We describe the use of finite state automata for the description of natural languages. We demonstrate the use of this model of grammar through linguistically varied examples, from time adverbials and sentential determiners to elementary sentences of a lexicon-grammar.

1. Models of Grammar

N. Chomsky (1955, 1956) gave a discussion of formal models of grammars and concluded that neither finite-state grammars nor phrase structure grammars (context-free or context sensitive) were adequate to describe natural languages. N. Chomsky’s mathematical ‘proof’ proceeds by showing that the description of certain syntactic phenomena requires formal devices that are beyond the power of those he criticized. Chomsky used examples that he singled out for the purpose of the discussion. However, a careful analysis of these examples indicates that they can well be considered as exceptional linguistic structures, hence they could be treated independantly of the bulk of syntactic phenomena.

To show the inadequacy of finite-state grammars, Chomsky invokes the phenomenon of self-embedding, that is, the relative clause embedding of the examples:

\[ \text{The cake was stale} \]
\[ \text{The cake (that the rat ate) was stale} \]
\[ \text{The cake (that the rat (that the cat killed) ate) was stale} \]

It is true that the rule that embeds relative clauses whose pronoun is an object is recursive. But it is also clear that with respect to understanding, embedding has to be limited to depth 3 at most. What is more interesting is that this recursive phenomenon seems unique: outside of this particular
type of relative clause embedding, it is hard to find another clear-cut exam­ple. On the contrary, we mostly observe finite-state structures such as:

_The cat killed the rat that ate the cake that was stale_

We can set aside the self-embedding mechanism, either by considering it as an exception to be treated by a special device or by limiting arbitrarily the depth of embedding.

To show that context-free grammars are inadequate, Chomsky used the same type of argument, observing that coordinations involving the adverb _respectively_ cannot be correctly described by phrase-structure grammars. But again, when one investigates the structures of English (and of other well-described languages), one finds practically no other phenomena of this type, except for the construction:

_\text{Bob will work, leave or stay according to whether Jo will stay, leave or sing}_

where the verbs of each half are paired in a way that generates an un­bounded number of ‘crossing’ constraints, as shown by the paraphrase:

_If Bob works, Jo will stay, if he leaves, she will leave, if he stays, she will sing_

As a consequence, the transformational model remains the only adequate candidate for the description of these phenomena. We won’t discuss how this conclusion is logically entailed from such examples (M. Gross, 1972), we will just insist on the fact that syntactic phenomena present a large va­riety and that only very few of them, those N. Chomsky pointed out, escape the range of application of the weakest models. Along the same line of dis­cussion, G. Harman (1963) has provided convincing arguments running against Chomsky’s conclusion.

2. Finite State Graphs

Finite state automata are by now a familiar object in computational lin­guistics. Among the well-known uses of this model is the ATN system (Augmented Transition Network, W. A. Woods, 1970) and its variants, used for specific applications. From a theoretical point of view, the variety
of notational variants can be reduced to a minimal set of algebraic structures (e.g. D. Perrin, 1994).

Linguistic phenomena are represented in a natural way by the formalism of graphs. Other formalisms such as triples \((\text{State}, \text{symbol}, \text{State})\), rewriting rules: \(S_i \rightarrow a, S_j\), regular expressions or algebraic systems do not reflect as directly as graphs the word sequences to be described.

We illustrate the use of graphs\(^1\) by two examples of a different formal nature:

Example 1: Adverbial expressions that correspond to rounded dates such as in the example:

\((\text{It happened}) \text{ in the early twenties}\)

\[(\text{It happened}) \text{ in the early twenties}\]

![Diagram of a graph representing adverbial expressions]

Fig. 1

In this example, the family of adverbs corresponds exactly to all sequences that can be read from the initial (left-most) state to the final (right-most)

\(^1\) M. Silberztein (1993) has design a graphic tool FSGRAPH for the construction of such finite-state graphs and of associated parsers.
Example 2: Double conjunctions such as:

