, were described and tested in Chapter 5. Dominant factors, which were revealed in Chapter 4 and 5 were combined as the normalized scales of the scouring in Chapter 6. Lastly, concise conclusions and summaries of this study was decribed in Chapter 7. Brief information of the methodologies of this study was schematized in Figure 1.1.
Figure 1.1 Schematic Diagram of the Research Methodologies
CHAPTER 2
THEORETICAL BACKGROUNDS

2.1 Local Scouring and Equilibrium State

2.1.1 Conceptual Model

Local scouring results directly from the impact of the structure and its operation on the flow and types of scour can be distinguished into jet scour, constriction scour, bend and bank scour, and etc. with sediment supply from the upstream or not. Scour process and notations of this study were schematized in Figure 2.1. \( L_s \) and \( y_m \) are the total length of scour hole (e.g. longitudinal length from the transition to the first initial bed elevation at each time step) and the maximum scour depth (e.g. the first minimum value of bed elevation from the transition at each time step), respectively. \( L_1 \) is the longitudinal distance from the transition \((x = 0)\) to the location of \( y_m \) at each time step. And the bed slopes of \( L_1 \) and from \( L_1 \) to \( L_s \) \((\theta_u & \theta_d): \) upstream and downstream scour slope) respectively affect the stability of the upstream structures and were found to be reached an equilibrium state faster than the other dimensions (Hoffmans, 1993). Meanwhile, the eroded sediment particles from the bed are moved toward downstream and deposited randomly and this sediment transport can make upper dimensions of scour hole. Especially, \( y_m \) is the most important dimension for the design of upstream structures such as bed protection, and has been considered dominantly in previous researches (Breusers, 1966; Monsonyi and Schopppmann, 1968; Dietz, 1969; van der Meulen and Vinjé, 1975; Buchko et al., 1987; Hoffmans and Verheij, 1997; Balachandar and Kell, 1997; Amoudry and Liu, 2009; Termini, 2010).
$Q$: water discharge from the upstream of the flume (m/s$^3$)

$h_0$: water depth at the tailgate of the flume (m)

$\eta_0$: initial bed elevation (m)

$L$: total length of scour hole (m)

$y_m$: maximum scour depth (m)

$L_1$: longitudinal distance from the longitudinal transition ($x=0$) to the location of $y_m$ (m)

$\theta_u$: upstream scour slope (degree)

$\theta_d$: downstream scour slope (degree)

$t_n$: time step (hour)

Figure 2.1 Conceptual Model of Local Scouring at the Downstream of Fixed Bed
2.1.2 Temporal Development

Based on the clear-water (no sediment supply from the upstream) scour experiments by Breusers (1966) and Dietz (1969), Zanke (1978) suggested four phases of the temporal evolution of maximum scour depth (Figure 2.2): an initial phase, a development phase, a stabilization phase and an equilibrium phase.

In the initial phase of local scour, the flow to the movable bed is mostly uniform in the longitudinal direction and erosion capacity in this phase is the most severe. Breusers (1966) showed that some bed material near the upstream scour slope goes into suspension at the beginning of the scour process. And most of the suspended particles follow convectional paths within the primary flow and remain in suspension due to the internal balance between the upward diffusive and the downward flux due to the gravity dominantly. Also some of the sediment particles will be settled and resuspended owing to the large scale and frequency of bursts of the turbulent flow near the movable bed, while some particles with a jump height smaller than a defined saltation or reference height are transported as the bed load.

In the development phase, dimensions of scouring increase considerably with same shape. In other words, ratios of $L_1$ and $y_m$ at each time step in this phase are more or less constant. And values of $\theta_u$ reaches to the equilibrium state, but ones of $\theta_d$ changes slightly milder. Therefore, the values of the sediment transport in the upper part of the upstream scour slope is negligible, since the contribution of the sediment transport due to the instantaneous velocities in the downstream direction is approximately equal to the transport resulting from the instantaneous velocities in the upstream direction. Temporal change of normalized maximum scour depth was clearly revealed with power function in this phase.
Figure 2.2 Temporal Phases of Normalized Maximum Scour Depth

(Hoffmans and Verheij, 1997)
In the stabilization phase the evolution rate of the maximum scour depth decreases gradually. The erosion capacity in the vicinity and upstream part of $L_1$ are much smaller than downstream of the point of reattachment, so that the values of $L_s$ increase faster than those of $y_m$ at each time step. In the stabilization and equilibrium phase both $\theta_u$ and $y_m$ are mostly achieved. The equilibrium phase can be defined as the phase in which the dimensions of the scour hole do no longer change significantly (Zanke, 1978; Hoffmans and Verheij, 1997). However, each temporal phase does not have any quantitative boundary, so that they can be defined only with the laboratory measurement and field observation.

In the stabilization phase the evolution rate of the maximum scour depth decreases gradually. The erosion capacity in the vicinity and upstream part of $L_1$ are much smaller than downstream of the point of reattachment, so that the values of $L_s$ increase faster than those of $y_m$ at each time step. In the stabilization and equilibrium phase both $\theta_u$ and $y_m$ are mostly achieved. The equilibrium phase can be defined as the phase in which the dimensions of the scour hole do no longer change significantly (Zanke, 1978; Hoffmans and Verheij, 1997). However, each temporal phase does not have any quantitative boundary, so that they can be defined only with the laboratory measurement and field observation.

Since Breusers in 1966 conducted physical tests on local scour at the downstream of the fixed bed and suggested the temporal evolution of maximum scour depth in development phase, several hundreds of tests in which no sediment supply from the upstream were conducted by Mosonyi and Schoppmann (1968), Dietz (1969), van der Meulen and Vinjé (1975), Buchko et al. (1987), Hoffmans and Pilarczyk (1995), Balchandar and Kells (1997), and recently Termini (2011). Especially, Breusers (1966) suggested functional relationship between normalized maximum scour depth and time in development phase as follows:
\[ \frac{y_m(t)}{h_0} = \left( \frac{t}{t_1} \right)^\gamma \]  \hspace{1cm} (2.1)

in which \( t \) and \( t_1 \) are elapsed time and characteristic time at which \( y_m = h_0 \) respectively. The maximum scour depth at \( t \) is denoted as \( y_m \). And \( \gamma \) is the calibration exponent and also scouring rate (\( \cdot \)). The left side of Eq. 2.1 is normalized length scale and right side of the upper equation is normalized time scale. Therefore each term in both sides of the equation 2.1 should have same units. Also values and ranges of calibration exponent (\( \gamma \)) have been previously estimated as 0.27-0.35 by Mosonyi and Schoppmann (1968), 0.34-0.40 by Dietz (1969), 0.4-0.8 by van der Meulen and Vinjé (1975), 0.2-0.4 by Hoffmans and Verheij (1997).

However, one of the limitations of Breuser’s method is that it can be only applicable in the development phase of the temporal evolution of maximum scour depth (Hoffmans and Pilarczyk, 1995). Shortage on the prediction of scour development, because this method is drastically dependent on the calibration exponent. And also this method has an assumption that the length scale of largest eddy size is in the order of initial water depth, \( h_0 \). Therefore only the case, which equilibrium maximum scour depth is greater than the initial water depth, can use this method and acquire the reasonable accuracy on the prediction of it. Even the dimensions of largest eddy size for deep water conditions were suggested as those of the hydraulic structures, this method is not sufficient on most cases and problems of the local scouring and those prediction and appropriate characteristic length scale, which is dominant factor on local scouring near the transition, should be suggested (Hoffmans and Verheij, 1997).
Also the dependence of the characteristic time on the hydraulic conditions and material characteristics of channel bed has been investigated by several researchers (Breusers, 1966; Dietz, 1969; van der Meulen and Vinjé, 1975; Zanke, 1978; de Graauw and Pilarczyk, 1981). From those studies, $t_1$ could described by:

$$t_1 = \frac{Kh_0^2 \Delta^{1.7}}{(\alpha U_0 - U_c)^{4.3}}$$

(2.2)

in which $K$ is 330 hrs m$^{-3}$/s$^{4.3}$, $\alpha$ is turbulence coefficient ($= 1+3r_0$), $r_0$ is depth-averaged relative turbulence intensity at the transition ($= \sqrt{k_0/U_0}$), $k_0$ is depth-averaged turbulent kinetic energy at the transition, $U_c$ is critical mean velocity ($= u_{*c} C/\sqrt{g}$, m/s), $u_{*c}$ is critical shear velocity, which can be estimated from the Shields diagram, $C$ is Chézy friction coefficient, $g$ is gravitational acceleration ($= 9.81$ m/s$^2$), and $D_r$ is relative density of bed materials.

$$t_1 = \frac{h_0}{U_0} \frac{K_1 D_r^a}{\alpha_u^4 \text{Fr}^c \text{Re}^d}$$

(2.3)

Where, $U_0$ is cross-sectional velocity at the transition (m/s), $K_1$ ($= g^{-1.43} \rho^{-0.43}$) is coefficient (-), $\alpha_u$ is coefficient ($= \alpha - U_c/U_0$), Fr and Re are Froude number ($= U_0 \sqrt{gh_0}$) and Reynolds number ($= U_0 h_0/\nu$), $\nu$ is kinematic viscosity ($= \mu/\rho$, $10^{-6}$ m$^2$/s in 20 °C water), $\mu$ and $\rho_w$ are dynamic viscosity and density of water ($= 1$ t/m$^3$), and suggested values of empirical coefficients and exponents in equation 2.3 were compared in table 2.1.
Table 2.1 Empirical Coefficients and Exponents in Equation 2.2

(Hoffmans and Verheij, 1997)

<table>
<thead>
<tr>
<th>Researchers</th>
<th>( K_1 )</th>
<th>( a )</th>
<th>( b )</th>
<th>( c )</th>
<th>( d )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Breusers (1967)</td>
<td>0.94</td>
<td>1.62</td>
<td>4.0</td>
<td>2.70</td>
<td>0.30</td>
</tr>
<tr>
<td>Dietz (1969)</td>
<td>9.96</td>
<td>1.50</td>
<td>4.0</td>
<td>2.50</td>
<td>0.50</td>
</tr>
<tr>
<td>van der Meulen and Vinje (1975)</td>
<td>12.9</td>
<td>1.70</td>
<td>4.3</td>
<td>2.87</td>
<td>0.43</td>
</tr>
<tr>
<td>Zanke (1978)</td>
<td>-</td>
<td>1.33</td>
<td>4.0</td>
<td>2.67</td>
<td>0.33</td>
</tr>
<tr>
<td>De Graauw and Pilarczyk (1981)</td>
<td>17.1</td>
<td>1.70</td>
<td>4.3</td>
<td>2.87</td>
<td>0.43</td>
</tr>
</tbody>
</table>
2.1.3 Equilibrium State

Schematic diagram of equilibrium state of scour hole was described with concepts of the continuity equation in Figure 2.3. $q_0$ and $q_{m,e}$ are the discharge per unit width ($m^2/s$) at $x=0$ and $L_1$, respectively. $h_{m,e} (= h_0 + y_{m,e})$ is water depth at $x=L_1$.

Applying the continuity equation in the equilibrium state of the scoured hole,

$$U_0 h_0 = U_{m,e} h_{m,e} = U_{m,e} \left( h_0 + y_{m,e} \right)$$  \hspace{1cm} (2.4)

where $U_{m,e}$ is cross-sectional mean velocity at $x=L_1$.

Assuming the equilibrium state with Eq. 2.4, and then Eq. 2.4 can be written as:

$$\frac{y_{m,e}}{h_0} = \frac{U_0 - U_{m,e}}{U_{m,e}}$$  \hspace{1cm} (2.5)

Dietz (1969) applied $U_{m,e} = U_c / \alpha$ in Eq. 2.5 and suggested as follows:

$$\frac{y_{m,e}}{h_0} = \frac{\alpha U_0 - U_c}{U_c}$$  \hspace{1cm} (2.6)

$U_c$ in RHS of Eq. 2.6 can be estimated as follows:

$$U_c = 2.5 \sqrt{\psi D_g d_{s0} \ln \left( \frac{12 h_0}{k_s} \right)}$$  \hspace{1cm} (2.7)
Figure 2.3 Equilibrium State of Maximum Scour Depth and Flow Characteristics
where $\psi_c$ is Shields’ parameter and $k_s$ is Nikuradse equivalent roughness height (m) and can be calculated with consideration of hydraulic roughness as follows:

$$Re_* = \frac{u_*k_s}{v}$$  \hspace{1cm} (2.8)

where $Re_*$ is the boundary Reynolds number and $k_s$ equals to $3d_{50}$ (hydraulically rough, $Re_*$<4) and $k_s$ equals to $2d_{50}$ (hydraulically smooth, $Re_*$>100), respectively.

Also Shields’ parameter in Eq. 2.7 can be calculated from the Figure 2.4 with sedimentological diameter ($D_*$) as follows:

$$D_* = d_{50}\left(\frac{\Delta g}{\nu^2}\right)^{1/3}$$  \hspace{1cm} (2.9)

Using Eq. 2.6, 2.7, 2.8, and 2.9, Maximum scour depth in the equilibrium state can be predicted.

Additionally turbulence coefficient, $\alpha$ in Eq. 2.6 depends mostly on the upstream geometric characteristics and can be interpreted as the erosion capacity. And several empirical expressions for $\alpha$ have been suggested (Table 2.2). A value of $\alpha$ can be calculated with depth-averaged relative turbulence intensity, $r_0$ which can be calculated with turbulence kinetic energy and depth-averaged flow velocity as follows:

$$r_0 = \frac{\sqrt{k_0}}{U_0}$$  \hspace{1cm} (2.10)
Figure 2.4 Shields Diagram (Revised by Hoffmans and Verheij, 1997)

Table 2.2 Turbulence Coefficient at the Transition (Hoffmans and Verheij, 1997)

<table>
<thead>
<tr>
<th>Researchers</th>
<th>turbulence coefficient ($\alpha$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Dietz (1969)</td>
<td>$2r_0 + 2/3$ or $3r_0 + 1$</td>
</tr>
<tr>
<td>Popova (1981)</td>
<td>$0.87 + 3.25\text{Fr} + 0.3r_0$</td>
</tr>
<tr>
<td>Rossinsky (1956) &amp;</td>
<td></td>
</tr>
<tr>
<td>Blazejewski (1991)</td>
<td>$1.05 - 1.7$</td>
</tr>
</tbody>
</table>
where, $k_0$ is depth-averaged turbulence kinetic energy and can be calculated as follows:

$$k_0 = \frac{1}{h} \int_0^h k(z) \, dz$$

(2.11)

where, turbulence kinetic energy per mass ($k$) is usually defined as:

$$k = 0.5 \left( \overline{u'^2} + \overline{v'^2} + \overline{w'^2} \right)$$

(2.12)

with three dimensional turbulence intensity:

$$k_x = \sqrt{u'^2} \quad (= \text{stream-wise direction})$$

(2.13-a)

$$k_y = \sqrt{v'^2} \quad (= \text{span-wise direction})$$

(2.13-b)

$$k_z = \sqrt{w'^2} \quad (= \text{water-depth direction})$$

(2.13-c)

Also three dimensional turbulence intensity can be calculated with difference from instantaneous flow velocity and time-averaged flow velocity as follows:

$$u = \overline{u} + u', \quad v = \overline{v} + v', \quad w = \overline{w} + w'$$

(2.14)

$u$, $v$, $w$ are represented as stream-wise, span-wise, and water-depth directional flow velocity, respectively. And apostrophe denotes the standard deviation of 3-D flow velocity.
2.2 Mean and Turbulent Flow in Open Channel Flow

2.2.1 Bed Roughness Effects

a) Turbulent Boundary Layer

Bed roughness in open channel flow disrupts the laminar sublayer with frictional forces, which retard the motion of the fluid. The concept of a boundary layer is mostly due to Prandtl in 1904, who showed that the effects of friction within the fluid are significant only in a very thin layer close to the surface. The use of boundary layer theory has many important applications, such as the calculation of flow separation and skin friction drag.

Figure 2.5 presents a schematic showing the development of a vertical 2-D boundary layer on a smooth flat plate. The existence of the no-slip boundary condition at the wall retards the flow, resulting in a smooth stream-wise mean velocity profile \( U(z) \), which smoothly merges into the external freestream velocity field, \( U_e \). The boundary layer thickness \( \delta(x) \) is considered to be the location above the surface at which the local mean velocity is 99% of the freestream value. Experimentally it is found that the \( \delta(x) \) depends on the variables \( U, \rho, \mu \) and the position \( x \) along the plate. And with those variables, \( \delta \) is observed to be

\[
\delta \sim \frac{\mu x}{\rho U} \sim \frac{x}{\sqrt{\text{Re}_x}} \tag{2.15}
\]

However, \( \delta \) cannot be established with precision since the point separating the boundary layer from the zone of negligible viscous influence is not clearly separated.
a) 2-D Tubulent Boundary Layer

b) Shear Stress

Figure 2.5 Schematic Diagram of 2-D Tubulent Boundary Layer and Shear Stress on a Smooth Flat Plate (Daily and Harleman, 1966)
Therefore, apart from the boundary layer thickness, there are two other relevant length scales, namely, the displacement thickness, $\delta^*$ and momentum thickness, $\theta$. The displacement thickness is the imaginary distance by which the wall would have to be displaced outward in a hypothetical frictionless flow so as to maintain the same mass flux as in the actual flow (Figure 2.6).

