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이학석사 학위논문

# Recalibrating Black Hole Mass Estimators Using High S/N Ratio Keck Spectra 

KECK 스펙트럼을 이용한<br>블랙 홀 질량 측정법 보정

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물리•천문학부 천문학 전공
박 다 우

# Recalibrating Black Hole Mass Estimators Using High S/N Ratio Keck Spectra 

# A thesis submitted in partial fulfillment of the final requirement for the degree of Master of Science 

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#### Abstract

We compare and recalibrate black hole mass estimators using a sample of 36 moderateluminosity Type 1 AGNs selected at $z \sim 0.4$. Combining the high S/N ratio Keck spectra with SDSS archival spectra, we perform a detailed multi-component spectral decomposition analysis and measure the width and luminosity of the Mg II 2798 $\AA$, $\mathrm{H} \beta$ $4861 \AA$ and $\mathrm{H} \alpha 6563 \AA$ lines, to calibrate single-epoch mass estimators. By using the best-calibrated $\mathrm{H} \beta$ line width and AGN continuum luminosity at $5100 \AA$ as reference values, we derive black hole mass ( $\mathrm{M}_{\mathrm{BH}}$ ) recipes based on various combinations of the line widths and luminosities. After applying new calibrations, mass estimators based on the combination of line dispersion and luminosity show best agreement within 0.16 dex scatter while mass estimators based on the FWHM and luminosity of emission lines are also reliable within 0.27 dex.


Keywords: black hole physics - galaxies: active - galaxies: evolution - quasars: general

Student Number: 2010 - 20389

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## Chapter 1

## Introduction

It is generally believed that the growth of supermassive black holes (BHs) is closely related with galaxy evolution as implied by the relatively tight correlations between BH mass $\left(\mathrm{M}_{\mathrm{BH}}\right)$ and galaxy properties, e.g., the $\mathrm{M}_{\mathrm{BH}}$-stellar velocity dispersion relation in the present-day universe (Ferrarese \& Merritt 2000; Gebhardt et al. 2000; Gültekin et al. 2009; Woo et al. 2010). For determining $\mathrm{M}_{\mathrm{BH}}$ as one of the most fundamental parameters in investigating the nature of BH-galaxy coevolution, various methods have been devised.

For broad-line (Type 1) AGNs, $\mathrm{M}_{\mathrm{BH}}$ can be determined from the kinematics of broad-line region (BLR), which are generally believed to be virialized by the gravitational potential of the central BH (see Peterson 1993, Park et al. 2012). By combining the measured gas velocity from the width of broad emission lines and the measured photon-travel time to BLR as the size of BLR using the reverberation mapping technique, $\mathrm{M}_{\mathrm{BH}}$ has been determined for $\sim 50$ local Seyfert 1 galaxies and QSOs based on the virial assumption (e.g., Kaspi et al. 2000; Perterson et al. 2004; Bentz et al. 2009; Denney et al. 2010; Barth et al. 2011; Grier et al. 2012).

A more popularly-used indirect method is the so-called single-epoch (SE) method, which is applicable to a large sample of AGNs based on single spectroscopic obser-
vations. Instead of direct reverberation-mapping, this method relies on the empirical relation between the BLR size and AGN continuum luminosity, enabling $\mathrm{M}_{\mathrm{BH}}$ estimation using single-epoch spectra (e.g., Wandel et al. 1999; Kaspi et al. 2000, 2005; Bentz et al. 2009). Although the uncertainties of $\mathrm{M}_{\mathrm{BH}}$ estimates from the SE method is much larger than direct reverberation measurements (see discussion by Park et al. 2012), the SE method can be applied to statistical studies of AGN $\mathrm{M}_{\mathrm{BH}}$ (e.g., Woo \& Urry 2002; Salviander et al. 2007; Treu et al. 2007 ; Bennert et al. 2011; Shen et al. 2011).

Although the SE method has been best-calibrated for $\mathrm{H} \beta$ and $\mathrm{H} \alpha$ lines since the most reverberation mapping results have provided the $\mathrm{H} \beta$ or $\mathrm{H} \alpha$ BLR size, various other broad-emission lines can be also used for estimating $\mathrm{M}_{\mathrm{BH}}$, including rest-frame UV lines (C IV and Mg II ; Vestergaard \& Peterson 2006, Wang et al. 2009, Shen \& Liu 2012), and near-IR lines ( $\mathrm{P} \alpha ; \mathrm{Kim}$ et al. 2010). For AGNs at $z>0.6$, the Balmer lines are redshifted out of optical spectral range, hence the rest-frame UV lines can substitute the Balmer lines. The Mg II $2798 \AA$ line is a prominent line for AGNs at $0.6<z<2$ (e.g., McLure \& Dunlop 2004; Woo 2008; McGill et al. 2008) while the C IV 1549Å line can be used for higher-z AGNs (e.g., Vestergaard et al. 2004; Vestergaard et al. 2006; Assef et al. 2011; Shen \& Liu 2012).

Although direct reverberation mapping results based on Mg II have not been reported due to the lack of line flux variability (Woo 2008), a Mg II-based SE estimator has been devised by calibrating AGN continuum luminosity at $3000 \AA$ with the $\mathrm{H} \beta$ emitting BLR size, and by comparing widths of Mg II and $\mathrm{H} \beta$ (McLure \& Dunlop 2002; McLure \& Dunlop 2004). Consequently, the uncertainties of $\mathrm{M}_{\mathrm{BH}}$ based on Mg II are larger than those of Balmer lines (see McGill et al. 2008, Wang et al. 2009; Shen et al. 2011).

Another source of systematic uncertainty of Mg II-based $\mathrm{M}_{\mathrm{BH}}$ comes from the complexity of the Mg II region, which is often called small blue bump (Wills et al. 1985) and presents strong Fe II features. Thus, it is necessary to subtract the Fe II for measuring
the width of Mg II. Since the measured line width of Mg II can be heavily affected by Fe ir subtraction, it is controversial how the underline Fe ir can be best removed (Bruhweiler \& Verner 2008, Tsuzuki et al. 2006, Vestergaard \& Wilkes 2001). For example, Vestergaard \& Wilkes (2001) provided a Fe in template directly obtained from the observed spectrum of the narrow line Seyfert 1 galaxy, I Zw 1, while Tsuzuki et al. (2006) developed a new template by adding the FeII emission under the Mg ir line based on photoionization model, CLOUDY (Ferland et al. 1998). Consequently, there can be large difference of Mg ir line width depending on the choice of Fe ir template, leading to systematic difference between $\mathrm{H} \beta$ and Mg ir line widths as reported by Wang et al. (2009).

Regarding gas velocity, Peterson et al. (2004) suggested that line dispersion (second moment, $\sigma_{\text {line }}$ ) of the line profile is a better velocity indicator than full width at half-maximum (FWHM) since $\sigma_{\text {line }}$ presents the virial relationship better than FWHM. FWHM measurements can be easily affected by the narrow component while line dispersions are not. In contrast, if the spectra quality is moderate as in the case of the Sloan Digital Sky Survey (SDSS) data, then the noise on the continuum can easily affect the fitting process, and wings of the line can be under/overestimated. Also, careful multi-component fitting is required for blended lines, particularly for high-mass AGNs with large line widths.

Several previous studies have calibrated various SE estimators (e.g., McLure \& Jarvis 2002; Vestergaard \& Peterson 2006; Wang et al. 2009; Assef et al. 2011; Shen et al. 2011; Shen \& Liu 2012). However, these works were based on relatively low quality spectra and mainly used the FWHM measurements for deriving SE mass estimators. Hence, detailed calibrations using line dispersion measurements based on high quality spectra are necessary to improve the SE mass estimators, and constrain the additional uncertainties introduced to other broad line estimators.