On the one hand, Bob is wrong, but on the other, one should listen to him

Moreover, the part CONJ₁ has adverbial mobility in S₁ and so has CONJ₂ in S₂:

\[ CONJ₁S₁CONJ₂S₂ \]

In Fig. 2, we did not attempt to represent the exact sentence structures. The graph simply indicates that both parts CONJ₁ and CONJ₂ can be separated by an arbitrary number of words, a feature represented by a loop (or cycle) on the variable MOT i.e. WORD). Moreover, we gave no indication in the graph about adverbial mobility, the reason being that the formalism of automata is not well adapted to the description of sentences that differ by a permutation of some of their parts.

The main difference between graphs 1 and 2 is that graph 1 is strictly finite.

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² To be complete, one should append to this graph productive forms such as in the 1970s.
³ There are examples with unbounded number of parts:
Firstly \( S₁ \), secondly \( S₂ \), thirdly \( S₃ \), etc.
nite. Such finite graphs are called DAGs (directed acyclic graphs), in contrast, graph 2 contains one cycle. Graphs without cycles (DAGs) can be seen as a natural extension of a text. A text can be considered as a flat graph, read from left to right, as in Fig. 3:

![Fig. 3]

A non trivial DAG is read in the same way, but contains possible options in the reading process: at each branching point, several texts are possible. This remark is used to represent ambiguities and variants of texts. 4

The difference between strictly finite and cyclic structures can be used to classify syntactic phenomena. For example, a good deal of the structure of noun phrases is strictly finite. Consider the general form:

(1) $\text{Prep Det } N$

where the preposition $\text{Prep}$ and the determiner $\text{Det}$ can be ‘zero’. This oversimplified global structure corresponds to a large variety of complex forms:

- $\text{Prep}$ can be a complex form such as: $\text{on behalf of}$,
- $\text{Det}$ can also be a complex determiner, such as $\text{a large number, forty of fifty}$.

Hence, (1) can correspond to the phrase:

$\text{on behalf of a large number of players}$

Moreover, the noun can be preceded by adjectives, themselves modified by adverbs:

$\text{on behalf of a large number of very well motivated players}$

In the absence of a detailed analysis of the sequence of modifiers that can precede a noun, a loose way of representing the structure is by means of the cyclic graph of Fig. 4.

4 E. Roche (1993) has represented in this way the ambiguities of texts to be parsed automatically.
However, more refined studies of the compounding process of modifiers (e.g. Z. S. Harris, 1976) show that the sequence of pre-nominal modifiers is strictly finite, this result eliminates all loops in the graph of Fig. 4. Instead, strictly finite graphs have to be built, they are much more complex, but much more precise.

**Remarks**

1. In post-nominal positions, conjoined sequences of modifiers are common, less so in pre-nominal positions. Since, constraints on conjoined units are not describable by linguistic tools, one must use loops to represent them.

2. Inserts may occur in structure (1), such as in the following form:

    *on behalf, we think, of forty of fifty players*

The insert *we think* is of a sentential nature, hence its length is unbounded, for example it could be replaced by the longer insert: *we are absolutely sure of this fact*. Longer inserts can be stylistically awkward, but they are still grammatical. It is clear that such inserts, do not belong to the structure of noun phrases. We will discuss them in a general way below in §4.

**3. Finite Constraints**

The original model of transformational grammar proposed by Z. S. Harris (1952) and the first model of generative grammar (N. Chomsky, 1955) both make a clear separation between two sentence types:

- elementary, simple or kernel sentences which constitute generators, for
- complex sentences.

In these models, unary transformations affect the elementary structures and binary transformations combine simple structures into complex ones. This natural schema is also present in traditional textbooks, but has disap-
peared from the later models of generative grammar.