$\delta^*$ can be defined as follows:

$$
\rho U_e \delta^* = \rho \int_0^h (U_e - u) \, dz \quad (2.16-a)
$$

$$
\delta^* = \int_0^h \left( 1 - \frac{u}{U_e} \right) \, dz \quad (2.16-b)
$$

The flow retardation within $\delta$ also causes a reduction in the rate of momentum flux. It is useful to define a momentum thickness, $\theta$ as an imaginary layer of fluid of velocity $U$ for which the momentum flux rate equals the reduction caused by the vertical distribution of velocity (Daily and Harleman, 1966; Kundu and Cohen, 2008).

$\theta$ is defined by

$$
\rho \theta U_e^2 = \rho \int_0^h (U_e u - u^2) \, dz \quad (2.17-a)
$$

$$
\theta = \int_0^h \frac{u}{U_e} \left( 1 - \frac{u}{U_e} \right) \, dz \quad (2.17-b)
$$

Upper length scales are caused by bed roughness, which can make a turbulent fluctuation from the bed and were described with respect to the bed roughness in detail.
b) Bed Roughness

Bed roughness in open channel flow can be categorised as a complex boundary condition (Tachie et al., 2004). As mentioned earlier, the main effect of bed roughness is to increase the turbulence in vicinity of bed roughness elements. And the roughness properties such as friction coefficient, roughness height, and thickness of turbulent layer in uniform flow were widely researched by previous studies and mostly considered to analyze the mean and turbulent flow in open channel. However, no single formula cannot describe the velocity profiles over its total thickness, $\delta$. Therefore, according to the value of $Re^*$ (described in Eq. 2.8), hydraulical roughness can be categorized in Figure 2.6. From the concept of the Prandtl’s mixing length theory, distribution of universal velocity in smooth wall was developed as follows:

$$\frac{u(z)}{u_*} = \frac{1}{\kappa} \ln \left( \frac{u_* z}{v} \right) + C_s$$

(2.18)

where, $\kappa$ is von Kármán coefficient ($\approx 0.4$) and $C_s$ is a integral coefficient (approximately 5; $\pm 25\%$).

Also, distribution of universal velocity in smooth wall was developed as follows:

$$\frac{u(z)}{u_*} = \frac{1}{\kappa} \ln \left( \frac{z}{k_s} \right) + C_r$$

(2.19)

where, $C_r$ is a integral coefficient (approximately 8.5; $\pm 15\%$).
Figure 2.6 Classification of Hydraulic Roughness (Nezu and Nakagawa, 1993)
2.2.2 Initial Motion of Sediment

Initial condition of sediment particle movement is based on the balance of the total forces, i.e. drag force, weight of sediment particle, lift force, and resistance force on sediment particle in water flows. Also geometric characteristics of sediment particle such as shape factor (ratio of longest and shortest length of sediment particle), and specific weight and median size of it affect initiation of motion. Especially the concept of shear stress on sediment particle has played a major role in the initiation of sediment transport. Shields (1936) expressed the critical shear stress for the initiation of motion as a relation between the nondimensional shear stress, \( \psi_c \) (also called the Shields parameter or the Shields entrainment function) defined as:

\[
\psi_c = \frac{u_{*c}^2}{\Delta gd_{50}}
\] (2.20)

Several researches have modified Eq. 2.20 with more scatters from many laboratory experiments and field measurements (Simões, 2014; Figure 2.4).

In the case of sediment transport with hydraulic structures in rivers and stream, significant difference between bed protection and river bed with movable sediment particles. Neglecting the effects due to adaptation to a new flow pattern, the effective friction factor can be represented by an arithmetic average of the each friction factors, i.e.:

\[
f_{\text{eff}} = \frac{f_{\text{smooth}} + f_{\text{rough}}}{2}
\] (2.21)
Several researches have been done for the flow with a serial roughness change. A smooth-to-rough change causes an overshoot in bed shear stress due to the stream-wise advection of water with a relative high velocity close to the bottom. And Vermaas (2008) have analyzed that a serial change in bed roughness gives caused to extra friction in comparison to the arithmetic mean friction factor calculated by equation 2.21 with experimental researches. Therefore, a serial roughness change is schematized here as an abrupt change (smooth to rough bed) in bed roughness in stream-wise direction (Figure 2.7). Substantially larger value of turbulent layer thickness will be appeared and cyclic motion of flow and turbulence will also appear in this layer.

2.2.3 Backward Facing Step Flow

Steady and uniform stream flow past an abrupt change of the bed elevation (i.e. backward-facing step flow) has been researched by many researchers, such as Nakagawa and Nezu (1987), and Malley et al. (1991). Nakagawa and Nezu (1987) found that the instantaneous reattachment zone, which has a log-law distribution of stream-wise velocity, occurred over a distance of 3 to 9 times the step height, and gradually decreased as the Reynolds number becomes larger. Also Malley et al. (1991) revealed that the effective length scale of reattachment zone and step height and values of pressure from the transition to reattachment length scale were negative. To analyze the cyclic motion in the turbulent shear layer behind the step, both of these researches applied the Kelvin-Helmholtz model and kolk-boil vortices, respectively (Figure 2.8). Especially length scale of reattachment zone is 5-18 times of step height in the case of Re<10,000 and 5-8 times in the case of Re>20,000, respectively (Figure 2.9).
Figure 2.7 Flow Separation and Turbulent Shear Layer in Abrupt Change of Bed Roughness

Cyclic wake motions in the turbulent shear layer due to the abrupt increase of bed roughness

Figure 2.8 Flow Separation and Turbulent Shear Layer in Backward-facing Step Flow

Cyclic wake motions in the turbulent shear layer due to the backward facing step flow
Figure 2.9 Variation of Normalized Reattachment length Scale and the Reynolds Number in Backward-facing Step Flow in Open Channel
2.3 Estimation of Flow and Turbulence Properties

2.3.1 Despiking Method

Due to the many reasons, such as mistake of configuration, capture of the undesirably moving particles, and rapidly varied flow conditions, single and multiple points of the spiked signals of velocity data can be acquired with Acoustic Doppler Velocimetry as invalid data. Several methods to overcome these problems were suggested previously (Goring and Nikora, 2002; Doroudin, et al., 2010; Jesson, et al., 2012). Measured velocity data in the invalid region of the velocity of this study were detected with the PST (Phase-Space Thresholding) method which was suggested by Goring and Nikora (2002). This method iterates until the number of good fittable data becomes constant (or, equivalently, the number of new points identified as spikes falls to zero). Each iteration has the following procedures:

- Calculate the surrogates for the first and second derivatives from the following equations:

\[
\Delta u_i = \frac{(u_{i+1} - u_{i-1})}{2} \quad (2.22)
\]

\[
\Delta^2 u_i = \frac{(\Delta u_{i+1} - \Delta u_{i-1})}{2} \quad (2.23)
\]

- Calculate the standard deviations of all three variables, \(\sigma_u\), \(\sigma_{\Delta u}\), and \(\sigma_{\Delta^2 u}\), and then also estimate the expected maximum using the Universal criterion as follows:
\[ E \left( \left| \xi_i \right|_{\text{max}} \right) = \sqrt{2 \ln n} = \lambda_i \]  
(2.24-a)

\[ \lambda_i, \hat{\sigma} = \sqrt{2 \ln n} \hat{\sigma} \]  
(2.24-b)

- Calculate the rotation angle of the principal axis of \( \Delta^2 u_i \) versus \( u_i \) using the cross correlation as follows:

\[ \theta_r = \tan^{-1} \left( \sum u_i \Delta^2 u_i / \sum u^2_i \right) \]  
(2.25)

- Here, it should be noticed that for \( \Delta u_i, u_i \) and for \( \Delta^2 u_i \) versus \( u_i \), \( \theta \equiv 0 \) due to the symmetry.

- For each pair of variables, calculate the ellipse that has maxima and minima from 3 above. Thus, for \( \Delta u_i \) versus \( u_i \) the major axis is \( \lambda_i \sigma_{u_i} \) and the minor axis is \( \lambda_i \sigma_{u_i,\Delta u_i} \); for \( \Delta^2 u_i \) versus \( \Delta u_i \) the major axis is \( \lambda_i \sigma_{\Delta u_i} \) and the minor axis is \( \lambda_i \sigma_{\Delta^2 u_i} \); and for \( \Delta^2 u_i \) versus \( \Delta u_i \) the major and minor axes, \( a_m \) and \( b_m \), respectively, can be shown by elementary geometry to be the solution as follows:

\[ a_m^2 \cos^2 \theta + b_m^2 \sin^2 \theta = (\lambda_i \sigma_{\Delta u_i})^2 \]  
(2.26-a)

\[ a_m^2 \sin^2 \theta + b_m^2 \cos^2 \theta = (\lambda_i \sigma_{\Delta^2 u_i})^2 \]  
(2.26-b)

For each projection in phase space, identify the points that lie outside of the ellipse and replace them. Eliminated data sets were replaced with the method of the cubic polynomial interpolation of best fit through the 12 data points on either side of the eliminated data.
2.3.2 Integral Time Scale and Ensemble Averaging

Most researches related to the capability of acoustic Doppler velocimeters to resolve the flow turbulence has focused on definition of the noise level present in the signal and how it can be removed by many researches (García et al., 2005). With consideration of integral time scale, it is known that undesired fluctuations of velocity fluctuation can be stabilized in time domain.

A normalized autocorrelation function, \( r(\tau) \) of single value, \( u_i(t) \) at two times \( t \) and \( t+\tau \) can be defined as follows:

\[
 r(\tau) = \frac{u_i(t)u_i(t+\tau)}{u_i^2} \quad (2.27)
\]

The correlation coefficient, \( r(\tau) \) specifies how correlated \( u_i(t) \) and \( u_i(t+\tau) \) are to each other. A typical autocorrelation plot is shown in Figure 2.10. Under normal conditions value of \( r(\tau) \) goes to 0 as time lag, \( \tau \to \infty \), because a process becomes uncorrelated with itself after a long enough time. A measure of the width of the correlation function can be obtained by replacing the measured autocorrelation distribution by a rectangular height 1 and width \( T_i \), which is given by:

\[
 T_i = \int_0^\infty r(\tau) \, d\tau \quad (2.28)
\]
Figure 2.10 Auto-correlation and Integral Time Scale (Kundu and Cohen, 2008)
This is called as the integral time scale, which is a measure of the time over which is highly well-correlated with itself. In other words, \( T_i \) is a measure of the memory of the process (Kundu and Cohen, 2008). Obviously, \( r(\tau) \) equals one. Because the estimated values of it are not zero, O’Neill et al. suggested and compared the determinations of the integral time as:

- Integration over the entire available domain (theoretical method);
- Integration only up to the value where the autocorrelation function is a minimum, if the autocorrelation function has a negative region (Tritton, 1988);
- Integration only up to the first zero-crossing (Katul and Parlange, 1995); or
- Integration only up to the value where the autocorrelation function falls to \( 1/e \) (Tritton, 1988).

And third method (Katul and Parlange, 1995) to determine the integral time scale was applied in this research. After determining values of integral time scales from total data of 3-D instantaneous flow velocity, data of instantaneous flow velocity can be ensemble averaged with based on maximum value of determined integral time scales in three dimensional direction of measuring sensor with assumption of ergodic state (Figure 2.11). This method can remove the totally-uncorrelated or despiked values of instantaneous flow velocity data from the mistake on mis-alignment of physical setup, velocity range, sampling volume, transmit length, and relatively low level of SNR of measuring sensor. Therefore it can also make us to avoid the excessive calculation of turbulence properties.
Figure 2.11 Schematic Diagram of Ensemble Averaging with Using Integral Time Scale

Auto-correlation of 3-D velocity fluctuations
Integration of \( r(t) \) to the first zero crossing

Ensemble averaging velocity and turbulence properties at each determined integral time step

\[
\overline{U} = \frac{1}{n} \sum_{i=1}^{n} \overline{u_i}
\]

\[
\overline{u'} = \frac{1}{n} \sum_{i=1}^{n} \overline{u_i}
\]
2.3.3 Mean and Turbulent Flow

a) Mean Continuity Equation

Analyzing the flow characteristics in scoured hole, an appropriate method of ensemble averaging was suggested in previous chapter. Spatial distribution of time averaged velocity should be satisfied with continuity equation as follows:

\[
\frac{\partial}{\partial x_i} (U_i + u_i) = \frac{\partial U_i}{\partial x_i} + \frac{\partial \bar{u}_i}{\partial x_i} = \frac{\partial U_i}{\partial x_i} + \frac{\partial \bar{u}_i}{\partial x_i} = 0
\]  

(2.29)

where \( U_i \) is time averaged velocity and \( u_i \) is turbulent deviation of the \( U_i \). And subscript of \( i \) denotes the three dimensional direction. Using \( \bar{u}_i = 0 \), we can get:

\[
\frac{\partial U_i}{\partial x_i} = 0
\]  

(2.30)

which is a condition of the continuity equation for the mean flow. And with Eq. 2.30, the following formula is also suggested (Kundu and Cohen, 2008).

\[
\frac{\partial \bar{u}_i}{\partial x_i} = 0
\]  

(2.31)

Eq. 2.30 and 2.31 were used for the analysis of the time averaged values of mean flow and turbulence properties in the next chapter.
b) Turbulence Intensity

Nezu (1993) investigated the distribution of turbulent structure in smooth and rough bed open channel flows. Vertical distributions of normalized 3-D turbulence intensities with Eq. 2.13 were formulated in uniform flow condition as follows:

\[
\frac{k_x}{u_*} = \frac{\sqrt{u'^2}}{u_*} = \alpha_u \exp \left( -\frac{z}{b} \right) \quad (2.32-a)
\]

\[
\frac{k_y}{u_*} = \frac{\sqrt{v'^2}}{u_*} = \alpha_v \exp \left( -\frac{z}{b} \right) \quad (2.32-b)
\]

\[
\frac{k_z}{u_*} = \frac{\sqrt{w'^2}}{u_*} = \alpha_w \exp \left( -\frac{z}{b} \right) \quad (2.32-c)
\]

where \(\alpha_u, \alpha_v, \) and \(\alpha_w\) are coefficients (= 1.92, 1.34, 1.06, respectively). It is shown that the turbulent velocity fluctuations are order of bed shear velocity, \(u_*\). The stream-wise turbulence intensities, \(k_z/u_*\) are the largest, because the shear production initially feeds the energy into the \(u\)-component: the energy is subsequently distributed into the other lateral components \(v\) and \(w\) (Kundu and Cohen, 2008). The turbulent intensity initially rises as the wall is approached, however goes to zero right at the wall in a very thin wall layer as mentioned in previous chapter.

c) Depth-averaged relative turbulence intensity

For smooth and rough channel flows, Graf (1998) defined the vertical distribution of turbulent kinetic energy per mass with Eq. 2.32 from Nezu’s experimental relations as follows:
\[ k(z) = 0.5 \left[ k_x^2(z) + k_y^2(z) + k_z^2(z) \right] = k_b \exp \left( -\frac{2z}{h} \right) \] (2.33)

with

\[ k_b = 3.3 \bar{u}^2 \] (2.34)

where \( k_b \) is the turbulence energy at \( z^+ = u_z/v = 70 \). For hydraulically smooth and uniform flow conditions, Nezu (1977) found

\[ k_y(z) = \alpha_{uv} k_x(z) \] (2.35-a)

\[ k_z(z) = \alpha_{uv} k_x(z) \] (2.35-b)

where \( \alpha_{uv} = 0.71 \) and \( \alpha_{uv} = 0.55 \). Hoffmans and Verheij (1997) combined Eqs. 2.32, 2.33, 2.34, 2.35 and suggested depth-averaged value of turbulence energy as follows:

\[ k_0 = \frac{1}{h} \int_0^h k(z) dz = (\alpha_0 u_*)^2 \] (2.36)

\[ \alpha_0 = \sqrt{0.5 \left( 1 - \exp(-2) \right) \cdot 0.5 \alpha_u^2 \left( 1 + \alpha_{uv}^2 + \alpha_{aw}^2 \right)} = 1.2 \] (2.37)

where \( \alpha_0 \) is coefficient.