As a pilot study, McGill et al. (2008) have used high S/N Keck spectra to cali-
brate mass estimators using 19 moderate-luminosity Type 1 AGNs, and presented SE mass estimators. By enlarging the sample size and dynamical range, we present the detailed comparison of $\mathrm{H} \beta, \mathrm{H} \alpha$, and Mg II mass estimators in this paper by combining our new data with previous spectra from McGill et al. (2008). In particular, we used more sophisticated fitting procedure including stellar population models for removing stellar lines and new FeII templates for $\mathrm{Mg}_{\text {II }}$ region. We describe the sample selection, observations, and data reduction in $\S 2$, and present emission line fitting analysis and measurements in $\S 3$. Comparison between various line widths and luminosities are presented in $\S 4$, followed by the new calibrations in $\S 5$. Finally, we conclude and summarize in $\S 6$. Following cosmological parameters are used throughout the paper : $H_{0}=70 \mathrm{~km} \mathrm{~s}^{-1} \mathrm{Mpc}^{-1}, \Omega_{\mathrm{m}}=0.30$, and $\Omega_{\Lambda}=0.70$.

## Chapter 2

## Observations \& Data Reduction

### 2.1 Sample Selection

The sample was initially selected for measuring stellar velocity dispersions of AGN host galaxies to study the $M_{\mathrm{BH}}-\sigma_{*}$ relation (e.g., Treu et al. 2004; Woo et al. 2006). Readers are referred to the papers by Woo et al. (2006) and Bennert et al. (2010) for the detailed procedure of sample selection. We initially selected broad-line AGNs at $0.35<z<0.37$ with $\mathrm{H} \beta$ equivalent width and Gaussian width $>5 \AA$ from the SDSS Data Release 2 (Woo et al. 2006; McGill et al. 2008). Then, we added additional sample by limiting $\mathrm{M}_{\mathrm{BH}}$ smaller than $10^{8} \mathrm{M}_{\odot}$ to increase the dynamical range from SDSS DR7 (Bennert et al. 2010; J.-H. Woo et al. 2012 in preparation). These targets were mostly moderate-luminosity AGN, for which AGN-to-galaxy flux ratio was relatively lower, hence stellar velocity dispersions were easier to measure. The choice of redshift was made in order to prevent two major stellar absorption features, $\mathrm{Mg} b$ triplet ( $\sim 5175$ $\AA)$ and Fe ( $5270 \AA$ ), from overlapping with sky emission lines. Calibrations of SE mass estimators were studied by McGill et al. (2008) based on the initial sample of 19 AGNs. Here, we present the enlarged sample by adding 18 lower $\mathrm{M}_{\mathrm{BH}}$ AGNs (see Bennert et al. 2010). Table 2.2 presents the properties of all targets in the enlarged sample.
Table 2.1: Target Properties

Table 2.2: Target Properties

| Name <br> (1) | $\begin{gathered} \mathrm{Z} \\ (2) \end{gathered}$ | $\begin{gathered} \hline \hline \text { R.A. (J2000.0) } \\ (3) \\ \hline \end{gathered}$ | Decl. (J2000.0) <br> (4) | $\begin{gathered} \hline i^{\prime} \\ (5) \\ \hline \end{gathered}$ | Exposure (s) <br> (6) | S/N (blue) <br> (7) | S/N (red) <br> (8) | Run (9) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| S28. | 0.3679 | 161156.29 | +451610.91 | 18.63 | 5760 | 152 | 74 | 3, 4 |
| S29. | 0.3575 | 215841.92 | -011500.32 | 18.95 | 3600 | 69 | 56 | 3 |
| S31. | 0.3505 | 101527.26 | +625911.52 | 18.15 | 9000 | 249 | 78 | 8, 9 |
| SS1. | 0.3566 | 080427.98 | +52 2306.21 | 18.55 | 9000 | 235 | 26 | 5 |
| SS2. | 0.3672 | 093455.60 | +051409.15 | 18.82 | 7200 | 122 | 32 | 5 |
| SS4. | 0.3630 | 095850.15 | +4003 42.33 | 18.74 | 5400 | 175 | 65 | 8 |
| SS5. | 0.3733 | 100706.25 | +084228.41 | 18.69 | 3600 | 97 | 46 | 8 |
| SS6. | 0.3584 | 102103.57 | +30 4755.87 | 18.92 | 5400 | 127 | 49 | 8 |
| SS7. | 0.3618 | 104331.50 | -010732.88 | 18.82 | 5400 | 161 | 56 | 8 |
| SS8. | 0.3656 | 104610.60 | +035031.26 | 18.45 | 9900 | 359 | 85 | 8, 9, 10 |
| SS9. | 0.3701 | 125838.71 | +455515.55 | 18.56 | 5400 | 178 | 70 | 8 |
| SS10. | 0.3658 | 133414.84 | +114221.52 | 17.83 | 3600 | 333 | 85 | 9 |
| SS11. | 0.3732 | 135226.90 | +392426.84 | 18.39 | 2400 | 178 | 48 | 9 |
| SS12. | 0.3625 | 150116.82 | +533102.13 | 17.80 | 5500 | 176 | 119 | 6 |
| SS13.. | 0.3745 | 150541.78 | +493519.99 | 18.73 | 11100 | 202 | 107 | 7, 8 |
| SS14. | 0.3706 | 211531.68 | -0726 27.50 | 19.24 | 9000 | 168 | 51 | 6 |
| SS15. | 0.3595 | 014412.77 | -000610.54 | 19.46 | 8700 | 78 | 49 | 6 |
| SS17. | 0.3554 | 214410.62 | -010113.42 | 18.47 | 5400 | 286 | 63 | 6 |
| SS18....... | 0.3582 | 234050.52 | +010635.47 | 18.50 | 7200 | 253 | 65 | 6 |

### 2.2 Observations

We observed the targets using the Keck telescope between 2003 September and 2009 April as listed in Table 2.3. We used the Low-Resolution Imaging Spectrometer (LRIS) to obtain wide spectral ranges containing broad-emission lines, Mg II $(2798 \AA)$ and $\mathrm{H} \beta$ ( $4861 \AA$ ) in the blue and red CCDs simultaneously. All blue spectra were taken with the 600 lines $\mathrm{mm}^{-1}$ grism at a pixel scale of $0.63 \AA \times 0.135$ " and a velocity resolution (line dispersion) of $\sim 145 \mathrm{~km} \mathrm{~s}^{-1}$, while the spectra at red CCD were obtained with the 900 lines $\mathrm{mm}^{-1}$ grating at a pixel scale of $0.85 \AA \times 0.215$ " and a resolution of $\sim 55 \mathrm{~km} \mathrm{~s}^{-1}$. Six targets were observed with the 831 lines $\mathrm{mm}^{-1}$ grating in the red. Exposure times for each target and their $\mathrm{S} / \mathrm{N}$ are listed in Table 2.2.