The study of elementary sentences can be performed in a way totally independent of the complex structures. It amounts to determining the argument structure of sentences and the possible modifications of basic argument structures by unary transformations. Descriptions of elementary structures have been systematically performed for several languages within the theory of lexicon-grammar. One important empirical result then obtained is that the maximum number of arguments of verbs is three, as for example in a sentence such as:

*Bob gave a ring to Jo*

Forms with more arguments can be observed, but they are quite restricted and may be subject to reanalysis with fewer arguments:

— there can be true exceptions such as the French idiomatic form with five arguments (all obligatory):

\((Luc)\_a\_tourné\_dans\_sabouche\_avant\_de\_parler\),

— there are remaining theoretical difficulties in separating the essential arguments of a given verb from its circumstantial ones. The latter ones are brought, in principle, into the simple sentence through binary transformations of the type:

*Bob gave a ring to Jo yesterday*

\(=\) *Bob gave a ring to Jo, this happened yesterday*

But in the following sentences with four arguments, the argument status of *for ten dollars* and of *for this ring* is not so clear:

*Bob paid ten dollars to Max for this ring*

*Bob bought this ring from Max for ten dollars*

Both *for*-complements may seem circumstantial, however their *NP* part may occur in a direct object position which is definitely an argument position of the verb. In the same way, in the sentence:

*Bob wasted ten hours on this report*

*ten hours* is a direct object but is transformationnally related to the duration complement of *write* in the complex sentence:
Bob wasted ten hours writing this report

— certain unary transformations may change the number of arguments of a sentence. The Passive transformation leaves invariant the number of arguments:

\[(Bob)_{o} \text{ attacked (the fort)},\]
\[= (The \text{ fort}), was attacked by (Bob)_{o}\]

but the nominalization:

\[(Bob)_{o} \text{ attacked (the fort)},\]
\[= (Bob)_{o} (\text{ launched} + \text{ made}) (an \text{ attack}), against (the \text{ fort})_{2}\]

increases by one the number of arguments. However, the main verbs are of a very different nature in such paired sentences: to attack is a distributional verb which constrains semantically its subject and object, whereas to launch is a support verb, namely a grammatical auxiliary with limited semantic role. Nominalizations with support verbs do not always increase by one the number of arguments, in many cases they modify the role of arguments. For example, in the relation with support verb to put:

\[(Bob)_{o} \text{ coated (the cake)}, with (chocolate),\]
\[= (Bob)_{o} \text{ put (a coating of chocolate)}, on (the cake)\]

coating, the nominal form of the verb, has for noun complement the instrument complement of the verb, that is the noun chocolate. From a syntactic point of view coating of chocolate is a single noun phrase, hence it should be counted as a single argument; consequently, both the nominal and the verbal sentences have three arguments. In the process of nominalization, an argument of a verb has become a modifier of a noun, which could be seen as having a non essential role in a sentence. Such changes in the syntactic properties of the various arguments show the complexity of the correspondance between syntactic structures and argument structures that are closer to semantic interpretation.

After a systematic study of the French lexicon, the set of kernel sentence forms appears to be the following:\(^5\)

\(^5\)In English and other languages, the structures and even their numerical proportions in the lexicon do not seem to be essentially different.
intransitive forms
2 arguments, Prep can be 'zero'.
3 arguments, Prep can be 'zero'

and marginally:

$N_0 V (Prep N)^n$, with $n$ no larger than 4.

Such a set of structures is thus strictly finite and is described in a very natural way\(^6\) by the finite automaton of Fig. 5.

The same form of automaton can be used for a different purpose. Consider the sentence with three arguments:

(\(Bob\))\(_o\) talked to (\(Jo\))\(_o\), about (\(the\) \(ring\))\(_z\)

the complement arguments are not obligatory, and the following forms are also accepted as sentences:

(\(Bob\))\(_o\) talked to (\(Jo\))\(_o\),
(\(Bob\))\(_o\) talked about (\(the\) \(ring\))\(_z\),
(\(Bob\))\(_o\) talked

The automaton of Fig. 5 can represent this set of four sentences. However, this set is only valid for \(to\) talk, we need a different automaton for \(to\) mention, which has the different paradigm:

\(Bob\) mentioned the ring to \(Jo\)