Normalized value of depth-averaged turbulence energy with Eq. 2.36 was suggested
in Eq. 2.10 and can also be estimated with traditional bed roughness coefficient Chézy’s $C$ as follows:

$$r_0 = \frac{\sqrt{k_0}}{U_0} = \alpha_0 \frac{u_*}{U_0} = \alpha_0 \frac{\sqrt{g}}{C}$$ (2.38)

d) Reynolds Shear Stress

By averaging the Navier-Stokes equation with Eq. 2.29, 2.30 and 2.31,

$$\frac{\partial U_i}{\partial t} + U_j \frac{\partial U_i}{\partial x_j} = -\frac{1}{\rho} \frac{\partial P}{\partial x_i} - \frac{\partial}{\partial x_j} u_i' u_j' + \nu \frac{\partial U_i}{\partial x_j}$$ (2.39)

which is known as Reynolds equation and $P$ is pressure. This equation can be rewritten in the form of a general equation of motion for a fluid as follows:

$$\frac{\partial}{\partial t} \rho U_i + \rho U_j \frac{\partial}{\partial x_j} = \frac{\partial}{\partial x_j} \left[ -P \delta_i^j - \rho u_i' u_j' + \mu \left( \frac{\partial U_i}{\partial x_j} + \frac{\partial U_j}{\partial x_i} \right) \right]$$ (2.40)

Where $\delta_i^j$ is the equivalent $3 \times 3$ matrix.

The first and second terms in LHS were represented the additional turbulent stress, i.e. the Reynolds shear stress. And for fully developed turbulence, the Reynolds shear stress approximately equals to vertical velocity gradient ($= \mu du/dz$).
2.3.4 Bed Shear Stress

Traditionally, to estimate the bed shear stress in open channel flow is one of the most important engineering works. Rashid (2010) suggested and compared six kinds of methods to estimate the bed shear stress from the data of flow velocity and turbulence characteristics in uniform open channel flow. In this study, 4 methods from the previous studies in uniform flow were introduced. And new concept of bed shear stress estimation was applied in non-uniform flow, i.e. flow condition in the scoured hole.

\[ \tau_0 = -\rho_\omega u^* w^* + \mu \frac{\partial u}{\partial z} \] (2.41)

where the first term in the LHS represents the turbulent effect and the second one is based on the viscosity near the bottom of the channel.

a) LOW (Law of the Wall) method

With log-distribution of normalized stream-wise velocity Eq. 2.19 previously described, bed shear velocity can be estimated with consideration least-square method. In this method, practical ranges (\(z^+\)) of fitting were proposed previously, such as 30 or 70-500 or 2000 by Daily and Harleman (1966), 30-500 by Monin and Yaglom (1965), and 30-300 by Kundu and Cohen (2008) (Figure 2.12). The range of \(z^+\) by Kundu and Cohen (2008) was selected in this study. LOW method have widely compared with newly-developed methods for the estimation of bed shear stress in many researches until now.

In this research, values of \(u^*\) and \(\delta^*\) were calculated with this method and compared with the others, which were introduced in the following chapters.
Figure 2.12 Functional Relationship between Dimensionless Stream-wise Velocity and Depth (Kundu and Cohen, 2008)
b) TKE (Turbulent Kinetic Energy) method

Graf (1998) suggested the Eq. 2.36 with using the results of Nezu and Nakagawa (1978). And Chézy coefficient can be also used to estimate the bed shear velocity with no experiment.

c) RSS (Reynolds Shear Stress) method

With experimental researches, vertical distribution of normalized Reynolds shear stress was proposed as follows:

\[
\frac{\bar{u}'\bar{w}'}{u_c^2} = \left( \frac{z}{h_0} - 1 \right) \tag{2.42}
\]

Bed shear stress can be extrapolated from the Eq. 2.41 with fitting the bed shear velocity. And if viscous shear stress,

\[
\tau_{0,RSS} = -\rho \overline{(u'w')}_{z=0} \tag{2.43}
\]

d) SVE method

Three methods proposed previously, can be applied only in the case of uniform flow condition. Therefore new estimation method of bed shear stress and velocity, which is applicable in the case of non-uniform flow condition, such as in the scoured hole, was suggested. Graf and Song (1995) suggested methods to estimate bed shear stress from the Saint Venant equation. 1-D Continuity and momentum equation are as follows respectively:
Figure 2.13 Vertical Distributions of Shear Stress in Open Channel Flow
\[
\frac{\partial h}{\partial t} + U \frac{\partial h}{\partial x} + h \frac{\partial U}{\partial x} = 0
\]  
(2.44)

\[
\frac{1}{A} \frac{\partial Q}{\partial t} + \frac{1}{A} \frac{\partial}{\partial x} \left( \frac{Q^2}{A} \right) + g \frac{\partial h}{\partial x} - g(S_0 - S_f) = 0
\]  
(2.45)

Substituted \( Q = AU \) into Eq. (2.41)

\[
\frac{\partial U}{\partial t} + \frac{\partial U^2}{\partial x} + g \frac{\partial h}{\partial x} - gS_0 + gS_f = 0
\]  
(2.46)

Divided by \( g \)

\[
\frac{1}{g} \frac{\partial U}{\partial t} + \frac{U}{g} \frac{\partial U}{\partial x} + \frac{\partial h}{\partial x} - S_0 + S_f = 0
\]  
(2.47)

Substituted \( \tau_0 = \gamma R_s S_f = \rho gh S_f \)

\[
\frac{1}{g} \frac{\partial U}{\partial t} + \frac{U}{g} \frac{\partial U}{\partial x} + \frac{\partial h}{\partial x} - S_0 + \frac{\tau_0}{h \rho g} = 0
\]  
(2.48)

Multiplied \( gh \) to both sides of equation

\[
\frac{h \partial U}{\partial t} + U h \frac{\partial U}{\partial x} + gh \frac{\partial h}{\partial x} - gh S_0 + \frac{\tau_0}{\rho} = 0
\]  
(2.49)
Substituted $\tau_0 = \rho u_*^2$ and then can be rewritten as follows:

$$u_*^2 = -\frac{h \partial U}{\partial t} - U h \frac{\partial U}{\partial x} - gh \frac{\partial h}{\partial x} + gh S_0$$  \hspace{1cm} (2.50)

Substituted $Fr = U_0/\sqrt{gh_0}$ and then can be rewritten as follows with Eq. (2.40) by Graf and Song (1995)

$$u_*^2 = gh S_0 - gh \frac{\partial h}{\partial x} \left(1 - Fr^2\right) + \left(U \frac{\partial h}{\partial t} - h \frac{\partial U}{\partial t}\right)$$  \hspace{1cm} (2.51)

With an assumption of steady state ($\partial h/\partial t = \partial U/\partial t = 0$) in the stabilized scoured hole (or at equilibrium state), third term in the right hand of Eq. (2.51) can be negligible as follows

$$u_*^2 = gh S_0 - gh \frac{\partial h}{\partial x} \left(1 - Fr^2\right)$$  \hspace{1cm} (2.52)

Assuming that variation of the water surface is negligible,

$$S_0(x_i) = \frac{\Delta \eta_i}{\Delta x_i} = \frac{\eta_i - \eta_{i-1}}{x_i - x_{i-1}}$$  \hspace{1cm} (2.53-a)
\[ \frac{\partial h}{\partial x} = \frac{h(x_i) - h(x_{i-1})}{x_i - x_{i-1}} \]
\[ = \frac{h_0 + \eta_0 - \eta(x_i) - (h_0 + \eta_0 - \eta(x_{i-1}))}{x_i - x_{i-1}} \]
\[ = \frac{\eta(x_{i-1}) - \eta(x_i)}{x_i - x_{i-1}} = -S_0 \]

Substituted Eq. (2.53-a, b) into Eq. (2.52),

\[ u_s = \sqrt{ghS_0(2 - Fr^2)} \] (2.54)

Therefore, bed shear velocity at each longitudinal position in the stabilized scoured hole (\(\Delta\eta/\Delta x > 0\) and \(Fr^2 < 2\)) is as follows:

\[ u_{s,j} = \sqrt{\frac{\Delta \eta}{\Delta x_j} (h_{0,j} + y_{x,j}) \left( 2 - \frac{U_0^2}{g(h_0 + y_{x,j})} \right)} \] (2.55)

e) Modified RSS method

LOW, RSS method are not applicable to the non-uniform flow condition due to the assumption. Therefore to estimate the bed shear velocity near the scoured bed, modified RSS method was suggested with considering the change of bed elevation in the scoured hole as follows:

\[ \tau_{0,MRSS} = \rho \left( u'w' \right)_{z=0} / \cos \theta_{x_i} \] (2.56)
CHAPTER 3
LABORATORY EXPERIMENTS

3.1 Experimental Setup

3.1.1 Experimental Flume

Laboratory experiments of this research were carried out in a glass-walled flume with tilting devices. Dimensions of the whole flume are 17.5 m long, 0.6 m wide, and 0.8 m deep in the Hydraulic and Coastal Engineering Laboratory of Seoul National University (Figure 3.1). Head tank for stabilization of water supply with dimensions of 2.9 m long, 1.2 m wide, and 1.5 m high has been connected to the beginning of the channel and two perforated panels and submerged wall, which can effectively remove any rotational flow and irregular water surface undulation induced from the circulating pipeline, so that the stabilized flow can be supplied in the flume have been setup (Figure 3.2). Both sides of wall and partial part of channel bottom have been made of 8 mm and 12 mm thick glasses, respectively. A pair of sump tanks for water supply, storage and sediment entrapment were installed below the flume bottom and channel end, respectively and they were connected with a closed conduit (Figure 3.3). Especially transparent glassed bottom allowed the laser sheet to be shone from below the flume bottom. The flume was reinforced and supported by painted steel frameworks. Open channel for measurement was made with dimensions of 15.0 m long, 0.6 m wide, and 0.8 m wide. At the end of the channel, sluice gate which is made of a steel plate has been setup for controls of water surface elevation with motor operating system (Figure 3.4).
Figure 3.1 A photo of Flume from the Head Tank
a) Side View of Head Tank

b) Perforated Panels in the Head Tank

Figure 3.2 Photos of Head Tank
a) A View from Right Side of Tail Gate

b) A View from left side of Tail Gate

Figure 3.3 Photos of Flume from the Tail Gate
Figure 3.4 A Photo of Tailgate at the End of the Flume
Figure 3.5 indicated the water supply and re-circulation system from the sump tanks into the test section of the flume. And information of the specific setup were described in detailed in following chapter. Additionally carriage on rails of the walls was setup for moving and mounting experimental appratus. And the auto-traverse system for positioning spanwise and water depth direction was mounted on the carriage. The two-axis autotraverse system can be controlled with the digital panel, which is connected with personal computer and the carriage can be moved and fixed manually. Also the autotraverse has the riveting plate for the positioning measuring apparatus (Figure 3.6).

3.1.2 Water Supply and Control

Water discharge for experiments is totally circulating as follows: Water from the first water supply tank is supplied by a water supply pump through the trumpet-shaped suction pipe and the ultrasonic flowmeter has been setup in the middle of the water supply pipe (Figure 3.7). Three phased power pump can supply upto 0.04 cms of water discharge steadily (Figure 3.8). A perforated pipe which has been setup in the head tank, can supply stabilized discharge of water through a pair of perforated paneles and low weirs. Passing the channel, discharge of water can be caught in the second water supply tank and be delievered to the first water supply tank through the conneting rectangular culvert which has been setup 0.5 m high from the bottom of the tank. The ultrasonic flowmeter in the middle of 10 mm diameter pipe has ±15 m per second measuring range and ± 0.5 % or less accuracy and acquired value of velocity can be displayed on the integrated control panel with real time. On the control panel, flow and slope display, control valve of water discharge and control button of slope, and termination button were installed (Figure 3.9).
Figure 3.5 Schematic Diagram of Experimental Flume

Figure 3.6 A Photo of Carriage and Auto-traverse System
Figure 3.7 A Photo of Ultrasonic Flowmeter (Ultraflux, France)

Figure 3.8 A Photo of Water Supply Pump
Figure 3.9 A Photo of the Control Panel and Display
3.2 Experimental Measurement

3.2.1 Measuring Appratus

a) Velocimeter

Single-point measurements of flow velocity and bed elevation change were conducted with down-looking Vectrino with rigid stem (Nortek™). The Vectrino uses the Doppler Effect to measure flow velocity and turbulence with 4-beam down-looking probes. The Doppler effect (or Doppler shift) is the change in frequency of a wave (or other periodic event) for an observer moving relative to its source. It is named after the Austrian physicist Christian Doppler, who proposed it in 1842 in Prague. It is commonly heard when a vehicle sounding a siren or horn approaches, passes, and recedes from an observer. Compared to the emitted frequency, the received frequency is higher during the approach, identical at the instant of passing by, and lower during the recession (Figure 3.10).

For the 3-D flow data acquisition, a pulse is transmitted from the centre transducer, and the Doppler shift introduced by the reflections from suspended particles in the water, is picked up by the four receivers (Figure 3.11). Sweet spot of the flow observation is 50 mm from the central transducer of the sensor with based on the maximum values of correlation and SNR (sound to noise ratio, dB). Especially, the reliable values of 3-D flow velocity data can be acquired with adequate combination of velocity range (from 0.03 to 4.00 m/s), sampling volume (from 2.5 to 8.5 mm), and transmit length. Inadequate combination of them can make the spiked values of flow velocity data (Figure 3.12; Table 3.1; Nortek, 2009). Alignment of the sensor on the auto-traverse system was described in Figure 3.6 and configuration of it was explained in following chapter 4.
Figure 3.10 Schematic Diagram of the Pulse Coherent Processing of micro-ADV
Figure 3.11 Bottom View of Vectrino Velocimeter (Nortek, 2009)

Central transducer:
\[ \phi = 6 \text{ mm} \] ceramic disc Transmits at 10 MHz

4 receivers:
\[ 6 * 3 \text{ ceramic} \]

Flow direction

Figure 3.12 Schematic Diagram of Sweet Spot of theVectrino (Nortek, 2009)

Sampling volume:
optional from 2.5 to 8.5 (mm)

Sweet spot:
50 mm from the transducer
Table 3.1 Specification of Measuring Apparatus (Nortek, 2009)

<table>
<thead>
<tr>
<th>Specifications</th>
<th>values</th>
</tr>
</thead>
<tbody>
<tr>
<td>Sampling volume</td>
<td></td>
</tr>
<tr>
<td>Distance from the probe</td>
<td>50 mm (fixed value)</td>
</tr>
<tr>
<td>Diameter</td>
<td>6 mm</td>
</tr>
<tr>
<td>Cell size</td>
<td>-</td>
</tr>
<tr>
<td>Velocity range</td>
<td>± 0.01 ~ 4 m/s</td>
</tr>
<tr>
<td>Sampling rate</td>
<td>1 ~ 200 Hz</td>
</tr>
<tr>
<td>Accuracy</td>
<td>± 0.5 % of measured value ± 1 mm/s</td>
</tr>
<tr>
<td>Temperature</td>
<td>-4 ~ 40 ºC</td>
</tr>
</tbody>
</table>
b) PIV Measuring System

Particle Image Velocimetry, or PIV is an optical method to visualize fluid flows. PIV can measure the velocity of fluids and reveal fluid properties. Essentially for PIV measurement, the standard planar PIV system should be considered. PIV has been oftenly applied in aerodynamics and hydrodynamics to research how organisms swim, fly, and conduct fluids in the body and to design aircraft, submarines, cars, prosthetic hearts, etc. PIV refers to one of methods used in experimental fluid mechanics to determine instantaneous fields of the vectors by measuring the displacements of numerous fine tracer particles that accurately follow the motion of the fluid. Fundamental theory of the particle image capturing was schematized in Figure 3.13-a (Stella et al., 2001; Adrian and Jerry, 2010).

It consists of a double-pulsed laser, light-sheet-forming optics, particle seeding, a monoscopic (single-lens) camera, image digitization hardware, and a computer for data storage and analysis (Figure 3.13-b). For visualization of flow near step, four components have been used. A laser supply is 135 mJ dual Nd:YAG, specified with 532 nm wavelength and 15 Hz pulse rate. A digital camera with 2M resolution can capture the fluid motion with relatively large size of interrogation area. All of components can be synchronized for exchanging the signals of capturing commands and images with the synchronizer. Specification of components has been described in Figure 3.14-17.

In this research, PIV measurement was applied for flow visualization and turbulent thickness estimation in the backward facing step flow. Laser supply was setup on the carriage of the flume wall and CCD camera capture the particle movement on the platform. Injected laser became the planar laser sheet through the filtering optics. Laser sheet met the mirror and changed route to the top of the flume and then laser can emphasize motions of the reflected particles in water (Figure 3.18).
a) Displacement of Marked Particle (Adrian and Jerry, 2010)

\[
x_p(t + \Delta t) = x_p + \Delta x_p
\]

\[
x(t + \Delta t) = x + \Delta x
\]

b) Elements and Processes in a Planar Two-dimensional Particle Image Velocimetry

Figure 3.13 Schematic Diagram of the PIV Measurement and Its Processing
Specification: Wavelength(532 nm); Energy (135 mJ); Repetitation Pulse Rate (15 Hz); Pulse Duration (6–9 ns); Energy Stability (±3%); Timing Jitter (±2 ns); Beam Diameter (5 mm)

Figure 3.14 Photo and Specifications of PIV Laser Supply

Specification: Spherical Lens (FL= 500mm & 1000mm); cylindrical lenses (FL= -25 & -15 mm); Divergence angle (14, 25 degrees)

Figure 3.15 Photo and Specifications of Laser Filtering Optics
Specification: Computer control; External standalone type; Time Resolution (1 ns); Time Base (100MHz); External Trigger (TTL input: for phase-locked or single-trigger events); Communication (RS-232 to computer)

Figure 3.16 Photo and Specifications of PIV Synchronizer

Specification: Resolution (4M pixel resolution: 2048 x 2048); Pixel Size (7.4um x 7.4um); CCD Temperature (40°C); Dynamic Range (12-bit); Frame Rate (16 fps in Frame Straddling Mode); Frame Straddling Time (200 ns); Spectral Range (350 to 740nm); Quantum Efficiency (57 %); Binning Factor (1 to 12, horizontal and vertical); Protection Mask (Integrated protection mask for the CCD output circuit); Camera Interface (64-bit camera link); Included Lens( F-mount, Nikon 50mm F1.8 lens), Interface cables

Figure 3.17 Photo and Specifications of CCD Camera
Figure 3.18 Schematic Diagram of PIV Arrangement and Measurement
3.2.2 Experimental Conditions

The experimental conditions were consisted of two parts. The first part is preliminary test of flow measurement with abrupt change of bed elevation and roughness. Second one is scour test with no sediment supply from the upstream with two median sizes of sediment particle (0.6 and 1.2 mm). Additional information of each experimental conditions were explained in following chapters in detailed. Flow conditions of all experimental cases were described in Table 3.2.