Table 2.3: Journal of Observations

| Run | Date | Grating <br> $\left(\right.$ lines $\left.\mathrm{mm}^{-1}\right)$ | Slit Width <br> $(\operatorname{arcsec})$ | Seeing <br> $(\operatorname{arcsec})$ | Conditions |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $(1)$ | $(2)$ | $(3)$ | $(4)$ | $(5)$ | $(6)$ |
| 1 | 2003 Sep 3 | 900 | 1.5 | $\sim 1$ | Cirrus |
| 2 | 2004 May 14 | 900 | 1 | $\sim 1$ | Cirrus |
| 3 | 2004 May 22 | 831 | 1 | $\sim 0.8$ | Clear |
| 4 | 2005 Jul 7, 8 | $900 / 831$ | 1 | $\sim 0.7-0.9$ | Clear |
| 5 | 2007 Jan 24 | 900 | 1 | $\sim 1$ | Clear |
| 6 | 2007 Aug 18,19 | $831 / 900$ | 1 | $\sim 1-1.7$ | Clear |
| 7 | 2008 Aug 2,3 | 900 | 1 | $\sim 0.8$ | Clear |
| 8 | 2009 Jan 21,22 | 900 | 1 | $\sim 1.1-1.5$ | Clear |
| 9 | 2009 Apr 2 | 900 | 1 | $\sim 1.2$ | Cirrus |
| 10 | 2009 Apr 16 | 900 | 1 | $\sim 0.8$ | Clear |

### 2.3 Data Reduction

Spectroscopic data reductions were performed using the IRAF ${ }^{1}$ scripts developed for long-slit spectroscopic data reductions. The detailed data reductions for the red and blue were described in Woo et al. (2006) and McGill et al. (2008), respectively. Here, we briefly summarize the procedure. After a bias subtraction, cosmic rays were removed from each individual exposure using the Laplacian cosmic-ray identification software (van Dokkum 2001). Flat-fielding was performed by using internal flat images, which were taken at the location of each target. One-dimensional spectra were extracted using a 10 pixel wide aperture window, corresponding to $\sim 5 \mathrm{kpc}$ for the redshift of the targets. For blue spectra, wavelength calibration was performed using $\mathrm{Hg}, \mathrm{Ne}, \mathrm{Cd}$ arc lamp images taken in the afternoon while for red spectra, sky emission lines were used for wavelength calibration. Flux calibration was performed using spectroscopic standard stars and A0V stars. A0V stars were used for red part of our spectra, and standard star named Feige 34 was used for blue part because insufficient flux in short wavelength of A0V star caused a difficulty. A0V stars were also used for sky absorption (A-band and B-band) corrections.

After the spectroscopic flux calibration, we rescaled the flux level of the 1-dimensional spectra of each target to that of SDSS g' band and r' band photometry to compensate slit losses and other uncertainties. Finally, the Galactic extinction was corrected based on the method given in Schlegel et al. (1998). Figure 2.1 and 2.2 present the reduced Keck spectra of our sample overplotted with SDSS spectra. For the spectral region of the $\mathrm{H} \alpha$ line, only SDSS spectra were presented. Note that S16 was removed from the following analyses because of the lack of the $\mathrm{Mg}_{\text {II }}$ line, presumably due to high internal extinction.

[^0]

Figure 2.1: The rest-frame spectra of our sample. Blue and red spectra are taken by Keck LRIS, while grey and black data are from SDSS. All three spectra in each panel were calibrated their flux scale based on SDSS photometry, and extinction correction was also performed.

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Figure 2.2: Continued

## Chapter 3

## Measurements

$M_{\mathrm{BH}}$ can be determined from a single spectroscopic observation by the following equation,

$$
\begin{equation*}
\log M_{\mathrm{BH}}=\alpha+\beta \log v+\gamma \log L, \tag{3.1}
\end{equation*}
$$

where $v$ is the line width and $L$ is the luminosity of continuum or line and coefficients $\alpha, \beta$, and $\gamma$ can be empirically determined. To measure the line widths and luminosities, first we applied multi-component decomposition analysis to subtract various components underlying the broad line such as AGN power-law continuum, Fe ir emission blends, and narrow lines. After the subtraction was performed, we measured line dispersion and FWHM as BLR velocity estimators and continuum and line luminosity as BLR size estimators. Full spectral models for the $\mathrm{H} \alpha, \mathrm{H} \beta$, and Mg ir line regions are shown in Figure 3.1-3.6. The measured line and continuum properties are listed in Table 3.2. Note that $\mathrm{H} \alpha$ line properties of SS 5 are omitted due to the poor fitting quality.


Figure 3.1: Spectral decomposition fits. Left panel: rest-frame spectra from LRIS blue ccd (black), pseudocontinuum of combined AGN power-law continuum and Fe ir model (red), model of $\mathrm{Mg}_{\text {II }}$ broad emission lines (blue). Center panel : rest-frame spectra from LRIS red ccd (black), pseudocontinuum of combined power-law continuum and Fe II model and stellar spectra model (red), He ir broad and narrow component (magenta), O iil narrow component (orange), $\mathrm{H} \beta$ narrow component (blue, thin), $\mathrm{H} \beta$ broad component (blue, thick). Right panel : near the $\mathrm{H} \alpha$ region of rest-frame spectra from SDSS DR7 (black), AGN power-law continuum (green), total $\mathrm{H} \alpha$ model (red), $\mathrm{H} \alpha$ and $\mathrm{N}_{\text {II }}$ narrow component (blue, thin), $\mathrm{H} \alpha$ broad component (blue, thick).


Figure 3.2: Continued

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Figure 3.3: Continued


Figure 3.4: Continued

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Figure 3.5: Continued

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Figure 3.6: Continued

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Table 3.1: Broad line widths \& Continuum and line luminosities

| Object | $\begin{gathered} F W H M_{H \alpha} \\ \left(\mathrm{~km} \mathrm{~s}^{-1}\right) \end{gathered}$ | $F W H M_{H \beta}$ | $F W H M_{M g I I}$ | $\begin{gathered} \sigma_{H \alpha} \\ \left(\mathrm{~km} \mathrm{~s}^{-1}\right) \end{gathered}$ | $\sigma_{H \beta}$ | $\sigma_{M g I I}$ | $\begin{gathered} L_{3000} \\ \left(10^{44} \mathrm{erg} \mathrm{~s}^{-1}\right) \end{gathered}$ | $L_{5100}$ | $\begin{gathered} L_{H \alpha} \\ \left(10^{22} \mathrm{erg} \mathrm{~s}^{-1}\right) \end{gathered}$ | $L_{H \beta}$ | $L_{M g I I}$ | $\frac{f\left(H \beta_{\mathrm{NC}}\right)}{f([O I I I] \lambda 5007)}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) | (9) | (10) | (11) | (12) | (13) |
| S01 | 4138 | 4489 | 3379 | 2570 | 2170 | 1888 | 2.15 | 1.55 | 5.96 | 1.85 | 3.52 | 0.13 |
| S02 | 3723 | 4799 | 2919 | 2344 | 2197 | 1886 | 2.28 | 1.47 | 18.9 | 2.92 | 6.02 | 0.16 |
| S03 | 2857 | 2984 | 2244 | 1938 | 1772 | 1259 | 4.92 | 2.74 | 11.7 | 3.56 | 4.50 | 0.21 |
| S04 | 2632 | 2429 | 3064 | 1217 | 952 | 1570 | 2.28 | 1.99 | 4.03 | 0.66 | 3.63 | 0.08 |
| S05 | 4316 | 4693 | 3883 | 3289 | 3390 | 2597 | 3.67 | 2.18 | 12.1 | 3.30 | 6.01 | 0.11 |
| S06 | 3608 | 4708 | 3066 | 1387 | 1632 | 1478 | 3.46 | 1.82 | 2.34 | 1.07 | 3.66 | 0.11 |
| S07 | 4129 | 4685 | 3409 | 2454 | 2631 | 1951 | 4.29 | 2.97 | 11.3 | 4.81 | 3.38 | 0.11 |
| S08 | 2685 | 3268 | 2190 | 1526 | 1406 | 1091 | 2.48 | 2.45 | 4.13 | 0.90 | 1.07 | 0.12 |
| S09 | 2746 | 2649 | 2886 | 1582 | 1672 | 1596 | 3.60 | 2.52 | 9.45 | 2.61 | 7.01 | 0.14 |
| S10 | 3575 | 4763 | 3350 | 2106 | 2224 | 1805 | 7.02 | 3.67 | 16.1 | 5.15 | 6.38 | 0.07 |
| S11 | 2529 | 2629 | 2596 | 1495 | 1434 | 1389 | 3.46 | 2.34 | 8.50 | 2.27 | 2.51 | 0.12 |
| S12 | 7212 | 9331 | 6417 | 3254 | 3656 | 2853 | 5.13 | 2.87 | 13.4 | 3.66 | 7.92 | 0.05 |
| S21 | 8013 | 7761 | 4701 | 4117 | 3874 | 2460 | 3.15 | 7.07 | 67.3 | 9.51 | 2.88 | 0.09 |
| S23 | 8123 | 9868 | 5622 | 3492 | 4515 | 2752 | 3.81 | 2.94 | 13.1 | 3.78 | 5.64 | 0.11 |
| S24 | 5667 | 7102 | 4683 | 2891 | 3046 | 2530 | 3.61 | 2.86 | 11.4 | 3.26 | 7.22 | 0.12 |
| S26 | 4245 | 5416 | 4299 | 1685 | 2615 | 1884 | 2.48 | 1.78 | 7.68 | 3.17 | 2.83 | 0.08 |
| S27 | 2039 | 2366 | 2846 | 1268 | 1330 | 1183 | 2.82 | 1.84 | 7.18 | 2.07 | 3.01 | 0.19 |