\(^6\) It should be noted that the graph makes explicit the structural invariance of the sequence $N_0 V$, common to all sentences. This observation should be opposed to the insistence of linguists to consider the VP structure (verb phrases) as a universal invariant.
Bob mentioned the ring

* Bob mentioned to Jo

* Bob mentioned

As a consequence, to represent the optional or obligatory status of arguments of verbs, the general automaton of Fig. 5 must be lexically specified: the verb and the prepositions must be made explicit and the nature of the arguments clearly specified, which is the case in the matrix representations of the lexicon-grammar (M. Gross, 1975). This method of representation can be extended to other structures, for example to the structures obtained through transformations. This possibility directly derives from the nature of lexicon-grammar. Let us recall the principle of the matrix representations (Fig. 6). A row of a matrix is an entry, for example a distributional verb. It is important at this stage that the various meanings of the entry word, that is the word form appearing in editorial dictionaries, have been clearly separated.\(^7\) The argument structure of verbs has been used to establish a classification. For 12,000 French verbs we have defined about 50 classes (C. Leclère, 1991). Each class is represented by a specific matrix. The rows of a matrix correspond to the entries (e.g. the verbs). Columns are sentence form, for example:

- the Passive form: \(N_1 \text{be } V\text{-ed by } N_0\)
- the Impersonal form: \(it V N_0 \text{Prep } N_1\)

Hence, a transformation is a pair (unordered) of columns. The Extrapolation transformation can then be written:

\[ N_0 V \text{Prep } N_1 = it V N_0 \text{Prep } N_1 \]

That Bob would fail occurred to Jo

\(=\) It occurred to Jo that Bob would fail

At the intersection of a row (entry) and a column (sentence form), we place a `+` sign if the entry is compatible with the sentence form, a `−` sign otherwise. In this way, we associate to a given entry a set of compati-

\(^7\)For example figurative and proper meanings of a word often constitute separate entries, since in general for each meaning the set of syntactic properties differs (J.-P. Boons, 1971).
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<tr>
<th>Sujet</th>
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Fig. 6
ble sentence structures. In exactly the same way we associated above the substructures of the verbs *to talk* and *to mention* to finite automata, we can construct all the automata corresponding to all the entries of the lexicon-grammar. E. Roche (1993) has effectively constructed such automata in a highly formalized way, to the point where the automata he built can be used in automatic syntactic analysis (Fig. 7).
4. Inserts and Non-finite Constraints

If we attempt to match the basic structures described in the lexicon-grammar with sentences found in texts, many questions arise. One set of questions relates to complex sentences, answers to these questions lie in the detailed description of coordination and subordination, that is of binary transformations. Many questions are still open in this active area of research, in particular the role of the lexicon-grammar has to be determined (M. Mohri, 1993, M. Piot, 1991).

Another series of discrepancies between theoretical and observed forms is related to inserts of the type examplified in §2.

4.1. Adverbial Inserts

Let us consider an elementary structure of a general type:

(1) $N_0 Aux V Prep N_1 Prep N_2 = :$

*Bob has given a ring to Jo*

and any type of adverbial, namely *three days ago, generously, in a bar*, etc. Such adverbials may systematically occur at the juncture of the units of (1), that is next to any of the noun phrases or of the verbs. We mark these positions by a $-$ sign in:

(2) $N_0 \ Aux \ V \ Prep \ N_1 \ Prep \ N_2 \ = :$

*Three days ago, Bob has given a ring to Jo*

*Bob, three days ago, has given a ring to Jo*

*Bob has, three days ago, given a ring to Jo*

*Bob has given, three days ago, a ring to Jo*

*Bob has given a ring, three days ago, to Jo*

*Bob has given a ring to Jo, three days ago*

In general, Adverbial inserts are not permitted inside noun phrases. Some inserts are not allowed in all the $-$ positions.\textsuperscript{8}

\textsuperscript{8} The acceptability of Inserts may vary according to stylistic features. But all $-$ positions are in principle grammatical. An exception is observed with *barely*:

*Bob barely reads*

*Bob reads barely*

* Barely, Bob reads*
Adverbials have unbounded length, as in:

*the day they had decided to go to the beach*
*in the generous way his parents had always taught him*
*in a bar where several extremely serious accidents had occurred*

as a consequence, a relation between two of the sentence units of (1) can hold at any distance. For example, matching the person-number of the subject with the person-number of *Aux* may require that one the preceding lengthy insert has been recognized in the substructure *No Adv Aux.*

Performative inserts such as *I think, God knows why, as I just told my sister,* are also allowed in the same positions (M. Gross, 1990):

*God knows why, Bob has given a ring to Jo*
*Bob, God knows why, has given a ring to Jo*
*Bob has, God knows why, given a ring to Jo*

etc.

4.2. Sentential Determiners

Another syntactic process that can keep apart noun phrases from their verbs is an extension of the determiners of nouns. Common determiners such as articles (definite, indefinite), demonstrative and possessive provide a picture *Det N* of the noun phrase where a short *Det* can only be separated from its *N* by adjectives (cf. §2):

*Bob bought (the+a+this+my) car*
*Bob bought (the+a+this+my) extremely nice and inexpensive car*

In the following examples of *Det* are of a different nature:

*Bob bought God knows exactly how many cars*
*Bob bought I cannot tell you what brand of car*

The determiner sequence is sentential, and as such, it can be of any length. It is interesting to compare such determiners to the performative inserts, they are lexically related in the sense that it is the same types of main verbs that are found in both structures. But the structures are quite differ-

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9 Moreover, *Adv* may stand for more than one adverbial sequence.
ent, performative inserts can move freely between the phrases of the main structure, whereas the sentential determiner is fixed in the pre-nominal position Det of a noun phrase.

Another type of determiner generates sequences of unbounded lengths too. In principle, nominal determiners compound recursively:

- Bob bought a large number of books
- Bob bought a large number of a certain kind of books

However, very much as in the case of pre-nominal adjectives, the allowed combinations of nominal determiners are quite limited\(^\text{10}\) and even if we set aside the stylistic problem of length, it is difficult to find interpretable examples with more than three levels. The sentence:

- Bob bought a subset of a collection of a certain kind of books

is both logically correct and grammatically acceptable, but its set-theoretic relations which can be extended indefinitely do not translate into normal human discourse; the corresponding sentences belong to the language of set theory and are best phrased and interpreted by using the mathematical notations of the domain.

5. Parsing

The $^\text{2}$-positions of (2) in 4.1. introduce a difficulty in the analysis of (1). It is clear that if inserts could be recognized first, structure (1) would compare much more easily to the entry of to give in the lexicon-grammar. We advocate such a strategy of parsing, although it runs against the current attitude. Today, specialists are devising general processes as independently as possible of the specific grammatical features of the language to be parsed. Most parsers thus rely on a general model (usually some type of phrase-structure model) and algorithms that are applied (left-to-right, bottom-to top, etc.), are blind to the categorization of linguistic phenomena, even from the formal point of view we presented. For example, it is considered that phrase-structure parsing is general, powerful and efficient, be-

\(^{10}\)Examples such as:
- Bob bought a certain quantify of a large amount of books
have to be blocked.
cause it treats in the same way finite and recursive constraints between words or phrases.

Our approach consists in using formal differences observed at the empirical level. For example, we saw in §2 that sentence structures in languages that have fixed word-order can be modelled by finite-state automata in a very natural way. This is not the case for the structures with adverbial inserts we discussed in §4.1. They are best described by means of a specific permutation device that acts on a finite-state representation. In other terms, we are making more specific the early transformational models:

- kernel sentences are described in terms of finite automata,
- kernel sentences are submitted to operations that transform the finite-state graphs into other finite-state graphs.

Transformations then appear to be highly specific, we have illustrated here this feature by examples as different as the adverbial permutation and the insertion of sentential determiners of nouns, the detailed grammar of many different languages provide many more examples supporting this view.

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