3.2.3 Experimental Procedure

During scour tests, bed profiles at each time step were measured with Vectrino along the centerline of the flume. Measuring grid sizes of stream-wise direction were from 2 to 10 cm with consideration of noticeable change of bed elevations. Especially in the region of abrupt change of bed elevation, such as deposition ridge, grid sizes were smaller than in the region of gradually changed bed elevation. Dimensions of scoured hole, which were described in previous chapter 2, were converted from the data of bed profiles and continuously were measured until minimum value of bed elevation equals flume bottom elevation or gradient of minimum value of bed elevation nearly equals zero. At the moment of the upper condition ($\eta_{\text{min}} = -\eta_{\text{initial}}$ or $\Delta \eta \approx 0$), 3-D flow velocity were measured along the centerline. Measuring grid sizes of water-depth direction were 2 to 100 mm with based on the velocity fluctuation. 2-D mean flow velocity were used to describe the flow separation and recirculation in the scoured hole. And also distribution of turbulent properties were used to describe the turbulent shear layer and reattachment length scale in the scoured hole.
### Table 3.2 Experimental Conditions of Scour Test

<table>
<thead>
<tr>
<th>case number</th>
<th>Q</th>
<th>$h_0$</th>
<th>$d_{50}$</th>
<th>$U_0$</th>
<th>Fr</th>
<th>Re $\times 10^5$</th>
<th>$T$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Q20h120d12</td>
<td>0.020</td>
<td>0.120</td>
<td>1.2</td>
<td>0.28</td>
<td>0.30</td>
<td>0.24</td>
<td>345</td>
</tr>
<tr>
<td>Q30h150d12</td>
<td>0.030</td>
<td>0.150</td>
<td>1.2</td>
<td>0.33</td>
<td>0.34</td>
<td>0.33</td>
<td>314</td>
</tr>
<tr>
<td>Q30h120d12</td>
<td>0.030</td>
<td>0.120</td>
<td>1.2</td>
<td>0.42</td>
<td>0.45</td>
<td>0.36</td>
<td>434</td>
</tr>
<tr>
<td>Q35h120d12</td>
<td>0.035</td>
<td>0.120</td>
<td>1.2</td>
<td>0.49</td>
<td>0.53</td>
<td>0.42</td>
<td>142</td>
</tr>
<tr>
<td>Q35h144d12</td>
<td>0.035</td>
<td>0.144</td>
<td>1.2</td>
<td>0.41</td>
<td>0.42</td>
<td>0.39</td>
<td>510</td>
</tr>
<tr>
<td>Q30h145d12</td>
<td>0.030</td>
<td>0.145</td>
<td>1.2</td>
<td>0.35</td>
<td>0.35</td>
<td>0.34</td>
<td>717</td>
</tr>
<tr>
<td>Q20h125d06</td>
<td>0.020</td>
<td>0.125</td>
<td>0.6</td>
<td>0.27</td>
<td>0.24</td>
<td>0.24</td>
<td>700</td>
</tr>
<tr>
<td>Q35h120d06</td>
<td>0.035</td>
<td>0.120</td>
<td>0.6</td>
<td>0.49</td>
<td>0.53</td>
<td>0.42</td>
<td>120</td>
</tr>
<tr>
<td>Q35h150d06</td>
<td>0.035</td>
<td>0.150</td>
<td>0.6</td>
<td>0.39</td>
<td>0.32</td>
<td>0.39</td>
<td>330</td>
</tr>
<tr>
<td>Q32h120d06</td>
<td>0.030</td>
<td>0.150</td>
<td>0.6</td>
<td>0.44</td>
<td>0.49</td>
<td>0.38</td>
<td>200</td>
</tr>
</tbody>
</table>
In addition, as mentioned in chapter 2.3, three dimensional flow velocity near the scoured bed (z = 2 mm) were measured to calculate the bed shear stress. Data of Reynolds shear stress ($\overline{u'w'}$) from were converted into the bed shear stress ($-\rho\overline{u'w'}$) and also compared with critical shear stress from the Shields diagram.

Meanwhile, all data of the 3-D mean and turbulent flow were estimated with using ensemble averaged with based on the maximum values of integral time scale, which can be calculated with auto-correlation function of instantaneous velocity data as mentioned in chapter 2. As mentioned previously, undesired cyclic fluctuation and despiked values of instantaneous flow velocity could be stabilized and converted into the reliable data (Figure 3.19).

Size of particle in this experiments were selected with consideration of field conditions in 4 major river basins. Lee and Son (2011) measured the hydrological conditions and hydraulic characteristics in 4 major river basins (18 rivers and 37 sites) and estimated values of tractive forces. Median size of the bed materials in 15 sites (41 %) from 37 sites was in the ranges of ± 50 % and the values of the sedimentological diameter ($D_*$) of 25 sites (67.6 %) in 37 sites were in the ranges from 1 to 200. And the results of the sieve analysis of used bed materials in this study were in the ranges of distributions of Lee and Son (2012) (Figure 3.20).
Figure 3.19 Flow Chart of Data Acquisition
Figure 3.20 Results of the Sieve Analysis

a) case B \((d_{50} = 1.2 \text{ mm})\)

a) case C & D \((d_{50} = 0.6 \text{ mm})\)
CHAPTER 4
EXPERIMENTAL RESULTS AND ANALYSIS

4.1 Flow and Turbulence Structures at the Transition

4.1.1 Characteristics of Mean and Turbulent Flow

To analyze the dominant factors on local scouring, which were previously revealed, appropriate analysis of flow and turbulent characteristics with variation of bed elevation. In this chapter, preliminary test in the backward-facing step flow was conducted with single point measurement along the centerline. Sampling frequency of ADV and total duration of flow measurement were 50 Hz and 30 seconds, respectively at each measuring point. And then 3-D flow and turbulence at the stream-wise direction transition \((x = 0 \text{ m})\) were measured and analyzed with previously suggested methods.

a) Preliminary Test with Step Models

An acryllic model of backward-facing step flow was setup in flume. 3-D flow velocity at 4 sections were measured (Figure 4.1-a). Heights of the first step and second one were 0.035 m and 0.2 m, respectively. ADV was setup on the transversely middle of the auto-tranverse system and measuring position of the sensor was controlled with the value of the distance from the transmitter (Figure 4.1-b). Flow conditions of this preliminary test were described in Table 4.1. A value of water depth at the section 4 were same as 0.4 m and water discharge of Run-2 was two time as that of Run-1. Therefore values of cross sectional velocity and Froude number of Run-2 were two times as those of Run-1.
a) **Step Model and Measuring Sections**

![Diagram of Step Model and Measuring Setup](image)

b) **Measuring Setup (Front View)**

Figure 4.1 Schematic Diagram of Step Model and Measuring Setup

<table>
<thead>
<tr>
<th>Cases</th>
<th>Water discharge from the upstream (m³/s)</th>
<th>Water depth at the tailgate (m)</th>
<th>Cross sectional velocity (m/s)</th>
<th>Froude number (-)</th>
</tr>
</thead>
<tbody>
<tr>
<td>RUN-1</td>
<td>0.010</td>
<td>0.20</td>
<td>0.167</td>
<td>0.059</td>
</tr>
<tr>
<td>RUN-2</td>
<td>0.020</td>
<td>0.20</td>
<td>0.330</td>
<td>0.119</td>
</tr>
</tbody>
</table>
For appropriate analysis of the 3-D flow velocity, vertical distribution of the integral time scale based on the auto-correlation function were determined in Table 4.2. Vertical distance from the bottom, where the largest value were estimated, at section 1 and 2 were mostly near the maximum value of the vertical position. Meanwhile maximum values of integral time scale at section 3 were estimated in the middle of the vertical distribution such as from 0.03 to 0.12 m. In case of Run-1, range of the integral time scales were from 0.687 to 8.42 seconds and ranges of Run-2 were estimated from 0.840 to 10.93 seconds (Table 4.2). Integral time scale of stream-wise direction were nearly the maximum among the 3-D direction due to the magnitude of velocity fluctuation.

The first zero crossing time scale and integral time scale were compared in Figure 4.2. And linear relationship between the time to the first zero crossing and integral time scale were described as follows:

\[ T_i = a_i t_0 + b_i \] (4.1)

where \( t_0 \) is time to the first zero crossing from the auto-correlation function of 3-D flow velocity data. And \( a_i \) (0.03-0.22) and \( b_i \) (0.0003-0.002) were the calibration coefficients. With this values and distributions of integral time scale, we can decide how long enough measure the instantaneous flow velocity data with consideration of turbulence fluctuations and undesired excessive values of flow velocity, such as over 10 times of spatial mean velocity suddenly or over 10 times of negative values of stream-wise velocity. Also mentioned previously, mis-alignment and configuration of ADV can be modified with this consideration. In this study, 1500 samples in 30 second measuring duration is long enough than 5-10 times of the integral time scale at least.
Table 4.2-a) Estimation of Integral Time Scale (Run1_section1)

<table>
<thead>
<tr>
<th>depth (m)</th>
<th>Integral time scale (s)</th>
<th>Time to the first zero crossing (s)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$T_u$</td>
<td>$T_v$</td>
</tr>
<tr>
<td>0.003</td>
<td>0.591</td>
<td>0.213</td>
</tr>
<tr>
<td>0.005</td>
<td>0.420</td>
<td>0.977</td>
</tr>
<tr>
<td>0.01</td>
<td>1.09</td>
<td>7.45</td>
</tr>
<tr>
<td>0.015</td>
<td>2.96</td>
<td>0.452</td>
</tr>
<tr>
<td>0.02</td>
<td>0.751</td>
<td>1.020</td>
</tr>
<tr>
<td>0.025</td>
<td>3.86</td>
<td>0.273</td>
</tr>
<tr>
<td>0.03</td>
<td>1.216</td>
<td>0.270</td>
</tr>
<tr>
<td>0.035</td>
<td>1.33</td>
<td>1.681</td>
</tr>
<tr>
<td>0.04</td>
<td>3.11</td>
<td>1.002</td>
</tr>
<tr>
<td>0.045</td>
<td>2.08</td>
<td>0.315</td>
</tr>
<tr>
<td>0.05</td>
<td>2.01</td>
<td>0.287</td>
</tr>
<tr>
<td>0.06</td>
<td>1.875</td>
<td>0.304</td>
</tr>
<tr>
<td>0.07</td>
<td>7.91</td>
<td>0.263</td>
</tr>
<tr>
<td>0.08</td>
<td>0.280</td>
<td>0.305</td>
</tr>
<tr>
<td>0.09</td>
<td>0.315</td>
<td>6.75</td>
</tr>
<tr>
<td>Max.</td>
<td>7.91</td>
<td>7.45</td>
</tr>
</tbody>
</table>
### Table 4.2-b) Estimation of Integral Time Scale (Run1_section2)

<table>
<thead>
<tr>
<th>depth (m)</th>
<th>$T_u$</th>
<th>$T_v$</th>
<th>$T_w$</th>
<th>$t_u$</th>
<th>$t_v$</th>
<th>$t_w$</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.003</td>
<td>1.371</td>
<td>0.592</td>
<td>0.332</td>
<td>7.1</td>
<td>3.46</td>
<td>1.82</td>
</tr>
<tr>
<td>0.005</td>
<td>1.224</td>
<td>0.498</td>
<td>0.354</td>
<td>9.36</td>
<td>2.12</td>
<td>1.86</td>
</tr>
<tr>
<td>0.01</td>
<td>0.770</td>
<td>0.454</td>
<td>0.351</td>
<td>4.08</td>
<td>1.7</td>
<td>2.04</td>
</tr>
<tr>
<td>0.015</td>
<td>1.176</td>
<td>0.276</td>
<td>0.349</td>
<td>10.14</td>
<td>1.12</td>
<td>1.96</td>
</tr>
<tr>
<td>0.02</td>
<td>0.888</td>
<td>0.314</td>
<td>0.285</td>
<td>5.4</td>
<td>1.24</td>
<td>0.98</td>
</tr>
<tr>
<td>0.025</td>
<td>0.612</td>
<td>0.206</td>
<td>0.297</td>
<td>1.82</td>
<td>0.72</td>
<td>1.2</td>
</tr>
<tr>
<td>0.03</td>
<td>1.193</td>
<td>0.233</td>
<td>0.273</td>
<td>7.2</td>
<td>0.8</td>
<td>0.98</td>
</tr>
<tr>
<td>0.035</td>
<td>0.692</td>
<td>0.258</td>
<td>0.260</td>
<td>2.24</td>
<td>1.06</td>
<td>1.24</td>
</tr>
<tr>
<td>0.04</td>
<td>0.729</td>
<td>0.197</td>
<td>0.224</td>
<td>3.98</td>
<td>0.84</td>
<td>0.76</td>
</tr>
<tr>
<td>0.045</td>
<td>0.997</td>
<td>0.246</td>
<td>0.242</td>
<td>5.22</td>
<td>0.98</td>
<td>0.84</td>
</tr>
<tr>
<td>0.05</td>
<td>0.922</td>
<td>0.253</td>
<td>0.255</td>
<td>5.6</td>
<td>1.32</td>
<td>1.04</td>
</tr>
<tr>
<td>0.06</td>
<td>1.411</td>
<td>0.299</td>
<td>0.282</td>
<td>8.08</td>
<td>1.12</td>
<td>1</td>
</tr>
<tr>
<td>0.07</td>
<td>1.534</td>
<td>0.278</td>
<td>0.225</td>
<td>9.34</td>
<td>1.12</td>
<td>0.9</td>
</tr>
<tr>
<td>0.08</td>
<td>0.635</td>
<td>0.251</td>
<td>0.244</td>
<td>4.32</td>
<td>1.82</td>
<td>1</td>
</tr>
<tr>
<td>0.09</td>
<td>1.906</td>
<td>0.281</td>
<td>1.410</td>
<td>10.6</td>
<td>1.78</td>
<td>8.98</td>
</tr>
<tr>
<td>0.1</td>
<td>0.944</td>
<td>0.249</td>
<td>0.482</td>
<td>6.6</td>
<td>0.96</td>
<td>2.36</td>
</tr>
<tr>
<td>0.11</td>
<td>1.757</td>
<td>0.225</td>
<td>0.756</td>
<td>9.26</td>
<td>0.94</td>
<td>6.96</td>
</tr>
<tr>
<td>0.12</td>
<td>1.204</td>
<td>0.948</td>
<td>2.165</td>
<td>10.66</td>
<td>11.16</td>
<td>17.8</td>
</tr>
<tr>
<td>0.13</td>
<td>1.436</td>
<td>1.668</td>
<td>1.771</td>
<td>11.74</td>
<td>20.3</td>
<td>12.52</td>
</tr>
<tr>
<td>Max.</td>
<td>1.906</td>
<td>1.668</td>
<td>2.165</td>
<td>11.74</td>
<td>20.3</td>
<td>17.8</td>
</tr>
</tbody>
</table>
Table 4.2-c) Estimation of Integral Time Scale (Run1_section3)