[^1]Table 3.2: Broad line widths \& Continuum and line luminosities

| Object | $\begin{gathered} F W H M_{H \alpha} \\ \left(\mathrm{~km} \mathrm{~s}^{-1}\right) \end{gathered}$ | $F W H M_{H \beta}$ | $F W H M_{M g I I}$ | $\begin{gathered} \sigma_{H \alpha} \\ \left(\mathrm{~km} \mathrm{~s}^{-1}\right) \end{gathered}$ | $\sigma_{H \beta}$ | $\sigma_{M g I I}$ | $\begin{gathered} L_{3000} \\ \left(10^{44} \mathrm{erg} \mathrm{~s}^{-1}\right) \end{gathered}$ | $L_{5100}$ | $\begin{gathered} L_{H \alpha} \\ \left(10^{42} \mathrm{erg} \mathrm{~s}^{-1}\right) \end{gathered}$ | $L_{H \beta}$ | $L_{M g I I}$ | $\frac{f\left(H \beta_{\mathrm{NC}}\right)}{f([O I I I] \lambda 5007)}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) | (9) | (10) | (11) | (12) | (13) |
| S28 | 4432 | 5051 | 5339 | 2174 | 3008 | 2427 | 2.64 | 2.35 | 6.60 | 2.47 | 3.91 | 0.10 |
| S29 | 2018 | 3430 | 3000 | 1424 | 1644 | 1724 | 2.33 | 1.48 | 5.91 | 1.47 | 3.03 | 0.19 |
| S31 | 3457 | 3913 | 3499 | 1624 | 2017 | 1964 | 3.66 | 2.84 | 9.15 | 3.11 | 3.59 | 0.12 |
| SS1 | 2239 | 2693 | 2509 | 1173 | 1556 | 1224 | 2.64 | 2.04 | 6.50 | 2.05 | 2.49 | 0.39 |
| SS2 | 2767 | 2827 | 2738 | 1352 | 1329 | 1226 | 1.80 | 1.84 | 3.20 | 1.01 | 1.77 | 0.23 |
| SS4 | 1910 | 2207 | 2271 | 1191 | 1330 | 1069 | 1.84 | 1.83 | 5.42 | 1.56 | 2.43 | 0.12 |
| SS5 | -- | 2619 | 1870 | -- | 1352 | 924 | 2.60 | 2.05 | -- | 1.02 | 0.87 | 0.24 |
| SS6 | 1734 | 1958 | 2091 | 1003 | 1065 | 829 | 2.31 | 1.46 | 3.20 | 1.28 | 1.36 | 0.25 |
| SS7 |  | 2711 | 2030 | -- | 1217 | 1092 | 2.18 | 1.69 | -- | 1.04 | 1.39 | 0.64 |
| SS8 | 2189 | 2593 | 2454 | 1448 | 1516 | 1340 | 3.30 | 2.29 | 5.56 | 2.32 | 2.69 | 0.50 |
| SS9 | 2725 | 2684 | 3031 | 1535 | 1517 | 1475 | 3.37 | 2.24 | 6.98 | 2.21 | 4.27 | 0.28 |
| SS10 | 1743 | 1797 | 1663 | 988 | 1198 | 695 | 5.21 | 4.23 | 20.1 | 5.20 | 3.79 | 0.15 |
| SS11 | 2316 | 3486 | 2639 | 1328 | 1569 | 1578 | 3.75 | 2.96 | 4.31 | 1.24 | 2.14 | 0.19 |
| SS12 | 1967 | 1888 | 1850 | 1202 | 1191 | 872 | 3.88 | 4.49 | 29.7 | 5.87 | 1.99 | 0.19 |
| SS13 | 1802 | 2210 | 2183 | 913 | 1176 | 1042 | 2.78 | 2.06 | 4.18 | 1.17 | 1.98 | 0.08 |
| SS14 | 2200 | 2082 | 2412 | 1114 | 1096 | 1073 | 1.84 | 1.09 | 2.99 | 0.89 | 1.82 | 0.14 |
| SS15 | 1454 | 1486 | 1745 | 872 | 994 | 589 | 0.56 | 0.90 | 2.33 | 0.60 | 0.18 | 0.22 |
| SS17 | 1431 | 1870 | 1925 | 815 | 963 | 825 | 3.74 | 2.21 | 5.57 | 1.66 | 2.93 | 0.34 |
| SS18 | 1842 | 1510 | 1792 | 1171 | 1008 | 819 | 3.12 | 2.34 | 3.22 | 1.12 | 1.80 | 0.88 |

### 3.1 The $\mathbf{H} \beta$ lines

Measuring the line width of $\mathrm{H} \beta$ requires careful fitting of the line profile and continuum since other emission features (e.g., $\mathrm{Fe}_{\text {II }}$, $\mathrm{O}_{\text {iII }}$, and $\mathrm{He}_{\text {II }}$ ) are often blended with $\mathrm{H} \beta$. For low luminosity AGN with relatively high host galaxy starlight, it is also necessary to subtract stellar absorption lines to precisely measure the line width of $\mathrm{H} \beta$ (Park et al. 2012). We adopt the multi-component spectral decomposition procedure described by Park et al. (2012), in order to separate the $\mathrm{H} \beta$ broad emission line from Fe II $^{\text {, } \mathrm{O}}$ iII, and Не II , and stellar absorption lines. First, we fit the pseudo-continuum, which consists of a AGN power-law continuum, blended $\mathrm{Fe}_{\text {iI }}$ feature, and stellar absorption lines. Fe ir feature was modelled by broadening the template provided from Boroson \& Green (1992), which were convolved with various Gaussian velocities, while the stellar absorption lines were modelled by broadening a simple stellar population synthesis model of Bruzual \& Charlot (2003) with solar metallicity and age of 11 Gyr. The stellar model component is essential for the accurate $\mathrm{H} \beta$ line width measurements since the stellar absorption line affects the center of the $\mathrm{H} \beta$ emission line, to which the FWHM of $\mathrm{H} \beta$ is very sensitive. The pseudo-continuum fitting is carried out in the regions of $4430 \AA-4730 \AA$ and $5100 \AA-5400 \AA$, where Fe ir feature is strong, using the non-linear Levenberg-Marquardt least-squares fitting routine mpfit in IDL (Markwardt 2009). The blue side window is slightly adjusted to avoid the $\mathrm{H} \beta$ or $\mathrm{H} \gamma$ contamination if necessary. When the broad He ir line is clearly separated from the $\mathrm{H} \beta$ profile, a double Gaussian model for the broad and narrow components of He in $4686 \AA$ line was simultaneously fitted with the pseudo-continuum. Then, we subtract the pseudocontinuum model from the observed rest-frame spectra.

After the pseudo-continuum subtraction, we model the [ O III] $5007 \AA$ line with a tenth order Gauss-Hermite series to account for the significant blue wing of [ $\left.\mathrm{O}{ }_{\mathrm{III}}\right]$ line profile, then use the same model for [ $\mathrm{O}_{\text {III }}$ ] 4959£ by scaling the flux by $1 / 3$. For $\mathrm{H} \beta$, we fit the broad component with a sixth order Gauss-Hermite series while we used the

O iII model for the narrow component of $\mathrm{H} \beta$ using a scale factor as listed in Table 3.1. When the $\mathrm{H} \beta$ line is blended with the $\mathrm{He}_{\text {II }}$ line, Не it broad and narrow components were fitted together with $\mathrm{H} \beta$.

Based on these models, we measured the FWHM, line dispersion $\left(\sigma_{\mathrm{H} \beta}\right)$, and luminosity of the $\mathrm{H} \beta$ broad component. $L_{5100}$ was measured by averaging the flux between $5050 \AA \sim 5150 \AA$. Center columns of Figure 3.1-3.6 presents the observed H $\beta$ region and the best-fit models for each component.

### 3.2 The H $\alpha$ lines

Measuring the width of $\mathrm{H} \alpha$ is simpler than that of $\mathrm{H} \beta$ since $\mathrm{H} \alpha$ is stronger than $\mathrm{H} \beta$ and the $\mathrm{Fe}_{\text {ir }}$ feature is relatively weak in the $\mathrm{H} \alpha$ region. Since we are using relatively low quality SDSS spectra for fitting $\mathrm{H} \alpha$, we do not attempt to fit the stellar absorption lines or $\mathrm{Fe}_{\text {II }}$ feature. Instead, a featureless power-law can fit the observed continuum relatively well. Unfortunately, the $\mathrm{H} \alpha$ line is located at the red end of the SDSS spectral range due to the redshift of the sample. Thus, we model the continuum with a linear function using the rest frame $6100 \AA-6300 \AA$ region only. This region is relatively far from the blue wing of $\mathrm{H} \alpha$, consequently not affected by the wings of $\mathrm{H} \alpha$.

The $\mathrm{H} \alpha$ broad emission line is blended with the narrow $\mathrm{H} \alpha$ line, $\mathrm{N}_{\text {II }} 6548 \AA$, $\mathrm{N}_{\text {II }}$ $6583 \AA$, and also with two $\mathrm{S}_{\text {II }}$ lines at $6716 \AA, 6731 \AA$ in broader $\mathrm{H} \alpha$ targets. Given the low quality of SDSS spectra, the detailed Gauss-Hermite series modelling of narrow line components did not improve the fitting result. Thus, we modelled all narrow emission lines as a single Gaussian component by fixing the width of narrow lines as same as the velocity of the narrow $\mathrm{H} \beta$ line, which is already determined from the $\mathrm{H} \beta$ region. In the $\chi^{2}$ minimization process, all narrow line widths are fixed while their flux peaks are treated as free parameters with a constant flux ratio of 3 between two $\mathrm{N}_{\text {il }}$ lines. We simultaneously fit all narrow lines and the broad $\mathrm{H} \alpha$ line using single Gaussian models and a Gauss-Hermite series, respectively. Then, we measure the FWHM, line


Figure 3.7: A comparison of Mg it line profiles when the Fe ir emission blends are subtracted using the template from Vestergaard \& Wilkes 2001 (blue) and Tsuzuki et al. 2006 (red), respectively.
dispersion, and luminosity of the broad $\mathrm{H} \alpha$ line from the best line profile model. Right columns of Figure 3.1-3.6 presents the observed $\mathrm{H} \alpha$ line and the best-fit model.

### 3.3 The $\mathrm{Mg}_{\text {п }}$ lines

To measure the $\mathrm{Mg}_{\text {II }}$ line widths, we first subtract power-law continuum and Fe if emission features by fitting the continuum window of $2600 \AA-2750 \AA$ and $2850 \AA-$ $3090 \AA$. Then, we fit the Mg II line with a sixth order Gauss-Hermite series. A narrow component of $\mathrm{Mg}_{\text {II }}$ is not modelled because there is no significant feature implying the existence of narrow line.

On the other hand, we note that a careful treatment is required when dealing with Fe in emission in the region of $\mathrm{Mg}_{\text {if }}$ line. The Fe ii template provided by Vestergaard \& Wilkes (2001) has been popularly used (e.g., Fine et al. (2008), Vestergaard \& Osmer


Figure 3.8: Measured Mg iI line widths after Fe iI and continuum subtraction using different templates. Slopes of regression line are marked as numbers in each panel Upper left : FWHM of Mg II and $\mathrm{H} \beta$ after the subtraction of Tsuzuki template. Upper right : FWHM of $\mathrm{Mg}_{\text {II }}$ and $\mathrm{H} \beta$ after the subtraction of Vestergaard \& Wilkes template. Lower left : Line dispersion $(\sigma)$ of Mg iI and $\mathrm{H} \beta$ after the subtraction of Tsuzuki template. Lower right : Line dispersion ( $\sigma$ ) of $\mathrm{Mg}_{\text {II }}$ and $\mathrm{H} \beta$ after the subtraction of Vestergaard \& Wilkes template. Red dots are our measurements and small black dots are previous measurements by Wang et al. (2009) and Shen et al. (2011). Solid red lines are regression by OLS bisector method of our points, a green outlier (S04) in lower left panel was excluded in our line regression.
(2009), Shen et al. (2011)). However, the template contains no information of Fe if underneath the $\mathrm{Mg}_{\text {II }}$ line because it was directly made from the observed spectrum of the narrow line Seyfert 1 galaxy, I Zwicky 1. In contrast, Tsuzuki et al. (2006) suggested another template based on the I Zwicky 1 template by adding the Fe iI emission underneath the $\mathrm{Mg}_{\text {II }}$ line, which were calculated with the one-dimensional photoionization model, CLOUDY(Ferland et al. 1998). Therefore, we investigate the difference of line width measurements using these two different templates (see also Wang et al. 2009). Figure 3.7 compares the best $\mathrm{Fe}_{\text {iI }}$ emission models using Vestergaard \& Wilkes (2001) and Tsuzuki et al. (2006) templates, respectively for an object in our sample. The deblended Mg ir line profile is narrower and weaker when using Tsuzuki et al. (2006) template than using Tsuzuki et al. (2006) template, since Fe if emission underneath of $\mathrm{Mg}_{\text {II }}$ is removed.

To investigate which template is more appropriate, we compare the width of $\mathrm{H} \beta$ and the width of Mg II measured using two different templates. Upper two panels of Figure 3.8 compare FWHMs of $\mathrm{H} \beta$ and Mg in with different Fe ir subtractions. Comparison between FWHMs of Mg iI and $\mathrm{H} \beta$ shows non-linear proportionality and deviation from one-to-one relationship, indicating that the FWHMs of Mg II and $\mathrm{H} \beta$ are systematically different. To complement our comparison, we included available FWHM measurements from the literature. For example, Wang et al. (2009) investigated Mg ir and $\mathrm{H} \beta$ FWHMs of 495 SDSS AGNs with $S / N \geq 20$ in both lines by measuring the $\mathrm{FWHM}_{\mathrm{MgII}}$ after subtracting Fe ir based on Tsuzuki et al. (2006) template. In the case of $\mathrm{Mg}_{\text {II }}$ measurements based on the template of Vestergaard \& Wilkes (2001), we selected the sample of 4962 AGNs at $0.4 \leq z \leq 0.8$ with $S / N \geq 10$ in both emission lines from the catalog given in Shen et al. (2011) to ensure a rigorous comparison. Similar non-linear trend is present in the samples of Shen et al. (2011) and Wang et al. (2009), regardless of the template effect. As previous reported in Wang et al. (2009), these results imply that there is an intrinsic difference of the line profile or widths between
$\mathrm{H} \beta$ and Mg iI although it is beyond the scope of the current work to investigate the origin of this difference. In practice, the non-linear proportionality indicates that it is necessary to introduce the different value of coefficient $\beta$ in Eq. 3.1, in order to properly calibrate mass estimator based on $\mathrm{FWHM}_{\mathrm{MgII}}$.