<table>
<thead>
<tr>
<th>depth (m)</th>
<th>Integral time scale (s)</th>
<th>Time to the first zero crossing (s)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$T_u$</td>
<td>$T_v$</td>
</tr>
<tr>
<td>0.003</td>
<td>3.14</td>
<td>0.709</td>
</tr>
<tr>
<td>0.005</td>
<td>3.97</td>
<td>0.981</td>
</tr>
<tr>
<td>0.01</td>
<td>3.13</td>
<td>0.468</td>
</tr>
<tr>
<td>0.015</td>
<td>2.26</td>
<td>0.641</td>
</tr>
<tr>
<td>0.02</td>
<td>1.421</td>
<td>0.461</td>
</tr>
<tr>
<td>0.025</td>
<td>4.29</td>
<td>0.394</td>
</tr>
<tr>
<td>0.03</td>
<td>8.43</td>
<td>0.421</td>
</tr>
<tr>
<td>0.035</td>
<td>3.27</td>
<td>0.317</td>
</tr>
<tr>
<td>0.04</td>
<td>3.64</td>
<td>0.687</td>
</tr>
<tr>
<td>0.045</td>
<td>2.85</td>
<td>0.336</td>
</tr>
<tr>
<td>0.05</td>
<td>8.09</td>
<td>0.325</td>
</tr>
<tr>
<td>0.06</td>
<td>1.280</td>
<td>0.321</td>
</tr>
<tr>
<td>0.07</td>
<td>7.70</td>
<td>0.306</td>
</tr>
<tr>
<td>0.08</td>
<td>3.71</td>
<td>0.314</td>
</tr>
<tr>
<td>0.09</td>
<td>7.76</td>
<td>0.279</td>
</tr>
<tr>
<td>0.1</td>
<td>5.92</td>
<td>0.297</td>
</tr>
<tr>
<td>0.11</td>
<td>3.85</td>
<td>0.208</td>
</tr>
<tr>
<td>0.12</td>
<td>8.27</td>
<td>0.372</td>
</tr>
<tr>
<td>0.13</td>
<td>7.75</td>
<td>0.301</td>
</tr>
<tr>
<td>Max.</td>
<td>8.43</td>
<td>0.687</td>
</tr>
</tbody>
</table>
Table 4.2-d) Estimation of Integral Time Scale (Run2_section1)

<table>
<thead>
<tr>
<th>depth (m)</th>
<th>$T_u$</th>
<th>$T_v$</th>
<th>$T_w$</th>
<th>$t_u$</th>
<th>$t_v$</th>
<th>$t_w$</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.003</td>
<td>0.033</td>
<td>0.047</td>
<td>0.027</td>
<td>0.46</td>
<td>0.9</td>
<td>0.38</td>
</tr>
<tr>
<td>0.005</td>
<td>0.032</td>
<td>0.352</td>
<td>0.050</td>
<td>0.5</td>
<td>5.42</td>
<td>0.82</td>
</tr>
<tr>
<td>0.01</td>
<td>0.096</td>
<td>2.48</td>
<td>0.112</td>
<td>0.8</td>
<td>24.4</td>
<td>1.26</td>
</tr>
<tr>
<td>0.015</td>
<td>0.140</td>
<td>1.491</td>
<td>0.070</td>
<td>1.62</td>
<td>18.36</td>
<td>0.66</td>
</tr>
<tr>
<td>0.02</td>
<td>0.103</td>
<td>0.437</td>
<td>0.069</td>
<td>0.78</td>
<td>5.82</td>
<td>0.8</td>
</tr>
<tr>
<td>0.025</td>
<td>0.109</td>
<td>1.721</td>
<td>0.068</td>
<td>0.94</td>
<td>20.7</td>
<td>0.98</td>
</tr>
<tr>
<td>0.03</td>
<td>0.210</td>
<td>0.237</td>
<td>0.064</td>
<td>3.22</td>
<td>2.56</td>
<td>1</td>
</tr>
<tr>
<td>0.035</td>
<td>0.174</td>
<td>0.451</td>
<td>0.064</td>
<td>1.36</td>
<td>6.66</td>
<td>0.52</td>
</tr>
<tr>
<td>0.04</td>
<td>0.840</td>
<td>1.152</td>
<td>0.073</td>
<td>12.52</td>
<td>14.12</td>
<td>0.62</td>
</tr>
<tr>
<td>0.045</td>
<td>0.123</td>
<td>0.205</td>
<td>0.124</td>
<td>1.04</td>
<td>2.32</td>
<td>2.64</td>
</tr>
<tr>
<td>0.05</td>
<td>0.586</td>
<td>0.198</td>
<td>0.066</td>
<td>10.96</td>
<td>2.12</td>
<td>0.64</td>
</tr>
<tr>
<td>0.06</td>
<td>0.155</td>
<td>0.137</td>
<td>0.260</td>
<td>2</td>
<td>0.78</td>
<td>3.74</td>
</tr>
<tr>
<td>0.07</td>
<td>0.260</td>
<td>0.157</td>
<td>0.458</td>
<td>4.48</td>
<td>0.64</td>
<td>6.1</td>
</tr>
<tr>
<td>0.08</td>
<td>0.123</td>
<td>0.119</td>
<td>0.323</td>
<td>1.96</td>
<td>0.5</td>
<td>3.46</td>
</tr>
<tr>
<td>0.09</td>
<td>0.112</td>
<td>0.894</td>
<td>1.215</td>
<td>1.12</td>
<td>10.54</td>
<td>13.18</td>
</tr>
<tr>
<td>Max.</td>
<td>0.840</td>
<td>2.48</td>
<td>1.215</td>
<td>12.5</td>
<td>24.4</td>
<td>13.18</td>
</tr>
</tbody>
</table>
Table 4.2-e) Estimation of Integral Time Scale (Run2_section2)

<table>
<thead>
<tr>
<th>Depth (m)</th>
<th>Integral time scale (s)</th>
<th>Time to the first zero crossing (s)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$T_u$</td>
<td>$T_v$</td>
</tr>
<tr>
<td>0.003</td>
<td>0.288</td>
<td>0.237</td>
</tr>
<tr>
<td>0.005</td>
<td>0.342</td>
<td>0.191</td>
</tr>
<tr>
<td>0.01</td>
<td>0.316</td>
<td>0.105</td>
</tr>
<tr>
<td>0.015</td>
<td>0.160</td>
<td>0.074</td>
</tr>
<tr>
<td>0.02</td>
<td>0.166</td>
<td>0.062</td>
</tr>
<tr>
<td>0.025</td>
<td>0.160</td>
<td>0.059</td>
</tr>
<tr>
<td>0.03</td>
<td>0.141</td>
<td>0.054</td>
</tr>
<tr>
<td>0.035</td>
<td>0.190</td>
<td>0.051</td>
</tr>
<tr>
<td>0.04</td>
<td>0.183</td>
<td>0.044</td>
</tr>
<tr>
<td>0.045</td>
<td>0.187</td>
<td>0.068</td>
</tr>
<tr>
<td>0.05</td>
<td>0.220</td>
<td>0.051</td>
</tr>
<tr>
<td>0.06</td>
<td>0.425</td>
<td>0.067</td>
</tr>
<tr>
<td>0.07</td>
<td>0.813</td>
<td>0.097</td>
</tr>
<tr>
<td>0.08</td>
<td>1.384</td>
<td>0.114</td>
</tr>
<tr>
<td>0.09</td>
<td>1.565</td>
<td>0.137</td>
</tr>
<tr>
<td>0.1</td>
<td>1.143</td>
<td>0.120</td>
</tr>
<tr>
<td>0.11</td>
<td>1.008</td>
<td>0.105</td>
</tr>
<tr>
<td>0.12</td>
<td>0.848</td>
<td>0.146</td>
</tr>
<tr>
<td>0.13</td>
<td>0.335</td>
<td>0.867</td>
</tr>
<tr>
<td>Max.</td>
<td>1.565</td>
<td>0.867</td>
</tr>
</tbody>
</table>
Table 4.2-f) Estimation of Integral Time Scale (Run2_section3)

<table>
<thead>
<tr>
<th>Depth (m)</th>
<th>$T_u$ (s)</th>
<th>$T_v$ (s)</th>
<th>$T_w$ (s)</th>
<th>$t_u$ (s)</th>
<th>$t_v$ (s)</th>
<th>$t_w$ (s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.003</td>
<td>1.946</td>
<td>0.454</td>
<td>0.071</td>
<td>11.18</td>
<td>2.82</td>
<td>0.72</td>
</tr>
<tr>
<td>0.005</td>
<td>0.618</td>
<td>1.403</td>
<td>0.076</td>
<td>3.28</td>
<td>19.44</td>
<td>0.62</td>
</tr>
<tr>
<td>0.01</td>
<td>3.29</td>
<td>0.881</td>
<td>0.093</td>
<td>19.38</td>
<td>9.46</td>
<td>0.72</td>
</tr>
<tr>
<td>0.015</td>
<td>2.34</td>
<td>1.805</td>
<td>0.104</td>
<td>10</td>
<td>19.62</td>
<td>0.74</td>
</tr>
<tr>
<td>0.02</td>
<td>4.64</td>
<td>0.373</td>
<td>0.256</td>
<td>23.1</td>
<td>3.38</td>
<td>2.78</td>
</tr>
<tr>
<td>0.025</td>
<td>1.600</td>
<td>3.12</td>
<td>0.301</td>
<td>13.1</td>
<td>23.5</td>
<td>4.52</td>
</tr>
<tr>
<td>0.03</td>
<td>4.35</td>
<td>3.99</td>
<td>0.441</td>
<td>26.0</td>
<td>36.5</td>
<td>8.62</td>
</tr>
<tr>
<td>0.035</td>
<td>1.968</td>
<td>0.285</td>
<td>0.380</td>
<td>8.72</td>
<td>1.2</td>
<td>4.94</td>
</tr>
<tr>
<td>0.04</td>
<td>1.942</td>
<td>0.206</td>
<td>0.306</td>
<td>8.84</td>
<td>1</td>
<td>4.22</td>
</tr>
<tr>
<td>0.045</td>
<td>4.42</td>
<td>0.181</td>
<td>0.402</td>
<td>23.8</td>
<td>1.06</td>
<td>3.72</td>
</tr>
<tr>
<td>0.05</td>
<td>10.93</td>
<td>0.226</td>
<td>3.04</td>
<td>57.8</td>
<td>1.12</td>
<td>46.1</td>
</tr>
<tr>
<td>0.06</td>
<td>3.67</td>
<td>0.188</td>
<td>0.607</td>
<td>37.2</td>
<td>0.74</td>
<td>6.76</td>
</tr>
<tr>
<td>0.07</td>
<td>9.56</td>
<td>0.202</td>
<td>1.410</td>
<td>47.0</td>
<td>0.96</td>
<td>17.74</td>
</tr>
<tr>
<td>0.08</td>
<td>3.90</td>
<td>0.162</td>
<td>1.339</td>
<td>14.8</td>
<td>0.8</td>
<td>12.92</td>
</tr>
<tr>
<td>0.09</td>
<td>4.48</td>
<td>0.152</td>
<td>0.208</td>
<td>26.6</td>
<td>1.3</td>
<td>1.22</td>
</tr>
<tr>
<td>0.1</td>
<td>3.58</td>
<td>0.165</td>
<td>0.244</td>
<td>24.1</td>
<td>0.92</td>
<td>1.7</td>
</tr>
<tr>
<td>0.11</td>
<td>5.90</td>
<td>0.128</td>
<td>1.286</td>
<td>27.9</td>
<td>0.56</td>
<td>14.1</td>
</tr>
<tr>
<td>0.12</td>
<td>3.26</td>
<td>0.177</td>
<td>0.178</td>
<td>17.2</td>
<td>1.06</td>
<td>0.76</td>
</tr>
<tr>
<td>0.13</td>
<td>1.064</td>
<td>0.145</td>
<td>0.162</td>
<td>6.24</td>
<td>0.68</td>
<td>0.72</td>
</tr>
<tr>
<td>Max.</td>
<td>10.93</td>
<td>3.99</td>
<td>3.04</td>
<td>57.8</td>
<td>36.5</td>
<td>46.1</td>
</tr>
</tbody>
</table>
Figure 4.2 Linear Regression between the First Zero Crossing and Integral Time Scale

- \( u \)
- \( v \)
- \( w \)

- linear Regression
- discrepancy ratio
Ensemble time-averaged values of 2-D (stream-wise and water-depth directional) were plotted with vector arrows in Figure 4.3. Vertical variation of vectors at the first step (height= 0.035 m) were relatively smaller than the other larger step (height= 0.2 m). Because section 2 is not in the range of recirculation zone from the first step due to the longitudinal distance of section 2 (0.3 m) is larger than $X_{Re} (0.035*6 = 0.21$ m). On the other side, section 4 is in the range of recirculation zone from the second step, due to $X_{Re}$ of the second step is approximately 1.2 m. Reversal and backward flow pattern were occurred at the section 4 only. However the magnitude of flow is drastically smaller than vertical upper layer from the channel bottom (Figure 4.3). Additionally largest size of vortex due to the backward facing step, can be developed longitudinally from 6 to 17 times of water depth (Jovic and Driver, 1995; Jovic, 1996).

Figure 4.3 showed water-depth directional variation of the stream-wise direction velocity at each 4 sections. $u$ values were normalized with cross-sectional averaged velocity $U_0$ at each sections and $U_0$ value of the Run-1 is mostly half of Run-2. At the beginning of the step model, i. e. section #1, distributions of $u$ showed a relatively large difference between Run-1 and 2 along the water depth. From the section #2, vertical distributions were getting similar firstly near the bed. Variations of the upper part along the water depth ($z > 0.07$ m) were larger than lower part of the water depth ($z < 0.07$ m). Behind the biggest step, i. e. at section #4, values of $u/U_0$ were shown mostly same along the water depth, even there were backward flow. Variation of water-depth direction velocity, $w$ were relatively not larger than those of stream-wise velocity (Figure 4.5). Values of normalized water-depth direction velocity, $w/U_0$ were slightly negative at section #1, and mostly negative at section #2 and #3. And relatively larger negative values of $w/U_0$ were observed at section #4. Values of $w/U_0 (z)$ made reversal flow with $u/U_0$ as plotted in Figure 4.3 and mentioned previously.
a) Run-1

\((Q = 0.01 \text{ m}^3/\text{s}, h_0 = 0.4 \text{ m})\)

b) Run-2

\((Q = 0.02 \text{ m}^3/\text{s}, h_0 = 0.4 \text{ m})\)

Figure 4.3 Two-dimensional Vector Profiles in Backward-facing Step Flow
Figure 4.4 Vertical Distributions of Stream-wise Direction Velocity in Backward-facing Step Flow
Figure 4.5 Vertical Distributions of Water-depth Direction Velocity in Backward-facing Step Flow
With data of stream-wise directional velocity, LOW method (Eq. 2.19) were applied to estimate the shear velocity at each sections of two cases. Values of estimated shear velocity of Run-2 at each sections were mostly twice of those of Run-1. And also values of calibration coefficient were varied from 2.0 to 7.0 with logarithmic distribution of normalized velocity and distance from the channel bed.

Figure 4.7 and 4.8 showed the vertical distributions of stream-wise and water-depth directional turbulence intensity, which were normalized with $U_0$, respectively. As mentioned in previous chapter, $k_x/U_0$ and $k_z/U_0$ at section #2 were not well-distributed due to the location of recirculation zone of the first step. And those values at section #3 were shown that the turbulence was only due to the bed roughness. As resulted previously, the location of section #4 was in the recirculation zone of the second step. Therefore location of maximum values of $k_x/U_0$ and $k_z/U_0$ were occurred in the middle of water depth, 0.17 m from the channel bed (43 % from the bed) and gradually decreased toward the water surface and channel bed. Because values of turbulent kinetic energy is dominantly affected by the stream-wise direction turbulence intensity, Distributions of $k/U_0$ showed a similar distributions of $k_x/U_0$ (Figure 4.9). And values of $k/U_0$ of Run-2 showed approximately twice of those of $k/U_0$ of Run-2 along the water depth. Especially turbulent shear layer in the vicinity of the second step could revealed with excessive values of $k/U_0$ of Run-1 and Run-2. Figure 4.10 showed the comparisons of Reynolds Shear Stress, which were normalized with negative values of $U_0$ at each sections. Values of $-\overline{u'w'}/U_0$ at section #1 were represented with opposite direction of water flow, due to the approaching flow, but those of the other sections were not. Figure 4.11 showed the estimation of bed shear velocity with RSS method (Eq. 2.38 and 2.39). And the estimated values of bed shera velocity were compared in Table 4.3 and Figure 4.11.

81
Figure 4.6 Estimation of Bed Shear Stress with LOW Method
Figure 4.7 Vertical Distributions of Stream-wise Turbulence Intensity in Backward-facing Step Flow
Figure 4.8 Vertical Distributions Water-depth direction Turbulence Intensity in Backward-facing Step Flow
Figure 4.9 Vertical Distributions of Turbulent Kinetic Energy
in Backward-facing Step Flow
Figure 4.10 Vertical Distributions of Reynolds Shear Stress in Backward-facing Step Flow
a) Run-1, Section #1 ($\tau_0 = 0.023$ Pa)

b) Run-2, Section #2 ($\tau_0 = -0.24$ Pa)

c) Run-1, Section #2 ($\tau_0 = 0.068$ Pa)

d) Run-2, Section #2 ($\tau_0 = 0.25$ Pa)

Figure 4.11 Estimation of Bed Shear Stress with RSS method (Run-1) in Backward-facing Step Flow
c) Run-1, Section #3 ($\tau_0 = 0.159$ Pa)

f) Run-1, Section #2 ($\tau_0 = 0.051$ Pa)

g) Run-1, Section #4

h) Run-2, Section #4

Figure 4.11 Continued
Table 4.3 Comparison of Bed Shear Stress with two Methods in Backward-facing Step Flow

<table>
<thead>
<tr>
<th>x (m)</th>
<th>Reynolds Shear Stress method (Pa, extrapolation of $-\rho u'w'$)</th>
<th>Log Law method (Pa, using shear velocity)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Run-1</td>
<td>Run-2</td>
</tr>
<tr>
<td>-0.002</td>
<td>0.023</td>
<td>-0.24</td>
</tr>
<tr>
<td>0.3</td>
<td>0.070</td>
<td>0.25</td>
</tr>
<tr>
<td>2.4</td>
<td>0.159</td>
<td>0.051</td>
</tr>
<tr>
<td>3.6</td>
<td>-</td>
<td>-</td>
</tr>
</tbody>
</table>

Figure 4.12 Longitudinal Distribution of Bed Shear Stress on Backward Facing Step
b) Mean and Turbulent Flow at the Longitudinal Transition

It is known that the one of the most important dominant factors on local scouring is distribution of mean and turbulent flow at the longitudinal transition ($x = 0$ m). Especially depth-averaged relative turbulence intensity, $r_0$ has the properties of flow and turbulence characteristics, which can be determined by the bed roughness or geometry of hydraulic structures at the upstream. Therefore, measurement of 3-D flow velocity of each 10 cases at the longitudinal transition were conducted with using the Vectrino and analyzed (Table 4.4). Configurations of measurement were same as the preliminary test with step models. And experimental setup was schematized in Figure 4.13. A size of measuring interval ($\Delta z$) is 2 mm and total range of measurement is from 2 mm to 36 mm from the bed.

Figure 4.14 showed the vertical variation of the stream-wise direction velocity based on the logarithmic distribution. And normalized values of stream-wise direction velocity were plotted in Figure 4.15 with values of coefficient, $C$, which was varied from 4 to 9 in Eq. 2.19. Normalized values of turbulent kinetic energy ($= \text{TKE}/u_*^2$) were plotted in Figure 4.16. All of the cases were good fit with Eq. 2.34 (Figure 4.17). Also Normalized values of Reynolds shear stress ($= -\text{RSS}/u_*^2$) were plotted in Figure 4.18. And maximum value of each cases were distributed from 4 to 10 % of water depth (Figure 4.19).

c) Initial Bed Shear Stress

The values of bed shear velocity at each cases were estimated by using the Eq. 2.19, 2.34, and 2.38, respectively. And bed shear stress ($= \rho u_*^2$) were calculated and compared with those of different estimating method. Values of those with using the LOW method were represented the reliable data against the others. Also LOW method were used for extrapolation of free surface flow velocity, $U_{free}$ and estimation of turbulent layer thickness,
Table 4.4 Experimental Conditions of Flow Test at Longitudinal Transition

<table>
<thead>
<tr>
<th>case number</th>
<th>$Q$ (m$^3$/s)</th>
<th>$h_0$ (m)</th>
<th>$U_0$ (m/s)</th>
<th>Fr (-)</th>
<th>Re ($*10^5$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Q15h320</td>
<td>0.020</td>
<td>0.120</td>
<td>0.208</td>
<td>0.192</td>
<td>0.250</td>
</tr>
<tr>
<td>Q20h320</td>
<td>0.030</td>
<td>0.150</td>
<td>0.278</td>
<td>0.256</td>
<td>0.333</td>
</tr>
<tr>
<td>Q20h350</td>
<td>0.030</td>
<td>0.120</td>
<td>0.222</td>
<td>0.183</td>
<td>0.333</td>
</tr>
<tr>
<td>Q30h320</td>
<td>0.035</td>
<td>0.120</td>
<td>0.417</td>
<td>0.384</td>
<td>0.500</td>
</tr>
<tr>
<td>Q30h345</td>
<td>0.035</td>
<td>0.144</td>
<td>0.345</td>
<td>0.289</td>
<td>0.500</td>
</tr>
<tr>
<td>Q30h350</td>
<td>0.030</td>
<td>0.145</td>
<td>0.333</td>
<td>0.274</td>
<td>0.500</td>
</tr>
<tr>
<td>Q32h320</td>
<td>0.020</td>
<td>0.120</td>
<td>0.444</td>
<td>0.410</td>
<td>0.533</td>
</tr>
<tr>
<td>Q35h320</td>
<td>0.035</td>
<td>0.120</td>
<td>0.486</td>
<td>0.448</td>
<td>0.583</td>
</tr>
<tr>
<td>Q35h344</td>
<td>0.035</td>
<td>0.150</td>
<td>0.405</td>
<td>0.341</td>
<td>0.583</td>
</tr>
<tr>
<td>Q40h320</td>
<td>0.030</td>
<td>0.150</td>
<td>0.556</td>
<td>0.512</td>
<td>0.667</td>
</tr>
</tbody>
</table>

Figure 4.13 Schematic Diagram of 3-D Flow Measurement at Longitudinal Transition
Figure 4.14 Vertical Distribution of Stream-wise Velocity at Longitudinal Transition
Figure 4.1

Continued

Calculated values
($u^* = 0.017 \text{ m/s}$)

Calculated values
($u^* = 0.018 \text{ m/s}$)

Calculated values
($u^* = 0.022 \text{ m/s}$)

Calculated values
($u^* = 0.026 \text{ m/s}$)
Figure 4.15 Comparisons between Measured and Calculated Values of Normalized Stream-wise Velocity Distribution at Longitudinal Transition
Figure 4.16 Vertical Distribution of Normalized Turbulence Kinetic Energy at Longitudinal Transition
Figure 4.16 Continued
Figure 4.16 Continued

Figure 4.17 Comparisons between Measured and Calculated Values of Normalized Turbulent Kinetic Energy Distribution at Longitudinal Transition
Figure 4.18 Vertical Distribution of Normalized Reynolds Shear Stress at Longitudinal Transition
Figure 4.18 Continued
Figure 4.19 Comparisons between Measured and Calculated Values of Normalized Reynolds Shear Stress at Longitudinal Transition
δ* from the differences between $U_{free}$ and local velocity. Estimated values of bed shear velocity and stress by using three methods at the transition were determined and compared with different hydraulic parameters (mean flow velocity, Froude number, and depth-averaged relative turbulence intensity) in Table 4.5.

Estimated values of bed shear stress with LOW method were compared with those of TKE and RSS methods with using the definition ($=\alpha_0 u^*/U_0^*$) in Figure 4.20. Consequently, values of TKE method were distributed closer to LOW method than those of RSS method from the plots. Also it can be said that the values of RSS method should be modified with appropriate coefficient. Calculated and modified values of estimated $r_0$ of LOW and RSS method, respectively were plotted with coefficient, $\alpha_0$, which is suggested as 1.2 in Graf (1998) in Figure 4.21. Using TKE method, $r_0$ were calculated and relationships of Fr and $Re^*$ against $r_0$ were plotted in Figure 4.22. Functional relationships are as follows:

\[ r_0 = \alpha_1 Fr^{\beta_1} \]  \hspace{1cm} (4.2-a)

\[ r_0 = \alpha_2 Re^{\beta_2} \]  \hspace{1cm} (4.2-b)

where, $\alpha_1$ and $\alpha_2$ are the calibration coefficients, which are varied from 0.040 to 0.056 and from 0.144 to 0.19, respectively. $\beta_1$ and $\beta_2$ are the calibration exponents (-0.22). Also a linear relationship between Fr and $Re^*$ from the result of Figure 4.22 and Eq. 4.2 is

\[ Fr = \alpha_3 Re^* \times 10^{-3} \]  \hspace{1cm} (4.3)

where $\alpha_3$ is the calibration coefficient (from 1.44 to 2.16) from the results in Figure 4.23.
<table>
<thead>
<tr>
<th>case</th>
<th>$U_0$ (m/s)</th>
<th>Fr</th>
<th>LOW method</th>
<th>TKE method</th>
<th>RSS method</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td>$\tau_0$ (Pa)</td>
<td>$\delta^*$ (mm)</td>
<td>$U_{\text{free}}$ (m/s)</td>
</tr>
<tr>
<td>Q15h320</td>
<td>0.21</td>
<td>0.6192</td>
<td>0.121</td>
<td>8.4</td>
<td>0.26</td>
</tr>
<tr>
<td>Q20h320</td>
<td>0.28</td>
<td>0.26</td>
<td>0.23</td>
<td>7.8</td>
<td>0.35</td>
</tr>
<tr>
<td>Q20h350</td>
<td>0.22</td>
<td>0.183</td>
<td>0.144</td>
<td>8.7</td>
<td>0.28</td>
</tr>
<tr>
<td>Q30h320</td>
<td>0.42</td>
<td>0.38</td>
<td>0.44</td>
<td>9.0</td>
<td>0.49</td>
</tr>
<tr>
<td>Q30h345</td>
<td>0.35</td>
<td>0.29</td>
<td>0.29</td>
<td>8.1</td>
<td>0.43</td>
</tr>
<tr>
<td>Q30h350</td>
<td>0.33</td>
<td>0.27</td>
<td>0.32</td>
<td>8.6</td>
<td>0.41</td>
</tr>
<tr>
<td>Q32h320</td>
<td>0.44</td>
<td>0.41</td>
<td>0.48</td>
<td>9.0</td>
<td>0.52</td>
</tr>
<tr>
<td>Q35h320</td>
<td>0.49</td>
<td>0.45</td>
<td>0.68</td>
<td>11.2</td>
<td>0.61</td>
</tr>
<tr>
<td>Q35h344</td>
<td>0.41</td>
<td>0.34</td>
<td>0.48</td>
<td>10.1</td>
<td>0.53</td>
</tr>
<tr>
<td>Q40h320</td>
<td>0.56</td>
<td>0.51</td>
<td>0.84</td>
<td>10.6</td>
<td>0.69</td>
</tr>
</tbody>
</table>

Table 4.5 Comparisons of Hydraulic Conditions and Bed Shear Stress with Various Estimation Methods at Longitudinal Transition.
Figure 4.20 Comparisons of Bed Shear Stress with Various Estimation Methods at Longitudinal Transition
a) LOW method (Calculated by $\alpha_0 = 1.2$)

b) RSS method (Calculated by $\alpha_0 = 1.6$)

Figure 4.21 Comparisons of Depth-averaged Relative Turbulence Intensity with Various Estimation Methods at Longitudinal Transition
a) Froude number

Figure 4.22 Relationship between Hydraulic Parameters and Depth-averaged Relative Turbulence Intensity at Longitudinal Transition

b) Boundary Reynolds Number

Figure 4.22 Relationship between Hydraulic Parameters and Depth-averaged Relative Turbulence Intensity at Longitudinal Transition
Figure 4.23 Linear Relationship between Boundary Reynolds Number and Froude Number at Longitudinal Transition
4.1.2 Characteristic Length Scale

Previously, several hydraulic parameters were analyzed with various flow conditions at the longitudinal transition. In this chapter, development of turbulent shear layer thickness at the transition toward an abrupt bed elevation decrease were analyzed in backward-facing step flow. Appropriate length scale from this tests will be applied to normalize the temporal development of local scouring in the following chapter.

To analyze the development of turbulent shear layer thickness, vertical 2-D flow measurement were conducted with using PIV system in the backward-facing step flow. Experimental setup was decribed in Figure 4.24. Laser supply system is mounted on the carriage and reflectging mirror changed the direction of laser from the system. A field of view is ~300 * 300 mm in the vicinity of the step (height= 0.2 m). Measuring frequency was 10 Hz for 30 seconds (i.e. 300 data set). Measuring interests of this test were described in Figure 4.25 in detailed. Previously analyzed, flow separation and excessive increase of gradients of stream-wise velocity were estimated close to the step. Based on the data of \( \frac{dU}{dz} \) and recirculation profiles of vector flow field, developed length scale of turbulent shear layer thickness, \( \delta_{*m} \) and the longitudinal distance from the transition to the location of \( \delta_{*m} \) were determined from the contour plot in Figure 4.26. And the slope of the turbulent shear layer from the transition, \( \theta_\delta \) was calculated with the ratio of \( \delta_{*m} \) and \( L_{*m} \) and compared with upstream scour slope, \( \theta_{up} \) in the next chapter. Also properties of turbulent shear layer thickness in the backward-facing step flow were estimated in Table 4.6 and functional relationships of them were analyzed.
2-D Flow Measurement near the step with PIV system

(Not to scale)

Field of View
300 mm * 300 mm

Acrylic bed
$h = 20$ cm

Figure 4.24 Schematic Diagram of 2-D Flow Measurement in Backward-facing Step Flow

(Not to scale)

Anticorrelation

Increase of Turbulent Layer Thickness

Acrylic bed
$h = 20$ cm

$\delta_{*,m} = f(\delta_*, \text{Fr}, \text{Re}, \cdots)$

Figure 4.25 Development of Turbulent Layer Thickness in Backward-facing Step Flow
Figure 4.26 Distributions of Vector Fields and Shear Stress in Backward-facing Step Flow

a) $Q_{15h150}$ (Fr = 0.137)

b) $Q_{30h240}$ (Fr = 0.136)
c) Q20h150 (Fr= 0.183)

d) Q35h210 (Fr= 0.194)

Figure 4.26 Continued
Table 4.6 Flow Parameters and Results of Backward-facing Step Test

<table>
<thead>
<tr>
<th>case</th>
<th>$U_0$ (m/s)</th>
<th>Fr</th>
<th>Re*</th>
<th>$\delta_\star$ (mm)</th>
<th>$\delta_{\star,m}$ (mm)</th>
<th>$(\delta_{\star,m}-\delta_\star)/\delta_\star$</th>
<th>$L_{\star,m}$ (mm)</th>
<th>cot $\theta_i$ ($=2L_{\star,m}/\delta_{\star,m}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Q15h150</td>
<td>0.167</td>
<td>0.137</td>
<td>90</td>
<td>7.0</td>
<td>100</td>
<td>13.2</td>
<td>100</td>
<td>0.25</td>
</tr>
<tr>
<td>Q30h240</td>
<td>0.21</td>
<td>0.136</td>
<td>89</td>
<td>7.0</td>
<td>80</td>
<td>10.4</td>
<td>200</td>
<td>0.20</td>
</tr>
<tr>
<td>Q20h150</td>
<td>0.22</td>
<td>0.183</td>
<td>120</td>
<td>7.9</td>
<td>70</td>
<td>7.9</td>
<td>180</td>
<td>0.194</td>
</tr>
<tr>
<td>Q35h210</td>
<td>0.28</td>
<td>0.194</td>
<td>128</td>
<td>8.1</td>
<td>50</td>
<td>5.2</td>
<td>160</td>
<td>0.156</td>
</tr>
<tr>
<td>Q35h144</td>
<td>0.41</td>
<td>0.34</td>
<td>10</td>
<td>9.5</td>
<td>40</td>
<td>3.2</td>
<td>200</td>
<td>0.133</td>
</tr>
</tbody>
</table>

Figure 4.26 Continued
With data of two dimensional vorticity can be calculated as follows:

\[ d\Gamma = \left( \frac{\partial w}{\partial x} - \frac{\partial u}{\partial z} \right) dxdz \]  

(4.4)

Here, \( \Gamma \) denotes the value of vorticity in the \( x-z \) plane. Eq. 4.4 can be rearranged as follows:

\[ \frac{d\Gamma}{dxdz} = \xi_{xz} = \frac{\partial w}{\partial x} - \frac{\partial u}{\partial z} \]  

(4.5)

Here, \( \xi_{xz} \) denotes vorticity per unit area.

Distribution of \( \xi_{xz} \) were depicted in Figure 4.27 with the distribution of streamline. From the figures, two dimensional distribution of the per unit area were corresponded the distribution of the velocity gradients. And the maximum value of the vocity was occured at \( x \sim 0.4 \) m from the step. Also backward flow distribution were occured until \( x=1.0 \) m and then all of the streamline were headed toward downstream of the step.

Ratios of turbulent layer thickness at the longitudinal transition and in the turbulent shear layer is as follows:

\[ \frac{\Delta \delta_s}{\delta_s} = \left( \frac{\delta_{s,m} - \delta_s}{\delta_s} \right) \alpha_4 (Fr \cdot Re_s)^{\beta_i} \]  

(4.6)
Figure 4.27 Distribution of Velocity Gradient and Vorticity (case Q15h150; Fr= 0.137)
where $\alpha_4$ and $\beta_4$ are the calibration coefficient (= 40) and exponent (= -0.6), which were estimated in Figure 4.27-a). With Eq. 4.4, $\delta_{*m}$ can be rewritten as follows:

$$\delta_{*m} = \delta_0\left[\alpha_4 \left(Fr \cdot Re_*\right)^{\beta_4} + 1\right] \quad (4.6)$$

$\delta_{*m}$ represents the capacity of the local scouring due to the flow fluctuation and excessive values of stream-wise velocity gradients in the turbulent shear layer. Therefore characteristic length scale on the local scouring, $\lambda$ in this study was determined as follows:

$$\lambda = \delta_{*m} = f\left(\delta_0, Fr, Re_*\right) \quad (4.6)$$

$\lambda$ was also applied to normalize the length scale of scour depth and to determine the time scale of scouring in the following chapter as well.