Lower two panels of Figure 3.8 compare the line dispersions of Mg iл and $\mathrm{H} \beta$. In these plots, we present our measurements only since line dispersion measurements are not available in the literature. The effect of Fe ir template is clearly visible in the line dispersion comparison. When Tsuzuki template was used for measuring Mg ir line dispersion, line dispersions of $\mathrm{Mg}_{\text {II }}$ and $\mathrm{H} \beta$ show close linear relationship with a slight offset (bottom-left panel in Figure 3.8.) In contrast, there is a significant deviation from one-to-one relationship when Mg II $^{\text {line dispersion was measured using the Vestergaard }}$ \& Wilkes template. This difference is interpreted as that the line dispersion of Mg II is overestimated compared to that of $\mathrm{H} \beta$ since Vestergaard \& Wilkes template cannot properly subtract Fe in emission underlying the wings of the Mg II line as demonstrated in Figure 3.7. Therefore, we conclude that Tsuzuki temple provides more consistent line dispersion of Mg is compared to $\mathrm{H} \beta$, and decided to use Tsuzuki template for subtracting Fe if in the Mg II $^{\text {region in the following analysis. FWHM, line dispersion }}$ and line luminosity were measured from Mg i model, while $L_{3000}$ was measured from average flux between $2950 \AA \sim 3050 \AA$.

## Chapter 4

## Scaling Luminosities \& line widths

Single-epoch $\mathrm{M}_{\mathrm{BH}}$ can be described as a combination of two quantities is known, continuum luminosity and broad line width, as expressed in Eq. 3.1. We adopted the estimator based on $\sigma_{\mathrm{H} \beta}$ and continuum luminosity at $5100 \AA$ combined with the virial assumption and the size-luminosity relation from Bentz et al. (2006) as our fiducial $\mathrm{M}_{\mathrm{BH}}$ (Bennert et al. 2010). As a first step, for establishing new $\mathrm{M}_{\mathrm{BH}}$ equations for the other combinations, we investigate scaling relations among luminosities and line width, to decide $\beta$ and $\gamma$ in Eq. 3.1.

### 4.1 Line widths

As described in Section 3.3, scaling the line widths is very important to properly calibrate the $\mathrm{Mg}_{\text {II }}$ line width since it shows the systematic difference with that of $\mathrm{H} \beta$ line. For $\mathrm{FWHM}, \mathrm{Mg}$ II and $\mathrm{H} \beta$ line widths show the difference with a non-unity slope as found in many previous studies (e.g., Salviander et al. (2007), Wang et al. (2009), and Shen et al. (2011)). Upper two panels of Figure 3.8 contain a direct comparison
between FWHMs of Mg iI and $\mathrm{H} \beta$ and indicate that this trend is not stemming from the choice of template for Fe in emission. We find slightly shallower slopes than the previous results from Wang et al. (2009) and Shen et al. (2011), since they modelled the Mg ir line profile with a narrow component.

In the case of line dispersions, we could not compare our results with the previous measurements since they did not measure the line dispersion due to the low quality of spectra. Lower two panels of Figure 3.8 show a comparison between Mg iI and $\mathrm{H} \beta$ line dispersions of this work and show a clear dependency on the template used for the Fe ir subtraction. As described in Section 3.3, the subtraction using the template from Vestergaard \& Wilkes (2001) produces unbelievable line dispersion measurements due to the its lack of Fe in near $2800 \AA$ region, while the measured Mg ir line dispersion using Tsuzuki et al. (2006) template shows almost one-to-one relationship with $\mathrm{H} \beta$ line dispersion with slight systematic offset of $\sim 0.09 \mathrm{dex}$. In this comparison, we exclude one outlier, S04, because of its $\mathrm{H} \beta$ profile shows very wide flat feature under the $\mathrm{H} \beta$ even after the proper stellar and Fe in subtraction, then the measurement of $\mathrm{H} \beta$ could be underestimated.

Finally, we determine $\beta$, which properly scales the Mg II line width to the $\mathrm{H} \beta$ line widths, with the following relations,

$$
\begin{align*}
\log \left(F W H M_{M g I I}\right) & \propto 0.71 \pm 0.04 \times \log \left(F W H M_{H \beta}\right)  \tag{4.1}\\
\log \left(\sigma_{M g I I}\right) & \propto 0.98 \pm 0.08 \times \log \left(\sigma_{H \beta}\right) \tag{4.2}
\end{align*}
$$

Therefore our recipes using $\mathrm{Mg}_{\text {II }}$ line width will contain $F W H M_{M g I I}{ }^{2 / 0.71}$ or $\sigma_{M g I I}^{2 / 0.98}$ as the $\mathrm{M}_{\mathrm{BH}}$ estimator.

For Balmer lines, we simply adopt a result of Greene \& Ho (2005), who concluded a simple one-to-one relationship between $\mathrm{H} \alpha$ and $\mathrm{H} \beta$ FWHMs. Their conclusion is physically reasonable since $\mathrm{H} \alpha$ and $\mathrm{H} \beta$ emitting sources are intrinsically same. We use
$\beta=2$ in Equation 3.1 for both FWHM and $\sigma_{\text {line }}$ as our $\mathrm{M}_{\mathrm{BH}}$ estimator.

### 4.2 Luminosities

Based on previous reverberation mapping studies (i.e., McLure \& Jarvis 2002; Kaspi et al. 2005; Bentz et al. 2009), an empirical relation was derived for substituting a BLR size with AGN luminosities. Series of studies suggested a possibility of Balmer line luminosity instead of continuum luminosity a proxy for the BLR size $M_{B H}$ estimators (e.g., Greene \& Ho 2005, Vestergaard \& Peterson 2006). McGill et al. (2008) adopted this concept with the Mg ir line luminosity. We tried to verify the reliability of line luminosities for $\mathrm{M}_{\mathrm{BH}}$ estimators using our enlarged sample.

In this section, we compared several continuum and line luminosities with the best studied $L_{5100}$ in our data set, then extended the size-luminosity relation to other luminosities based on this comparison. Our comparisons of all measured luminosities are plotted in Figure 4.1. Prior to calculating the slope, we excluded two objects, S21 and SS15, from the $L_{5100}-L_{3000}$ comparison plot since they showed high internal extinction spectra.

However, this direct luminosity comparison contains an intrinsic problem due to the high stellar light contamination. Since stellar light contamination is not negligible, $L_{5100}$ of low luminosity AGNs are relatively higher than other luminosities , i.e., $L_{3000}$ and line luminosities in Figure 4.1, leading to a steep regression slope. Similar phenomenon is also found in the measurements of Shen et al. (2011) which were based on SDSS data. This result implies that our measured $L_{5100}$ contains contribution from stellar luminosities since our target AGNs have relatively higher stellar light fraction in the observed spectra. Unfortunately, this contamination still remains when we use AGN power-law luminosity to measure AGN continuum luminosity after removing stellar lights $\left(L_{5100 d e}\right)$ based on our spectral decomposition. Figure 4.2 compares luminosities between $L_{5100 d e}$ and other luminosities, and upper two panels shows the remaining


Figure 4.1: Correlations between $L_{5100}$ and other luminosities. X axises are the continuum luminosity at $5100 \AA$ obtained from spectral decomposition of LRIS red CCD spectra, while y axises are continuum luminosity at $3000 \AA$ and broad emission line luminosities. In lower left panel, black dots are 495 targets of Wang et al. (2009), specially selected from SDSS catalog. In other cases, dots are data from SDSS catalog of Shen et al. (2011), with $\mathrm{S} / \mathrm{N}$ ratio grater than 10, but the target pool is different in each panel due to the spectral range of SDSS. Solid green lines in upper panels show the relation of Greene \& Ho (2005), while solid red and black lines are regression lines of our targets and SDSS catalog obtained by OLS bisector regression analysis. Note that two green outliers, S21 and SS15, which show heavy internal extinction in Figure 2.1 and 2.2 , are excluded from our line regression in upper left and lower right panel, but two blue points, SS5 and SS12, are still included. Black dashed box in lower left panel means our arbitrary high luminosity cut for SDSS data.


Figure 4.2: Similar with Fig 4.1, but using $L_{5100}$ measured from the power-law continuum after subtracting Fe ii and stellar component
contamination.
To solve this problem and scale luminosity as a BLR size, we need to check previous results. First, for scaling Balmer line luminosities, we used the result of Greene \& Ho (2005) who selected a AGN sample with negligible host-galaxy contamination. In Figure 2 of that paper, a comparison between $L_{5100}$ and $L_{H \alpha}$ showed a slope of 1.157 , while a slope of $L_{5100}$ versus $L_{H \beta}$ was 1.133. In upper two panel of Figure 4.1, equations from Greene \& Ho (2005) are denoted as green lines, showing consistency with the highluminosity SDSS AGNs from Shen et al. (2011), for which stellar light contamination is also negligible. Thus, we decided to use the slopes from Greene \& Ho (2005) for the Balmer line luminosity scaling, leading to $\mathrm{M}_{\mathrm{BH}}$ estimators as following relations.

$$
\begin{align*}
\log \left(L_{H \alpha}\right) & \propto 1.157 \times \log \left(L_{5100}\right)  \tag{4.3}\\
\log \left(L_{H \beta}\right) & \propto 1.133 \times \log \left(L_{5100}\right) \tag{4.4}
\end{align*}
$$

For $L_{3000}$ and $L_{5100}$, we adopt an arbitrary high luminosity cut and extrapolate a regression result of higher luminosity points of SDSS catalog. In this case, the extrapolated regression is very close to one-to-one relation with small offset, and also shows consistency with our data points. Therefore estimator of $L_{5100}$ also can be adopted for $L_{3000}$. Also this consistency with $L_{5100}$ and $L_{3000}$ suggests a possibility of stellar light contamination in $3000 \AA$ from young blue stars, which can be inferred by the fact that seven of our targets show star formation rate by $3.3 \mu \mathrm{~m}$ polycyclic aromatic hydrocarbon emission (Woo et al. 2012).

Finally, for the $L_{\text {MgII }}$ in lower right panel in Figure 4.1, measurements are taken from Wang et al. (2009) since they used the same Fe ir template for measuring the Mg ir line width and luminosity. Similar to the $L_{3000}$ case, regression based on Wang et al. (2009) shows a slope almost one, then it is reasonable to conclude that $L_{M g I I}$ and $L_{5100}$ have similar relation with BLR size.

Based on comparison that we have presented in this section, we determine $\gamma$ for each luminosity: 0.448 for $\mathrm{H} \alpha, 0.457$ for $\mathrm{H} \beta$ using Equation 4.3 and 4.4 , and 0.518 for $L_{3000}$ and $L_{\mathrm{MgII}}$ because regressions between $L_{5100}$ and these luminosities are almost 1 . slopes in Figure 4.1 are almost 1.

## Chapter 5

## Calibrating $\mathrm{M}_{\mathrm{BH}}$ estimators

In this section, we finally calibrate the normalization constant $\alpha$ in Equation 3.1, for each line width and luminosity combination, and determine $\mathrm{M}_{\mathrm{BH}}$ estimators. We fix the values $\beta$ and $\gamma$ obtained from Section 4.1 and 4.2 and then determine $\alpha$ by fitting $\mathrm{M}_{\mathrm{BH}}$ estimates from each estimator with the best $\mathrm{M}_{\mathrm{BH}}$ using $\chi^{2}$ minimization method. As noted in Section 4, we use the $\mathrm{M}_{\mathrm{BH}}$ estimated with $\sigma_{H \beta}$ and $L_{5100}$ as the best $\mathrm{M}_{\mathrm{BH}}$ because the $\mathrm{H} \beta$ line is the best-calibrated broad emission line based on the reverberation mapping data. Newly determined $\mathrm{M}_{\text {BH }}$ with the determined $\alpha$ are shown in Figure 5.1 and 5.2.

## 5.1 $\mathrm{M}_{\mathrm{BH}}$ recipes for Balmer lines

In Figure 5.1, we plotted our calibrations for $\mathrm{H} \alpha$ and $\mathrm{H} \beta$ emission lines. The value of $\alpha$ is estimated from this comparison fit while the $\beta$ is fixed to be 2 and the $\gamma$ has the value from Section 4. Note that the rms scatter, which is given in the lower-right corner of each panel, reflects uncertainty of the newly derived mass estimators Although $L_{5100}$ shows the best agreement, $L_{H \alpha}$ and $L_{H \beta}$ give relatively good agreement with a scatter of $<0.16$ dex. For the velocity estimator, line dispersion ( $\sigma_{\text {line }}$ ) usually shows less scatter than FWHM, but the difference between $\sigma_{\text {line }}$ and FWHM is not remarkable


Figure 5.1: Cross-calibration fitting between newly derived $\mathrm{M}_{\mathrm{BH}}$ and fiducial mass with estimators from Balmer lines. X axis data points represent our target's fiducial mass, while y axis data points are $\mathrm{M}_{\mathrm{BH}}$ from $\alpha+\beta \log v_{1000}+\gamma \log L . v_{1000}$ means velocity estimator using $1000 \mathrm{~km} \mathrm{~s}^{-1}$ unit, L is luminosity estimator having $10^{44} \mathrm{erg} \mathrm{s}^{-1}$ unit for continuum or $10^{42} \mathrm{erg} \mathrm{s}^{-1}$ unit for emission line. $\beta$ and $\gamma$ in each panel depend on a kind of estimators which are shown in upper and left part of figure, and $\alpha$ is estimated by $\chi^{2}$ minimization fitting.
except for $\mathrm{H} \beta$.
By comparing our result with the Table 3 of McGill et al. (2008), we find an improvement of our result. In addition to enlarging the sample size and dynamical range, scatters of newly derived $\mathrm{M}_{\mathrm{BH}}$ are reduced by $0.05-0.15$ dex compared to McGill's result and the signs of systematic uncertainty also disappeared.

## $5.2 \mathrm{M}_{\mathrm{BH}}$ recipes for $\mathrm{Mg}_{\text {i৷ }}$ line

We compared $\mathrm{M}_{\mathrm{BH}}$ from $\mathrm{Mg}_{\text {II }}$ lines with that from $\mathrm{H} \beta$ in this section. Differing from the calibration of Balmer lines, we used the scaled value for the $\beta$ derived from Section 4 but not $\gamma$ because there are not negligible difference between the line widths from $\mathrm{Mg}_{\text {II }}$ and $\mathrm{H} \beta$. A result of calibrating $\mathrm{Mg}_{\text {II }}$ estimators is shown in Figure 5.2. Although Mg ir based $\mathrm{M}_{\mathrm{BH}} \mathrm{s}$ show more scatter than the those of the Balmer lines, each combination shows good correlation with the fiducial $\mathrm{M}_{\mathrm{BH}}$ with the scatter of $<0.27$ dex, suggesting more reliable $\mathrm{M}_{\mathrm{BH}} \mathrm{s}$ compared with the recipes from McGill et al. (2009) with $0.03 \sim$ 0.05 dex less scatter. This also shows possibility of using Mg iI line luminosity as a BLR size indicator in an $\mathrm{M}_{\mathrm{BH}}$ estimators.

In addition,we find another interesting fact about $\mathrm{M}_{\mathrm{BH}}$ based on $\mathrm{Mg}_{\mathrm{II}}$. Regarding the uncertainty of FWHM - based $\mathrm{M}_{\mathrm{BH}}$ and $\sigma_{M g I I}$ based $\mathrm{M}_{\mathrm{BH}}$, the latter is consistent with the fiducial $\mathrm{M}_{\mathrm{BH}}$ with $\sim 0.4$ dex scatter although the difference is not significant in case of $\mathrm{H} \alpha$, which is probably due to the lower quality SDSS spectra. Considering the quality of our spectra, we suggest that a reliability of $M_{B H}$ will be $\sim 15 \%$ improved when using $\sigma$, especially for high $\mathrm{S} / \mathrm{N}$ spectra.