Additionally, a longitudinal distance from the transition to the location of the maximum values of $\delta_*$ was denoted as $L_{*m}$ in Figure 4.25. A functional relationship of the slope of the turbulent shear layer and flow parameters were regressed as follows:

$$\frac{\delta_*}{2L_{*m}} = \cot \theta_\delta = \alpha_5 \left(Fr \cdot Re_*\right)^{\beta_5} \quad (4.7)$$

where $\alpha_5$ and $\beta_5$ are the calibration coefficient (= 0.5) and exponent (= -3.2), which were estimated in Figure 4.28-b). This slope of the layer were compared with the development of upstream scour slope in the scour test.
Figure 4.28 Functional Relationships of Turbulent Shear Layer Thickness and Slope in Backward-facing Step Flow
4.2 Temporal Development of Local Scour Hole

4.2.1 Scour Test

To conduct a scour test, Approaching wedge model was positioned at 3 m behind the headtank of the flume and 4 m-long and 0.2 m-high acrylic box model also was attached behind the wedge. And 8.5 m-long region, which is situated 2.5 m at the upstream of the tailgate of the flume was filled with the sand. Measurent of bed and 3-D velocity profiles in the scoured hole was performed with Vectrino on the autotraverse system (Figure 4.29).

At the beginning of the scour test, appropriate setup of sand in the region of the test is the most important procedure. Firstly, dry sand in the test region was packed and flattened with initial bed elevation \( \eta_0 = 0.2 \text{ m} \). And then the desirable value of water depth was reached with tap water only to keep the initial bed elevation. Secondly, elevation of movable bed was flattened again to reduce the soil pore with light compaction. Then the desirable water discharge was reached gradually (Figure 4.30). Lastly, scour test was started.

4.2.2 Temporal Development of Local Scour Hole

At each time steps, which were dependent to the scouring, distances from the transmitter of the Vectrino to the eroded bed were measured at each longitudinal measuring grid, which were also dependent to the scouring. Then those values were converted to the bed elevation \( \eta (x, t) \). Temporal developments of the \( \eta (x, t) \) of each 10 cases were plotted in Figure 4.31. To distinguish the change of the bed elevations, only 6 data set of the each cases were drawn and compared.
Figure 4.29 Schematic Diagram of Experimental Setup and Apparatus of Scour Test

Figure 4.30 Procedure of Scour Test
Figure 4.31 Temporal Development of bed Profiles
c) Q30h120d12

![Graph showing changes in bed elevation over time for Q30h120d12.](image)

- Initial bed elevation ($\eta = 20$ cm)
- 3 hrs. later
- 14 hrs. later
- 30 hrs. later
- 72 hrs. later
- 169 hrs. later
- 434 hrs. later
- Initial bed elevation ($\eta = 20$ cm)

d) Q30h145d12

![Graph showing changes in bed elevation over time for Q30h145d12.](image)

- Initial bed elevation ($\eta = 20$ cm)
- 12 hrs. later
- 62 hrs. later
- 110 hrs. later
- 206 hrs. later
- 354 hrs. later
- 693 hrs. later
- Initial bed elevation ($\eta = 20$ cm)
Figure 4.31 continued

e) Q35h120d12

f) Q35h144d12
g) $Q_{20h120d06}$

![Graph](image1)

h) $Q_{35h120d06}$

![Graph](image2)

Figure 4.31 continued
Figure 4.31 Continued
4.2.3 Normalized Maximum Scour Depth

From temporal changes of the bed profiles, properties of the local scouring were estimated as described in Chapter 2. And the most important property is the temporal development of the maximum scour depth, $y_m(t)$. Temporal change of the values of $y_m(t)$ were drawn and compared in Figure 4.32. To compare them accurately, a modified equation of temporal change of $y_m$ was described as follows:

$$\frac{y_m}{\lambda} = \left( \frac{t}{t_\lambda} \right)^\gamma$$ (4.8)

where $\lambda$ and $t_\lambda$ were defined as characteristic length and time scales and described as follows:

$$\lambda = \delta_{s,m}$$ (4.9-a)

$$t_\lambda = \left( \alpha U_0 - U_c \right) / \delta_{s,m}$$ (4.9-b)

With using the Eq. 2.6, Eq. 4.9-b can be rewritten as

$$t_\lambda = \frac{y_{m,e} U_c}{h_0 \lambda}$$ (4.10)

Additionally, differentiation of Eq. 4.8 was as follows:
\[
\frac{d\left(\frac{y_m}{\lambda}\right)}{dt} = \gamma \frac{t^{\gamma-1}}{t^\lambda} \quad (4.11)
\]

We found

\[
\frac{d\left(\frac{y_m}{\lambda}\right)}{dt} = \frac{\gamma}{t} \left(\frac{t}{t^\lambda}\right)^\gamma = \frac{\gamma}{t} \left(\frac{y_m}{\lambda}\right) \quad (4.12)
\]

And re-arranging Eq. 4.12

\[
\frac{d\left(\frac{y_m}{\lambda}\right)}{y_m/\lambda} = \frac{\gamma dt}{t} \quad (4.13)
\]

From the upper Eq. 4.13, a meaningful-physical factor on temporal change of \(y_m\), \(\gamma\) was described as follows:

\[
\gamma = \frac{d\left(\frac{y_m}{\lambda}\right)/\left(\frac{y_m}{\lambda}\right)}{dt/t} = \left(\frac{\text{Fractional change in scour depth}}{\text{Fractional change in time}}\right) \quad (4.14)
\]

Hydraulic-sedimentological parameters and dominant factors on local scouring to predict the equilibrium scour depth were estimated in Table 4.7 and 4.8, respectively.
Figure 4.32 Temporal Development of Maximum Scour Depth

a) Q20h120d12

b) Q30h150d12
c) Q30h120d12

\[ y_m (\text{cm}) \]
\[ t (\text{hr.}) \]

\[ y_m (\text{cm}) \]
\[ t (\text{hr.}) \]

\[ + \text{ Q30h120d12} \]

\[ - \text{ Q30h120d12} \]

\[ - \text{ Q30h120d12} \]

\[ \square \text{ Q35h144d12} \]

\[ \square \text{ Q35h144d12} \]

\[ \square \text{ Q35h144d12} \]

\[ \text{Figure 4.32 continued} \]

126
e) Q35h120d12

f) Q30h145d12

Figure 4.32 continued
g) Q20h120d06

h) Q35h120d06

Figure 4.32 continued
i) Q35h150d06

![Graph for Q35h150d06](image)

j) Q32h120d06

![Graph for Q32h120d06](image)

Figure 4.32 Continued
<table>
<thead>
<tr>
<th>case number</th>
<th>Flow Parameters</th>
<th>Sediment Parameters</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$U_0$ (m/s)</td>
<td>Fr (-)</td>
</tr>
<tr>
<td>Q20h120d12</td>
<td>0.27</td>
<td>0.30</td>
</tr>
<tr>
<td>Q30h150d12</td>
<td>0.33</td>
<td>0.34</td>
</tr>
<tr>
<td>Q30h120d12</td>
<td>0.42</td>
<td>0.45</td>
</tr>
<tr>
<td>Q35h120d12</td>
<td>0.49</td>
<td>0.53</td>
</tr>
<tr>
<td>Q35h144d12</td>
<td>0.41</td>
<td>0.42</td>
</tr>
<tr>
<td>Q30h145d12</td>
<td>0.35</td>
<td>0.35</td>
</tr>
<tr>
<td>Q20h120d06</td>
<td>0.27</td>
<td>0.24</td>
</tr>
<tr>
<td>Q35h120d06</td>
<td>0.49</td>
<td>0.53</td>
</tr>
<tr>
<td>Q35h150d06</td>
<td>0.39</td>
<td>0.32</td>
</tr>
<tr>
<td>Q32h120d06</td>
<td>0.44</td>
<td>0.49</td>
</tr>
<tr>
<td>case number</td>
<td>Characteristic Scales</td>
<td>Equilibrium Prediction</td>
</tr>
<tr>
<td>---------------------</td>
<td>-----------------------</td>
<td>------------------------</td>
</tr>
<tr>
<td></td>
<td>$\delta_{*,m}$ (mm)</td>
<td>$\lambda$ (-)</td>
</tr>
<tr>
<td>Q20h120d12</td>
<td>0.27</td>
<td>0.30</td>
</tr>
<tr>
<td>Q30h150d12</td>
<td>0.33</td>
<td>0.34</td>
</tr>
<tr>
<td>Q30h120d12</td>
<td>0.42</td>
<td>0.45</td>
</tr>
<tr>
<td>Q35h120d12</td>
<td>0.49</td>
<td>0.53</td>
</tr>
<tr>
<td>Q35h144d12</td>
<td>0.41</td>
<td>0.42</td>
</tr>
<tr>
<td>Q30h145d12</td>
<td>0.35</td>
<td>0.35</td>
</tr>
<tr>
<td>Q20h120d06</td>
<td>0.27</td>
<td>0.24</td>
</tr>
<tr>
<td>Q35h120d06</td>
<td>0.49</td>
<td>0.53</td>
</tr>
<tr>
<td>Q35h150d06</td>
<td>0.39</td>
<td>0.32</td>
</tr>
<tr>
<td>Q32h120d06</td>
<td>0.44</td>
<td>0.49</td>
</tr>
</tbody>
</table>
And the relationship between normalized velocity and equilibrium-maximum scour depth was plotted in Figure 4.33. This figure showed that the predicted $y_{m,e}$ of smaller $d_{50}$, were slightly larger than that of larger $d_{50}$. And also that of larger gaps of normalized velocity were remarkable larger than that of smaller gap of normalized velocity. Therefore, linear regression equation of its relationship is as follows:

$$
\frac{y_m}{h_0} = \alpha_{m,e} \left( \frac{U_0 - U_c}{U_c} \right) + \beta_{m,e}
$$

(4.16)

where $\alpha_{m,e} (= 3.3)$ and $\beta_{m,e} (0.64-0.96)$ are the calibration coefficient and intercept. Even the zero value of gaps normalized velocity can also make the scouring. Eq. 4.16 is applicable to the case, when it is not possible to estimate the turbulence properties at the longitudinal transition in field.

Normalized values of maximum scour depth and time of all cases were plotted and compared in Figure 4.34. And fractional exponents of scouring, $\gamma$ was estimated as ~0.4, which was suggested by Hoffmans and Verheij (1997).

### 4.2.4 Equilibrium-maximum Scour Depth

Equilibrium state values of the maximum scour depth were estimated from the suggestion of Dietz (1969) in Figure 4.33. And also it can be regressed with the following equation:

$$
y_{m,e} / h_0 = 1.3\ln(C_{eq}) - 0.13
$$

(4.17-a)

$$
C_{eq} = f(r_0, Fr, Re*) = r_0 * Fr^*Re*
$$

(4.17-b)
Figure 4.33 A Relationship of Normalized Velocity Difference and Equilibrium-maximum Scour Depth

Figure 4.34 Relationship between the Normalized Maximum Scour Depth and Time
4.3 Flow and Turbulence in Scoured Hole

4.3.1 Flow Separation and Turbulent Shear Layer

Flow patterns at 245 hours later (approximately 10 days later) of case Q20h120d12 in the upstream scour slope were captured motion of fine particles for visualization in Figure 4.35. Flow velocity was faster in the vertically upper part \((z > \eta_0)\) than in the lower part \((z < \eta_0)\) of scoured hole. And in the lower part of upstream scour slope, a reverse and circulating movement of particles with relatively much slower than primary flow were shown.

To reveal the flow patterns in the upstream scour slope quantitatively, three-dimensional velocity data (measured for 30 seconds and ensemble-averaged as mentioned in the Chapter 3) were measured and analyzed in Figure 4.36. Flow velocity near the end of fixed bed were faster than in the scour hole with vertically uniform distribution. From the transition to 0.2 m, the reverse flow near the bed (2-10 mm from the bed) were measured with slower than in the upper part of scour hole as mentioned previously. Values of 3-D turbulence intensity were calculated and plotted in Figure 4.37 and reversal flow were compared with turbulent kinetic energy. Mostly, at 2 cm from the scoured hole, the values turbulent kinetic energy were estimated with excessively increased due to the larger values of velocity gradients and flow circulation. Maximum value of turbulent kinetic energy was estimated as 0.1 m\(^2\)/s\(^2\)) at the 0.26 m from the transition. According to the results by Breusers (1966), high turbulence intensities are possible in decelerating turbulent flows, due to the formation of layers with great velocity gradients in abrupt expansions of water depth. Also Hoffmans and Booij (1993-b) described turbulent mixing (or shear) layer in the scour hole with experimental data and numerical approaches. As they proposed, re- circulation (or reverse
Figure 4.35 Snapshot of Visualization Particle in the Scoured Hole

Figure 4.36 Two-dimensional Vector Profiles in Scoured Hole
Figure 4.37 Distribution of Mean Flow and Turbulent Kinetic Energy in the Scoured Hole

a) Stream-wise Mean Flow Velocity

b) Turbulence Kinetic Energy
movement) of flow in the upstream scour slope occurs near the bed and a mixing layer develops between the transient flow and the recirculating flow. In the beginning of the scour process, when the flow near the bed is not directed against the primary flow, a wake zone appears (Hoffmans and Booij, 1993-b). From the Figure 4.37 and 4.38, a reverse flow and abrupt increase of $k$ (at 0.1 m from the bed) were measured in upstream scour hole. And these ultimate values of $k$ were reflected in the turbulent shear layer in particular location with respect to the depth (Hoffmans and Booij, 1993-b).

Behind the transition, a lower region of mean velocity and turbulence intensity took place and the ultimate values were gradually developed at $z= 2$ cm (17 % of the $h_0$) from the scoured bed. And the maximum values of $\delta_{m}$, which represent a thickness of the turbulent mixing layer revealed by Hoffmans and Booij, 1993-b, was 1.1 cm (50 % of 0.09$x$) at $x= 0.24$ m from the transition.

4.3.2 Bed Shear Stress in Scoured Hole

Applying 2.52, values of bed shear stress in the scoured hole were calculated with 3-D velocity data at $z= -2$ mm from the bed at each longitudinal measuring grid and time steps. Longitudinal distributions of Reynolds shear stress and kinetic energy along the scoured hole (case Q35h144d12) of each time step in Figure 4.38. in the upstream part of the maximum scour depth, values of turbulent kinetic energy were larger than in the downstream of it and decreased gradually toward the downstream. Values of Reynolds shear stress did not have excess differences between upstream and downstream of the maximum scour depth.
Figure 4.38 Temporal Change of Turbulence Properties near the Bed of Scoured Hole
c) 269 hours later

- bed elevation
- Reynolds shear stress
- Turbulent kinetic energy

\[ \eta (m) \]
\[ x (m) \]

\[ k, u'w' (m^2/s^2) \]

\[ \eta (m) \]
\[ x (m) \]

\[ k, u'w' (m^2/s^2) \]

Figure 4.38 Continued
e) 401 hours later

f) 437 hours later

Figure 4.38 Continued
Figure 4.38 Continued

- Bed elevation
- Reynolds shear stress
- Turbulent kinetic energy

Figure 4.38 Continued
4.3.3 Energy Dissipation Rate

Hydraulic gradient, $S_e$ is the slope of the hydraulic grade line (or mean energy slope) and it means the slope of the water surface in the open channel flow. For uniform flow conditions, estimating equation of $S_e$ by Graf (1998) as follows:

$$S_e = \frac{2\nu U_o}{gR_h^2} + \frac{u_*^2}{gR_h}$$  \hspace{1cm} (4.18)

Also Graf (1988) suggested the functional relationship between the friction coefficient of Darcy Weisbach equation, $f_{D,W}$ and depth-averaged relative turbulence intensity in open channel flows as follows:

$$f_{D,W} = 8 \left( \frac{u_*}{U_o} \right)^2 = 5.6r_0^2$$  \hspace{1cm} (4.19)

Substituting Eq. 4.19 into Eq. 4.18,

$$S_e = \frac{2\nu U_o}{gR_h^2} + \frac{0.7 \left( r_0 U_o \right)^2}{gR_h}$$  \hspace{1cm} (4.20)

The first term on the RHS of Eq. 4.20 represents the influence of laminar flow which can be neglected with respect to the second term if $Re>2,000$.

With the condition of turbulent open channel flow, Eq. 4.20 can be re-written as
Estimated values of energy slope (3 cases) were plotted with the values of bed elevation in Figure 4.39. Maximum value of $S_e$ was $5.15 \times 10^3$ and it was decreased gradually to the downstream of the scoured hole. Relationship between normalized energy slope and hydraulic radius was regressed as follows:

$$\frac{S_e(x)}{\eta(x)/\eta_0} = a_1 \left[ \frac{R_a(x)}{h_0} \right]^{a_2}$$ \hspace{1cm} (4.22)

where $a_1$ (4.5-89) and $a_2$ (= 8.5) calibration coefficient and exponent, respectively (Figure 4.40). Errors were analyzed with the following methods in Figure 4.41.

$$RMSE = \sqrt{\frac{1}{N} \sum_{n=1}^{N} \left( x_{n,cal} - x_{n,mea} \right)^2} = 0.0045$$ \hspace{1cm} (4.23)

$$MAE = \frac{1}{N} \sum_{n=1}^{N} \left| x_{n,cal} - x_{n,mea} \right| = 0.003$$ \hspace{1cm} (4.24)

$$AGD = \left[ \prod_{n=1}^{N} R_n \right]^{1/N} = 1.0992$$ \hspace{1cm} (4.25)
Figure 4.39 Longitudinal Distribution of Energy Slope in the Scoured Hole

Figure 4.40 Dimensionless Energy Slope and Hydraulic Radius in the Scoured Hole
Figure 4.41 Error Analysis of Empirical Equation of Energy slope
4.3.4 Flow and Turbulence Distribution in the Scoured Hole

Three dimensional velocity data were measured and analyzed spatially in the scoured hole, which was mostly stabilized for each 4 cases. At the upstream part from the $L_1$, relatively dense distributions ($\Delta x = 2$ cm) were setup and downstream part from the $L_1$, relatively coarse distribution ($\Delta x = 5$-50 cm) of measuring grid points were setup respectively. And also vertical intervals of measuring grid were from 2 mm to 5-20 mm from the scoured bottom (Figure 4.42).

As mentioned in Chapter 2.3, measured flow data can be spiked due to the mistakes of the sensor configuration in the zones of spatially varied flow and occasionally undesirable particle moving. Figure 4.43 showed the contaminated and filtered values of the stream-wise directional velocity data in time domain. Also Figure 4.44 showed the spiked values with the confidence ellipses and filtered values of the instantaneous velocity in the confidence ellipses.

With the despiking procedure, flow velocity and turbulence properties were plotted in Figure 4.45. Distributions of stream-wise velocity, which dominantly affects the sediment transport of bed materials, were analyzed that relatively high valued in the upper layer from the scoured hole. And near the bottom, reversal flow were analyzed like that in the backward facing step flow. Excessively large values of the velocity gradients of the stream-wise velocity made the turbulent shear layer, which also can affect the undesirable motion of bed materials. According to the results of the previous researches, this remarkable distribution of TKE is due to the large differences of the stream-wise velocity to the water depth direction. There is a slightly cyclic motion of the flow and it will be stretched to the depth and dissipated to the downstream.
Figure 4.42 Distribution of Measuring Grid Points in Scoured Hole

(case B-Q35h144d12; at $t = 330$ hrs. later)
a) $\Delta u$ vs. $u$

![Graph a)

b) $\Delta^2 u$ vs. $\Delta u$

![Graph b)

c) $\Delta^2 u$ vs. $u$

![Graph c)

Figure 4.43 Spiked Values of Velocity Data and Confidence Ellipses
Figure 4.44 Filtered Values of Velocity Data and Confidence Ellipses
a) Stream-wise velocity distribution

![Stream-wise velocity distribution](image1)

b) Reynolds shear stress distribution

![Reynolds shear stress distribution](image2)

c) Turbulent Kinetic Energy distribution

![Turbulent Kinetic Energy distribution](image3)

Figure 4.45-a) Flow and Turbulence Distributions in Stablized Scoured Hole
(case B-Q35h144d12; at $t=330$ hrs. later)
a) Stream-wise velocity distribution

b) Reynolds shear stress distribution

c) Turbulent Kinetic Energy distribution

Figure 4.45-b) Continued (Case B-Q30h145d12)
a) Stream-wise velocity distribution

b) Reynolds shear stress distribution

c) Turbulent Kinetic Energy distribution

Figure 4.45-c) Continued (Case B-Q30h120d12)
a) Stream-wise velocity distribution

b) Reynolds shear stress distribution

c) Turbulent Kinetic Energy distribution

Figure 4.45-d) Continued (Case B-Q35h120d12)
With data of the time averaged velocity, vorticity and three dimensional velocity data were measured and analyzed spatially in the scoured hole, which was mostly stabilized for each 4 cases. At the upstream part from the $L_1$, relatively dense distributions ($\Delta x = 2 \text{ cm}$) were setup and downstream part from the $L_1$, relatively coarse distribution ($\Delta x = 5-50 \text{ cm}$) of measuring grid points were setup respectively. And also vertical intervals of measuring grid were from 2 mm to 5-20 mm from the scoured bottom (Figure 4.42).
CHAPTER 5
LOCAL SCOURING WITH MESH GRID GENERATED TURBULENT FLOW

5.1 Experimental Setup

Previously, turbulence properties at the transition is one of the dominant factors on local scouring at the downstream of the fixed. In this chapter, to analyze the effect of the turbulence at the upstream of the transition, scour tests were conducted with a setup of rectangular shape meshed wall (fully blocked along the width of the cross section). Flow pattern with this mesh grid is named as mesh grid generated turbulent flow (MGGT flow) and it can make the increase of the turbulence properties at the longitudinal transition. Schematic diagram of this setup was described in Figure 5.1.

5.2 Comparison of Flow and Turbulence at the Transition

Firstly, 3-D flow velocity data were measured at the transition in MGGT flow and analyzed with same methods, which were applied in Chapter 4. Hydraulic conditions of the test were described in Table 5.1. The range of the Froude number is from 0.256 to 0.448 and that of mean flow velocity is from 0.278 to 0.486.

Configurations of measuring flow velocity in MGGT Test were same as those in no meshed flow. Estimated values of the tests were noted in Table 5.2 and compared with the data from the no meshed flow in previous chapter (Figure 5.2 and 5.3).
Figure 5.1 Schematic Diagram of MGGT Flow and Scour Test

Table 5.1 Experimental Conditions of MGGT Flow Test at Longitudinal Transition

<table>
<thead>
<tr>
<th>case number</th>
<th>$Q$ (m³/s)</th>
<th>$h_0$ (m)</th>
<th>$U_0$ (m/s)</th>
<th>Fr (-)</th>
<th>Re ($\times 10^5$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Q20h320</td>
<td>0.030</td>
<td>0.150</td>
<td>0.278</td>
<td>0.256</td>
<td>0.333</td>
</tr>
<tr>
<td>Q30h320</td>
<td>0.035</td>
<td>0.120</td>
<td>0.417</td>
<td>0.384</td>
<td>0.500</td>
</tr>
<tr>
<td>Q30h350</td>
<td>0.030</td>
<td>0.145</td>
<td>0.333</td>
<td>0.274</td>
<td>0.500</td>
</tr>
<tr>
<td>Q32h320</td>
<td>0.020</td>
<td>0.120</td>
<td>0.444</td>
<td>0.410</td>
<td>0.533</td>
</tr>
<tr>
<td>Q35h320</td>
<td>0.035</td>
<td>0.120</td>
<td>0.486</td>
<td>0.448</td>
<td>0.583</td>
</tr>
<tr>
<td>Q35h350</td>
<td>0.035</td>
<td>0.150</td>
<td>0.405</td>
<td>0.341</td>
<td>0.583</td>
</tr>
</tbody>
</table>
Figure 5.2 Comparisons of LOW Methods at the Transition
Figure 5.2 Continued

Figure 5.3 Comparisons of TKE Methods at the transition
Table 5.2 Hydraulic Conditions of MG GT Flow Test

<table>
<thead>
<tr>
<th>case</th>
<th>$U_0$ (m/s)</th>
<th>Fr (-)</th>
<th>LOW method</th>
<th>TKE method</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td>$\tau_0$ (Pa)</td>
<td>$\delta^*$ (mm)</td>
</tr>
<tr>
<td>Q20h120</td>
<td>0.28</td>
<td>0.26</td>
<td>0.23</td>
<td>8.4</td>
</tr>
<tr>
<td>Q30h320</td>
<td>0.42</td>
<td>0.38</td>
<td>0.63</td>
<td>12.2</td>
</tr>
<tr>
<td>Q30h350</td>
<td>0.33</td>
<td>0.27</td>
<td>0.32</td>
<td>12.2</td>
</tr>
<tr>
<td>Q32h320</td>
<td>0.44</td>
<td>0.41</td>
<td>0.68</td>
<td>11.8</td>
</tr>
<tr>
<td>Q35h320</td>
<td>0.49</td>
<td>0.45</td>
<td>0.84</td>
<td>11.0</td>
</tr>
<tr>
<td>Q35h350</td>
<td>0.41</td>
<td>0.34</td>
<td>0.44</td>
<td>16.3</td>
</tr>
</tbody>
</table>
5.3 Comparison of Local Scouring

5.3.1 Temporal Development of Local Scour Hole

Three cases of scour test in MGGT flow condition were conducted and compared with those of no meshed flow condition at the upstream (Table 5.3). Median grain size of movable bed is 0.6 mm. Developments of scoured hole at each time step were similar with those of no meshed flow. Especially, a group of ripples were moving toward downstream of the maximum scour depth like same case with no meshed flow (case Q20h120d06). Scouring also of the case Q35h150d06 is similar. However frequency of the rippled bed in MGGT flow condition is smaller than no meshed flow condition (Figure 5.4).

5.3.2 Maximum Scour Depth

Development of $y_m$ in MGGT flow is slightly smaller than that of no meshed flow condition and difference in the case Q20h120d06 is largest among those experimental cases.
Table 5.3 Experimental Conditions of MGGT Scour Test

<table>
<thead>
<tr>
<th>case number</th>
<th>$Q$ (m³/s)</th>
<th>$h_0$ (m)</th>
<th>$U_0$ (m/s)</th>
<th>Fr (-)</th>
<th>Re ($*10^5$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Q20h120</td>
<td>0.030</td>
<td>0.150</td>
<td>0.278</td>
<td>0.256</td>
<td>0.333</td>
</tr>
<tr>
<td>Q35h320</td>
<td>0.035</td>
<td>0.120</td>
<td>0.486</td>
<td>0.448</td>
<td>0.583</td>
</tr>
<tr>
<td>Q35h350</td>
<td>0.035</td>
<td>0.150</td>
<td>0.405</td>
<td>0.341</td>
<td>0.583</td>
</tr>
</tbody>
</table>
Figure 5.4 Temporal Change of Bed Profiles in MGGT Flow Condition
Figure 5.4 Continued

Figure 5.5 Comparisons of the Temporal Development of Maximum Scour Depth
b) Q35h120d06

[Graph showing data for meshed and no meshed conditions over time.]

c) Q35h150d06

[Graph showing data for meshed and no meshed conditions over time.]

Figure 5.5 Continued
CHAPTER 6
FUNCTIONAL RELATIONSHIPS BETWEEN DOMINANT FACTORS AND LOCAL SCOURING

6.1 Dominant Factors on Local Scouring

Previously analyzed, dominant parameters of flow condition and sediment characteristics were suggested and compared with the scour results. Especially the difference of the turbulent shear layer thickness between fixed bed and movable is significantly dominant. Although this factor has been dominantly suggested by previous studies, Quantification of the development of this thickness has never been applied to estimate and predict the scouring and its development. And also Shields parameter has been used to predict the equilibrium state of the scoured hole.

6.2 Equilibrium-maximum Scour Depth

Equilibrium state of scouring is hard to be predicted due to the slight motions of the particles and continuous bed erosion at the downstream of the scoured hole. Therefore stabilized values from the temporal development of the maximum scour depth can be replaced to predict the maximum scale of the scour hole. This replaced values also can be applied to design of the bed protection. From the results of the experiments, regression equation was formulated as Eq. 4.17 and Figure 6.1. Using the information of the flow conditions at the longitudinal transition and bed materials at the downstream of the bed protection, Equilibrium values of the maximum scour depth can be predicted.
Figure 6.1 Empirical Relationship between Equilibrium Coefficient and the Normalized Equilibrium-maximum Scour Depth

Equilibrium-maximum Scour Depth
CHAPTER 7
SUMMARY AND CONCLUSION

In this study, experimental approaches were conducted to analyze the local scouring at the downstream of the river bed protection, which is precisely important mechanism for the safety of the upstream hydraulic structures in rivers and streams. To acquire knowledge about the physical processes playing important roles in scouring, 20 cases of flow tests and 13 cases of scour tests were performed with variations of flow condition and sediment particle sizes. From the results of the physical tests in flumes, surface properties of the bed protection, flow condition from the upstream, and sedimentological parameter were revealed as the dominant factors on local scouring. Those results, which can be described with maximum scour depth, and longitudinal length and the position, etc. can be estimated and predicted with appropriate normalized length and time scale. These scales were also represented as the flow characteristics, which is affected from the bed roughness and properties of the movable bed. From the results of 3-D velocity profiles, fully log-law developed flow converted into the backward-facing step flow in the scoured hole and excessive values of the turbulent kinetic energy in the turbulent shear layer were measured in the scoured hole. To analyze the countermeasure against the local scouring, mesh grid generated turbulent flow tests were conducted and also scour tests were performed and compared with no mesh cases.

First of all, total durations of this studies were much longer than previous experimental researches (upto 10 times of total duration of previous tests) to reveal the continuity and equilibrium state of the local scouring. And these relatively longer duration could make the regression equation of the equilibrium state of the maximum scour depth. Secondly,
previous assumption of the largest vortex size in the empirical equation of the temporal change of the maximum scour depth could be modified with the reasonable dominant factors, which were related to the flow conditions at the longitudinal transition and characteristics of the bed materials at the movable bed. Thirdly, flow and turbulence characteristics in the stabilized scoured hole were analyzed with the high-resolution velocimetry sensor, Vectrino. To analyze the turbulence, statistical method were applied in the despiking the invalid velocity data due to the variation of the flow velocity and sediment transport in the scoured hole.

From the tests, appropriate normalized equation with dominant factors on local scouring can be applied to the cases and field condition. With the prediction of the scour scale, design criteria of the bed protection and gate operation at the upstream of the bed protection will be strongly substantial.
REFERENCES


국문초록

하천 하상보호구조물 하류부에서

국부세굴에 관한 실험적 연구

서울대학교 대학원
건설환경공학부
박 성 원

하천 하상보호구조물 하류부에서 발생하는 국부세굴은 고정식 혹은 수문식 위어, 그리고 댐 여수로 등의 상류부 수리구조물의 설계 및 지속가능한 관리측면에서 매우 중요한 부분 중 하나이다. 특히 수리구조물 주변에서 발생하는 하상재료의 유실은 상류부 수리구조물의 안전성에 큰 위협이 될 수 있다. 기존 연구에서는 수치 해석적 및 실험적 연구를 통해, 국부세굴 발생의 지배인자가 시간 변화성, 흐름 및 난류특성, 그리고 하상재료의 속성 등이라고 제안된 바 있다. 하지만 연구의 부적절한 가정과 계측방법 및 모니터링의 한계로 인하여 경험식이나 예측식이 불충분하게 쓰이고 있는 실정이다.
따라서 본 연구에서는 보다 진보된 설비와 계측방식을 활용한 고정하상 하류부에서의 국부세굴 실험이 수행되었다. 본 실험적 연구는 고정하상과
이동하상의 경계지점에서 발생가능한 과도한 하상유실의 방지를 위하여, 국부세굴공의 시간발달양상과 각 시간변화에 따른 세굴공 내부에서의 흐름 및 난류특성의 분석에 초점을 맞추었다. 우선, 시간변화에 따른 하상고의 변화를 측정하여 발생가능한 최대세굴심의 예측에 사용될 수 있는 최대세굴심의 시간변화율과 수리조건과의 경험적 관계식을 수립하였다. 특히 흐름방향 경계지점에서의 수심적분된 상대난류강도값과 하상전단응력 최대세굴심의 시간변화율과 평형상태값에 지배적임을 분석하였다. 그리고 안정화된 세굴공 내부에서의 흐름 및 난류특성을 분석하기 위해서 유사한 양상을 나타내는 후면단차흐름조건에서 PIV와 ADV 계측방법을 이용하여 흐름 및 난류특성을 측정 및 분석하였다. 고해상도의 PIV 계측결과와 적분시간규모가 고려된 양상블핑균방법과 디스파이킹된 3차원 ADV 계측결과로부터 단차주변에서의 흐름 및 난류특성을 분석할 수 있었다. 이 방법을 통해 안정화된 세굴공 내부에서 발생하는 회전류와 난류전단층의 발생이 추가적인 하상재료의 유실에 영향을 미치는 것을 분석하였다.

그리고 발생가능한 최대세굴심의 적절한 방지법을 찾기 위해서, 흐름방향 경계지점에 메쉬망 난류흐름조건에서의 동일한 국부세굴실험을 수행하였다. 메쉬망 난류흐름조건을 통해 발생된 수심적분된 상대난류강도의 증가는 최대세굴심의 저감 및 지체를 야기하였다. 본 연구에서 제안된 경험식을 이용하면 기존에 알려진 수리학적 인지만으로 하천 하상보호공 직하류에서 발생 가능한 국부세굴심을 예측할 수 있으며, 또한 국부세굴심 저감을 위한
하천 하상보호공의 보완 및 설계 시에 정량적인 목표치로 활용될 수 있을 것으로 사료된다.

주요어: 국부쇄굴, 하천 하상보호공, 수심적분된 상대난류강도, 최대쇄굴심, 하상전단응력, 난류전단층, 메쉬망 난류흐름

학번: 2009-30231