By comparing with previous studies of the $\mathrm{Mg}_{\text {II }}$ line, we obtained better agreement with $\sim 0.5$ dex larger mass range and twice larger sample compared with McGill et al. (2008). The luminosity range of our samples is $\sim 0.7$ dex lower than that of Wang et al. (2009), providing $\mathrm{M}_{\mathrm{BH}}$ recipes for low luminosity AGNs.


Figure 5.2: Cross-calibration fitting between the newly induced $\mathrm{M}_{\mathrm{BH}}$ and fiducial mass with estimators from $\mathrm{Mg}_{\text {II }}$ lines. The equation of $\mathrm{M}_{\mathrm{BH}}$ can be represented as a combination of estimators and $\alpha, \beta$ and $\gamma$. It is noticing that S21 and SS15 are not included in this analysis.

## Chapter 6

## Summary

In this paper, we have presented a calibration of $\mathrm{M}_{\mathrm{BH}}$ estimators using Keck and SDSS spectra of 35 AGNs at $\mathrm{z}=0.36$ with BH masses of $10^{7.5-9} M_{\odot}$. Our results are summarized as follows:
(1) In Section 3, we analyzed three major broad emission lines, $\mathrm{H} \alpha, \mathrm{H} \beta$, and Mg II with a multi-component spectral analysis method. AGN power-law continuum, Fe II emissions, and stellar spectra are removed if necessary, then the pure broad emission line was fitted with the Gauss-Hermite series. We measured FWHM, line dispersion, and luminosity of each broad emission line. There is found a systematic difference of Mg II line widths depending on the choice of Fe II templates applied.
(2) By comparing the line width and luminosity measurements from our data and previous works, we determined scaling coefficient of each luminosity and velocity estimators in Section 4, i.e, $F W H M_{H \beta} \propto F W H M_{M g I I}{ }^{1.408}, \sigma_{H \beta} \propto \sigma_{M g I I}{ }^{1.020}$ and $L_{5100} \propto L_{H \alpha}{ }^{0.864}, L_{H \beta}{ }^{0.883}$.
(3) We performed a cross-calibration of newly derived equations in Section 5, based on various combinations of velocity and luminosity indicators measured from $\mathrm{H} \alpha \mathrm{H} \beta$ and Mg ir lines. Setting $\mathrm{M}_{\mathrm{BH}}$ estimated with $\sigma_{H \beta}$ and $L_{5100}$ as our fiducial mass, we determined an uncertainty of each estimator by quantifying a scatter of new $\mathrm{M}_{\mathrm{BH}}$
estimates compared to the fiducial $\mathrm{M}_{\mathrm{BH}}$ estimates. All combinations using Balmer lines provide reliable equation with a scatter less than 0.16 dex. Especially the combinations of the continuum luminosity and line dispersion show the best reliability. For Mg ir, a combination of $L_{3000}$ and $\sigma_{M g I I}$ gives the best reliability with 0.16 dex scatter, but other combination with $F W H M_{\mathrm{MgII}}$ or $L_{\mathrm{MgII}}$ are more uncertain with scatter $\sim 0.27$ dex. Our result suggests that $\mathrm{M}_{\mathrm{BH}}$ based on $\sigma_{\text {line }}$ is more reliable than that based on FWHM, especially with good quality spectra. These new single - epoch $\mathrm{M}_{\mathrm{BH}}$ estimators will be useful to study AGN in broad range of luminosity and mass.

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## 요 약

21 세기 들어 대부분의 은하의 중심에 거대 블랙홀이 위치한다는 사실이 널리 받아 들여 지고 있다. 이런 블랙홀들은 단지 존재할 뿐 아니라 모 은하와 다양한 상관 관계를 보임으로 인해 모 은하의 진화에도 밀접하게 연관되어 있으리라 여겨지고, 따라서 거대 블랙홀을 연구하는 것은 은하 자체를 연구하는 데에 있어서도 중요한 부분이다.

많은 선행 연구를 통해, 블랙홀의 질량은 활동성 은하핵의 경우 넓은 방출선의 선폭 과 연속선 또는 방출선의 광도의 조합으로 나타낼 수 있다는 사실이 알려지게 되었다. 이 연구에서는 적색 편이 0.4 정도에 위치하는 36 개의 타입 1 활동성 은하핵을 분광 관측하여 그 중심에 있는 거대 블랙홀의 질량을 추산하는 여러 방법들을 비교 분석하 였다. 켁 망원경으로 관측하여 신호 대 잡음 비가 100 을 넘어서는 좋은 관측 자료와, 공개된 자료인 슬로안 디지털 하늘 탐사(Sloan Digital Sky Survey, SDSS) 에서 얻은 자료를 합하여 우리는 활동성 은하핵의 주요한 넓은 방출선들인 $\mathrm{H} \alpha 6563 \AA, \mathrm{H} \beta 4861$ $\AA$, 그리고 $\mathrm{Mg}_{\text {II }} 2800 \AA$ 의 세 방출선을 모든 대상에 대해 얻을 수 있었다.

가장 믿을 만한 블랙홀 질량을 제공한다고 여겨지는 $\mathrm{H} \beta$ 의 속도 분산과 $5100 \AA$ 의 연속선 광도로 구성되는 블랙홀 질량을 기준으로 하여 우리는 측정한 여러 방출선들의 선폭(Full-width at half maximum, FWHM) 과 속도 분산, 연속선 광도와 방출선 광도 를 여러 가지 방식으로 조합하여 다양한 블랙홀 질량 공식을 이끌어 내었으며, 시험해 본 모든 조합의 블랙홀 질량 공식이 기준이 되는 질량과 비교하였다. 발머 계열 방출 선을 이용한 블랙홀 질량들은 기준 질량과 비교하여 로그 단위에서 0.2 미만의 데이터 분산을 보였고, 마그네슘 라인을 이용한 블랙홀 질량 공식은 발머 계열의 신뢰도보다 다소 떨어지긴 하지만 로그 단위로 0.27 미만의 데이터 분산을 보임으로써 우리가 새로 이끌어낸 블랙홀 질량들이 신뢰할 만함을 입증하였다.

## 주요어:블랙홀 — 은하: 활동성 은하핵 — 은하: 진화 — 퀘이사

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[^0]:    ${ }^{1}$ IRAF is distributed by the National Optical Astronomy Observatories, which are operated by the Association of Universities for Research in Astronomy, Inc., under cooperative agreement with the National Science Foundation (NSF).

[^1]:    Col. (1): Target ID. Col. (2): FWHM of $\mathrm{H} \alpha$ line measured on the Gauss-Hermite model fit to SDSS data. Col. (3): FWHM of $\mathrm{H} \beta$ line measured on the Gauss-Hermite model fit to LRIS red data. Col. (4): FWHM of Mg il line measured on the Gauss-Hermite model fit to LRIS blue data. Col. (5): line dispersion of $\mathrm{H} \alpha$ line measured on the Gauss-Hermite model fit to SDSS data. Col. (6): line dispersion of Gauss-Hermite model fit to LRIS blue data. Col. (8): Rest-frame luminosity at $3000 \AA$ Col ( 9 ): Rest-frame luminosity at $5100 \AA$. Col. (10): Rest-frame luminosity of $\mathrm{H} \alpha$ line. Col. (11): Rest-frame luminosity of $\mathrm{H} \beta$ line. Col. (12): Rest-frame luminosity of Mg iI line. Col. (13): Ratio between $f\left(\mathrm{H} \beta_{\mathrm{NC}}\right)$ and $f\left(\left[\mathrm{O}_{\mathrm{III}}\right] \lambda 5007\right)$.

